



## $\partial E$

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Nuclear planetology is a new research field, tightly constrained by a coupled  $^{187}\text{Re}$ - $^{232}\text{Th}$ - $^{238}\text{U}$  systematics, which by means of nuclear astrophysics aims also at understanding the thermal evolution of Earth-like planets after Mercury-like contraction and Fermi-pressure controlled gravitational collapse events towards the end of their cooling period [1]. In nuclear planetology, Earth-like planets are regarded as old (redshift  $z > 15$ ), down-cooled and differentiated black dwarfs (Fe-C BLD's), so-called interlopers from the Galactic bulge [1], which are subjected to endoergic  $^{56}\text{Fe}(\gamma, \alpha)^{52}\text{Cr}$  (etc.) reactions (photodisintegration),  $(\gamma, n)$  or  $(\gamma, p)$  and fusion reactions like  $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ . It has recently been pointed out [1] that beside its surface temperature  $T_{eff}$  of its outer core surface, the Earth shows also striking similarity in volume  $V$  (radius  $r_{Earth} \approx 6.370$  km) with an old white dwarf star (WD;  $r_{WD} \approx 6.300$  km) like WD0346+246. This major boundary condition for nuclear planetology can be described in terms of  $V_{Earth} = V_{WD} = V_{const} = 4 \cdot \pi \cdot r^3 / 3$  ( $r_{WD} \approx r_{Earth}$ ). However, in addition to the fact that Earth is habitable, the most obvious difference between a WD and the Earth is their density  $\rho$  ( $\rho = m/V$ ;  $m$  mass,  $V$  volume): while a WD may contain  $1 M_O$  ( $M_O =$  solar mass) per  $V_{const}$ , the mass of the Earth is only a tiny fraction of this,  $\approx 3 \cdot 10^{-6} M_O$  per  $V_{const}$ . Therefore, it is crucial to understand  $\partial \rho$ , or why  $m_{Earth} \ll m_{WD}$  for  $V_{const}$ . Here I argue that the application of principles constrained by the theory of relativity [2] may offer a possible answer to this question: it is generally accepted that mass is directly related to energy,  $E = m \cdot c^2$  ( $E$  energy;  $m$  mass;  $c$  velocity of light) or  $m = E/c^2$ . From  $m \sim E$  we derive that any mass change can be described in terms of energy change [3]. Instead of  $\rho = m/V$  we may thus write  $\rho = E/c^2 \cdot V$ , and because of the special scenario  $V_{Earth} = V_{WD} = V_{const}$  discussed here, the denominator of this equation becomes a constant term  $C = c^2 \cdot V_{const} = 9.73 \cdot 10^{37} \text{ m}^5 \text{ s}^{-2}$ . From this it follows, that  $\rho = E/C$ , or  $\rho \cdot C = E$ . Therefore, we arrive at  $\rho \sim E$  for the WD/FeC-BLD case or, considering the evolution of the system over time  $t$ :  $\partial \rho / \partial t \sim \partial E / \partial t$ . Hence, concerning time integrated planetary evolution it may be concluded that any density change  $\partial \rho$  of an old stellar remnant towards a  $\approx 3 \cdot 10^{-6} M_O$  habitable Earth-like planet is a measure for the system's energy change  $\partial E$ .

[1] Roller (2016), Geophys. Res. Abstr. **18**, EGU2016-291-3. [2] Einstein (1905), Annalen d. Physik, **18**, 639-641.