



## Influence of nonuniform solid concentration on surge occurrence of muddy debris flow and viscous debris flow

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Debris flows are classified into some types by flow mechanism. Viscous debris flow and muddy debris flow have a common important characteristic that lots of surges flow intermittently. Authors have shown that surges are generated by flow instability as same as roll waves. This paper is reported the influence of nonuniform solid concentration in the flow into surge occurrence of muddy debris flow or viscous debris flow. It is difficult to discuss a general solution of any solid concentration form in the flow. Therefore it is simplified that the flow has two different concentration layers. The concentration of a lower layer is  $C_\ell$ , thickness  $h_\ell$  from bottom to  $h_\ell$ , the concentration of an upper layer is  $C_u$ , thickness  $h_u$  from  $h_\ell$  to surface of the flow, and  $C_\ell$  is greater than  $C_u$ . From the theoretical consideration, when the concentration is nonuniform, the flow is stable than uniform concentration. A theoretical result on muddy debris flow is as follows,

$$F_r \geq \frac{1}{\sqrt{\left\{ \Phi + \left( \frac{3}{2} - \beta \right) \right\}^2 - \beta(\beta - 1)}} \quad (1)$$

here,

$$\begin{aligned} \Phi &= \left[ \sqrt{1 + \phi_m^2} - \phi_u \right] \times \left[ \sinh^{-1} \left\{ \frac{1}{\phi_m} \right\} - \sinh^{-1} \left\{ \frac{1}{\phi_u} \right\} - \sqrt{1 + \phi_m^2} + \phi_m \right]^{-1} \\ \beta &= \left[ a \left\{ 2 + \left\{ \sinh^{-1} \left( \frac{Y_0}{\phi_\ell} \right) \right\}^2 \right\} - 2 \sinh^{-1} \left( \frac{Y_0}{\phi_\ell} \right) \phi_\ell + 2 \sinh^{-1} \left( \frac{Y_0}{\phi_\ell} \right) \sqrt{\phi_\ell^2 + a^2} \right. \\ &\quad - 2 \left\{ a \sinh^{-1} \left( \frac{Y_0}{\phi_\ell} \right) + \sqrt{\phi_\ell^2 + a^2} \right\} \cdot \sinh^{-1} \left( \frac{a}{\phi_\ell} \right) + a \left\{ \sinh^{-1} \left( \frac{a}{\phi_\ell} \right) \right\}^2 \\ &\quad + 2 + \left\{ \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) \right\}^2 - a \left\{ 2 + \left\{ \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) \right\}^2 \right\} + 2 \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) \sqrt{\phi_u^2 + 1} \\ &\quad - 2 \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) \sqrt{\phi_u^2 + a^2} - 2 \left\{ \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) + \sqrt{\phi_u^2 + 1} \right\} \cdot \sinh^{-1} \left( \frac{1}{\phi_u} \right) \\ &\quad + \left\{ \sinh^{-1} \left( \frac{1}{\phi_u} \right) \right\}^2 + 2 \left\{ a \sinh^{-1} \left( \frac{Y_0}{\phi_u} \right) + \sqrt{\phi_u^2 + a^2} \right\} \cdot \sinh^{-1} \left( \frac{a}{\phi_u} \right) \\ &\quad \left. - a \left\{ \sinh^{-1} \left( \frac{a}{\phi_u} \right) \right\}^2 \right] \times \left[ \sinh^{-1} \left( \frac{1}{\phi_m} \right) - \sinh^{-1} \left( \frac{Y_0}{\phi_m} \right) - \sqrt{1 + \phi_m^2} + \phi_m \right]^{-2} \end{aligned}$$

$\phi^2 = \left( \lambda^2 \frac{a_i \sin \alpha}{\kappa^2} \right)$ ,  $\lambda = \left\{ \left( \frac{C_*}{C} \right)^{\frac{1}{3}} - 1 \right\}^{-1}$  : linear concentration,  $H = h_\ell + h_u$  : depth of flow,  $a = \frac{h_\ell}{H}$ ,  $d$  : particle size,  $k_s$  : equivalent roughness,  $b=1/30$ ,  $\beta$  : momentum correction coefficient,  $F_r$  : Froude number,  $\kappa$  : Karman constant,  $\sigma$  : density of solid particle,  $\rho_m$  : mean density of flow,  $C_*$  : concentration of packed solid particles,  $C$  : mean concentration, suffix  $m$ : mean of depth,  $\ell$ : lower layer,  $u$ : upper layer.