



## **Implementation of numerically efficient, Coulomb friction (plastic) basal boundary conditions in a three-dimensional, higher-order ice flow model**

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Previous work has demonstrated that Coulomb friction basal boundary conditions can be efficiently implemented within two-dimensional, Shallow-Shelf Approximation (SSA, or “shelby-stream”) ice flow models in order to represent glacier sliding over plastic till (e.g. Schoof, 2006; Bueler and Brown, 2009). To date, little work has been done on exploring the implementation of this same type of basal boundary condition in fully three-dimensional, higher-order ice flow models. Here, we present an efficient method for doing so, based on methods developed for Coulomb-friction boundary conditions in elastic contact problems (e.g. Hueber et al., 2008). Analytical solutions (Raymond, 2000; Schoof, 2006) are used as targets to compare the rate of convergence for this new implementation versus that applied previously to SSA models.

### References

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