



## Geometric mean-field models for ilmenite-hematite solid solutions

Karl Fabian (1), Valera P. Shcherbakov (2), Peter Robinson (1), and Suzanne A. McEnroe (1)

(1) NGU, Geological Survey of Norway, Trondheim, Norway (karl.fabian@ngu.no), (2) Geophysical Observatory "Borok", Russian Academy of Science, Russia

The ilmenite-hematite solid-solution series  $\text{Ilm}X$  ( $X \text{ FeTiO}_3(1 - X) \text{ Fe}_2\text{O}_3$ ) is an important system for homogeneous or exsolved natural minerals with unusual magnetic properties. Statistical mean-field models are successful in predicting the ferromagnetic (FM) Curie temperatures  $T_C$  and  $M_S(T)$  curves of the  $\text{Ilm}X$  solid solutions. The results depend on the choice of interaction coefficients, which either have been determined by neutron diffraction measurements (Samuelson and Shirane, 1979), by Monte Carlo model fits (Harrison, 2006), or by density-functional theoretic calculations (Nabi *et al.*, 2010). To implement the varying Fe and Ti concentrations, and the random distribution of Fe ions in the solid solutions, the models either use statistical interactions between sites, whereby they effectively average over all possible configurations, or they describe specific random configurations. Both types of models will be discussed. A special class of mean-field modelling has been suggested by Ishikawa (1957), to estimate the size of interacting clusters in  $\text{Ilm}X$  beyond the FM percolation threshold ( $X > 87$ ), where global ferrimagnetic order breaks down, and only finite ferrimagnetically ordered clusters generate a pseudo-Langevin magnetization curve at temperatures between the FM Curie temperature and the antiferromagnetic Néel temperature  $T_N$ . Using a numerical inversion method, it is possible to fit measured hysteresis loops of synthetic  $\text{Ilm}X$  samples ( $X = 92, 97$ ) by improved theoretical pseudo-Langevin curves which depend on cluster-size- and exchange-interaction- distributions. Apart from statistical mean-field models, it is also possible to investigate specific atomic configurations, each corresponding to some fixed  $\text{Ilm}X$ . These models contain several tens to hundreds of ilmenite unit cells (e.g.  $3 \times 3 \times 3$  or  $5 \times 5 \times 5$ ) with periodic boundary conditions. Their main advantage is that they permit visual inspection of the geometric configuration in relation to the magnetic behaviour.