

# Transition of Dynamic Rupture Modes in Elastic Media

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Alice Gabriel<sup>1</sup>, Jean-Paul Ampuero<sup>2</sup>,  
Luis A. Dalguer<sup>1</sup>, P. Martin Mai<sup>3</sup>

<sup>1</sup> ETH Zürich

<sup>2</sup> California Institute of Technology

<sup>3</sup> King Abdullah University of Science & Technology



**ETH**

Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich



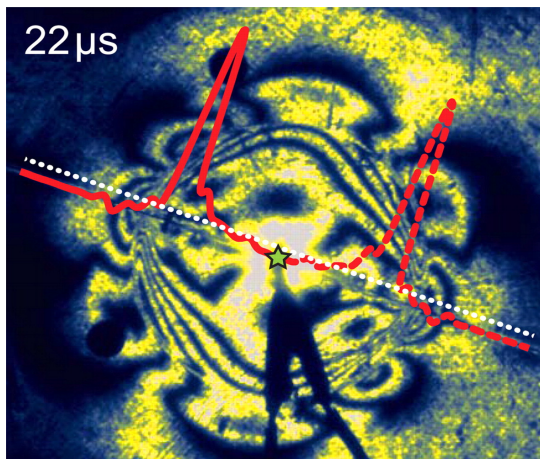
Why study rupture modes ?

- **Self-healing Pulse** vs. **Expanding Crack**

## Why study rupture modes ?

- Self-healing Pulse vs. Expanding Crack

Narrow slip-velocity pulse



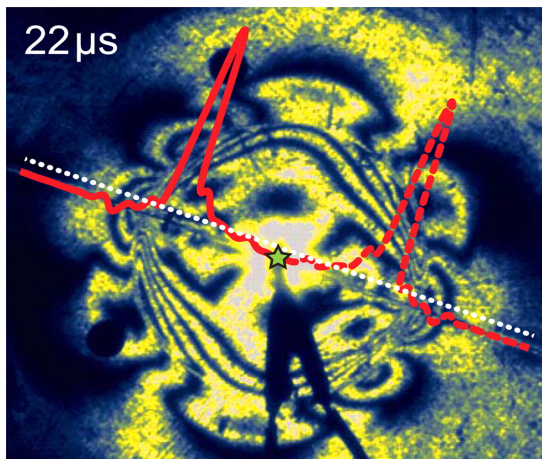
Lu, Lapusta, Rosakis, 2007

- Seismic inversions:
  - short rise times (T.H. Heaton 1990)
- Numerical simulations:
  - velocity weakening & background stress (e.g. Zheng & Rice 1998)
- High speed laboratory experiments:
  - strong friction drop & recovery

## Why study rupture modes ?

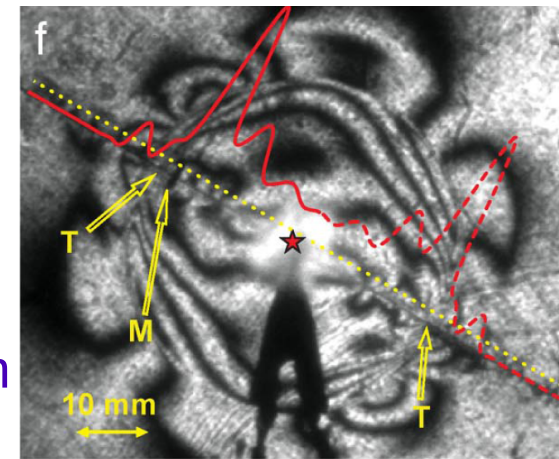
- **Self-healing Pulse** vs. **Expanding Crack**

Narrow slip-velocity pulse vs. fault sliding on entire length



Lu, Lapusta, Rosakis, 2007

- **Seismic inversions:**  
→ variable slip duration  
(e.g. Mw 8.8 2010 Chile Earthquake, Madariaga et al. 2010)
- **Numerical simulations:**  
→ velocity-independent fault strength & background stress
- **Laboratory experiments**

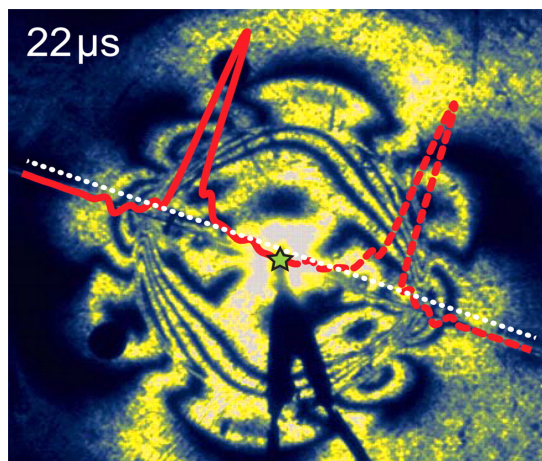


Lu, Lapusta, Rosakis, 2007

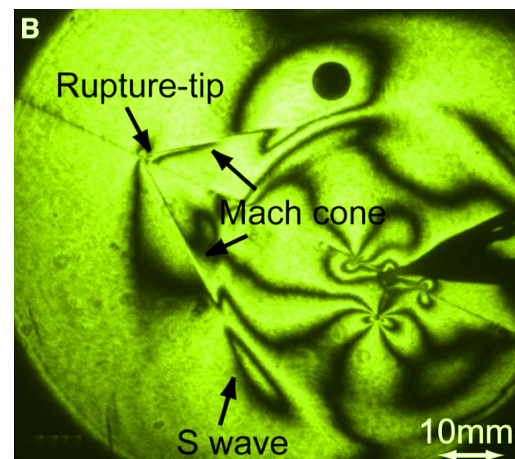
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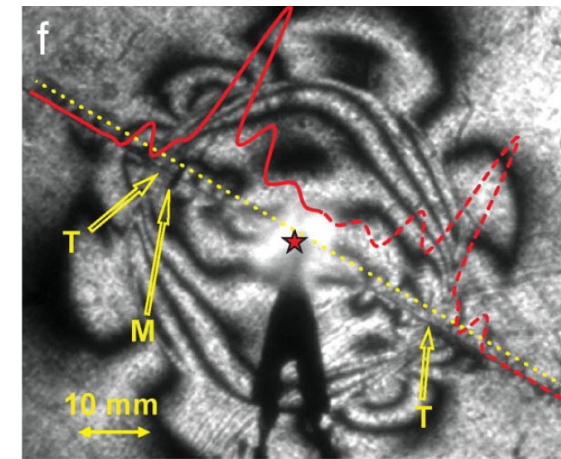
Narrow slip-velocity pulse vs. fault sliding on entire length



Lu, Lapusta, Rosakis, 2007



Xia, Rosakis, Kanamori, 2004



Lu, Lapusta, Rosakis, 2007

- Subshear vs. Supershear

Rupture speeds larger than S-wave speed

→ background stress & constitutive relation

(1979 Imperial Valley , 1992 Landers,  
1999 Izmit, Kunlunshan 2001, 2002 Denali)

## Why study rupture modes ?

- Self-healing Pulse vs. Expanding Crack

Narrow slip-velocity pulse vs. fault sliding on entire length

→ Earthquakes may not be restricted to one singular rupture mode but show **multiple rupture patterns**

→ What controls the initiation and transition of rupture modes ?

→ What are the dynamics of rupture pulses ?

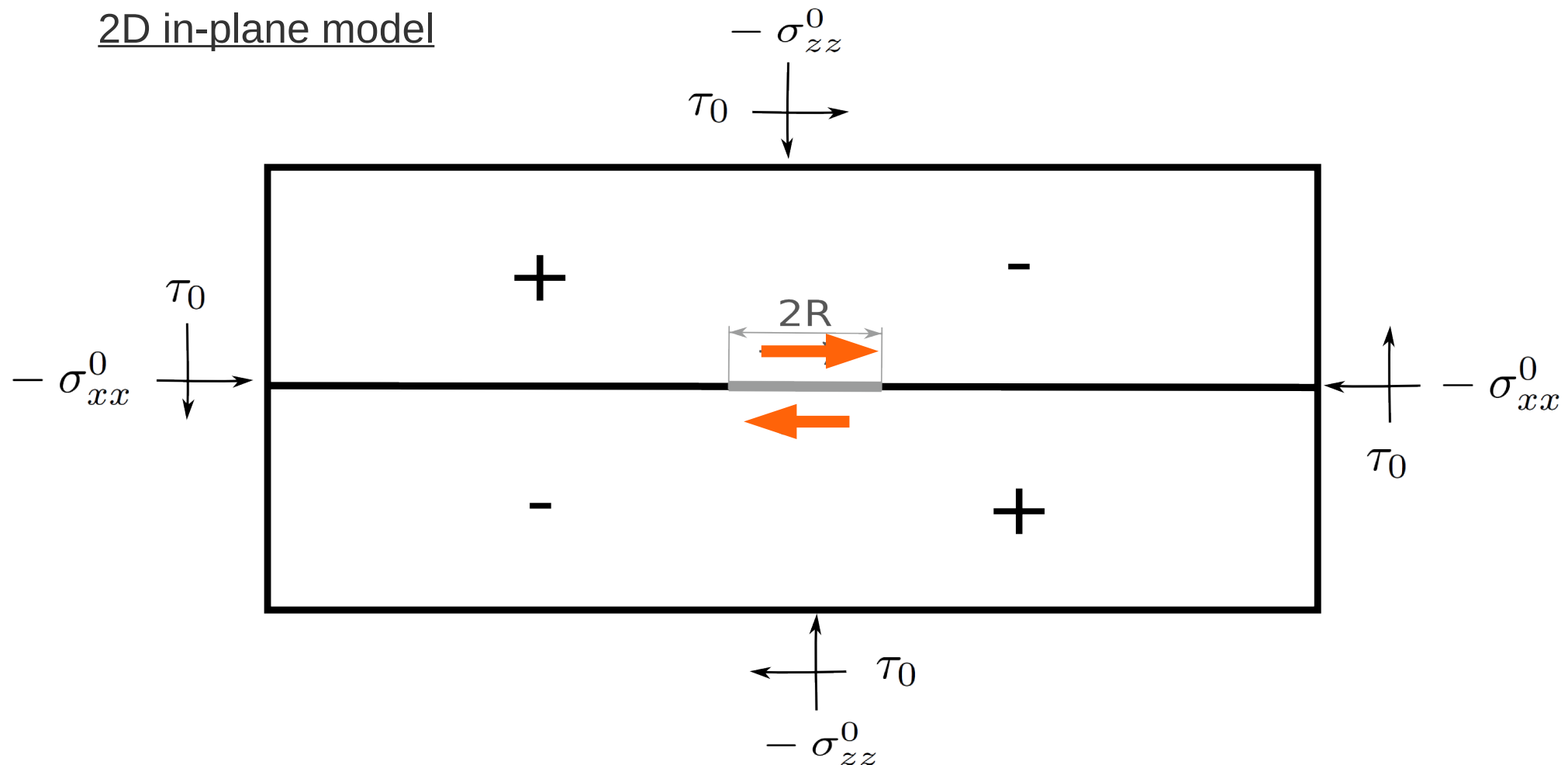
- Subshear vs. Supershear

Rupture speeds larger than S-wave speed

# Model setup

- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)

2D in-plane model

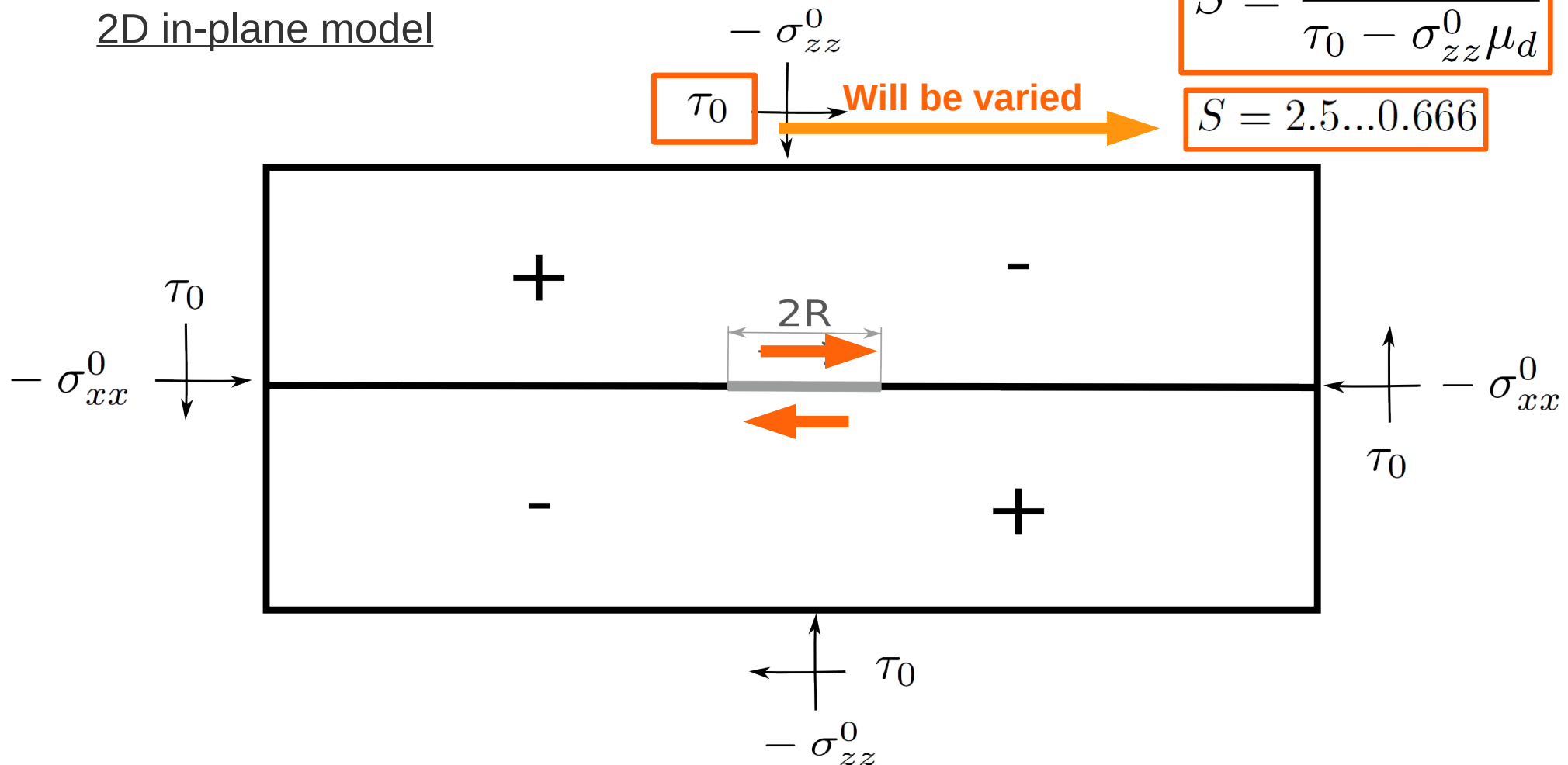


Andrews, 1976

# Model setup

- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)

2D in-plane model



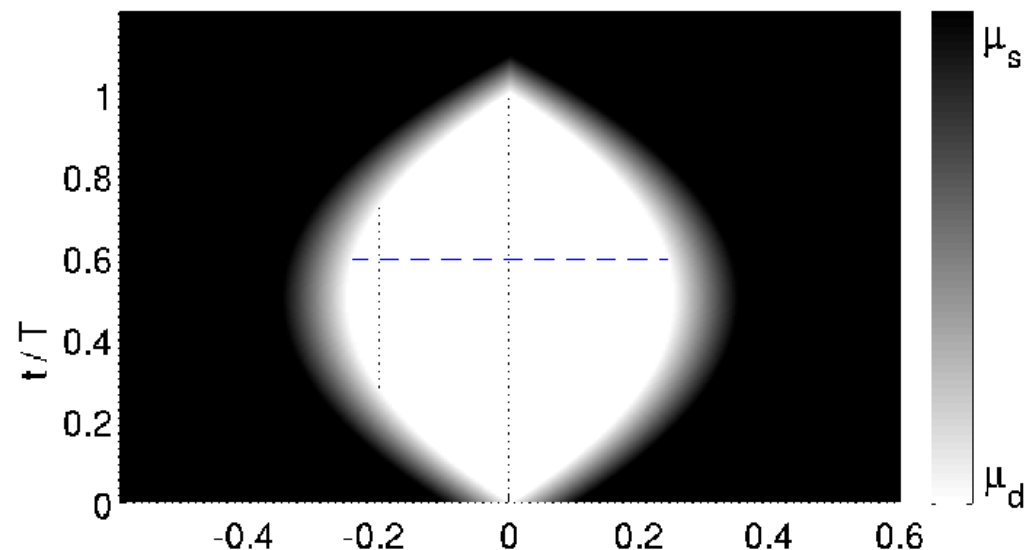
Andrews, 1976

# Model setup

- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)  
**+ 2 Nucleation procedures:** representing 2 extreme cases of frictional behavior

Prescribed time-dependent friction coefficient  $\mu_f$

a ) Nucleation procedure 1



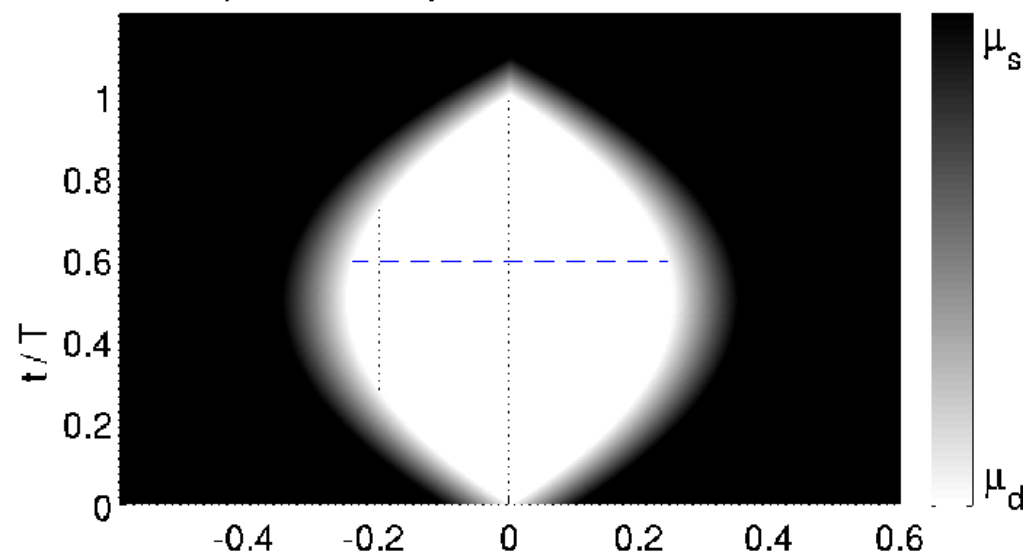
- Self-healing time-weakening**  
(Andrews and Ben-Zion, 97)

# Model setup

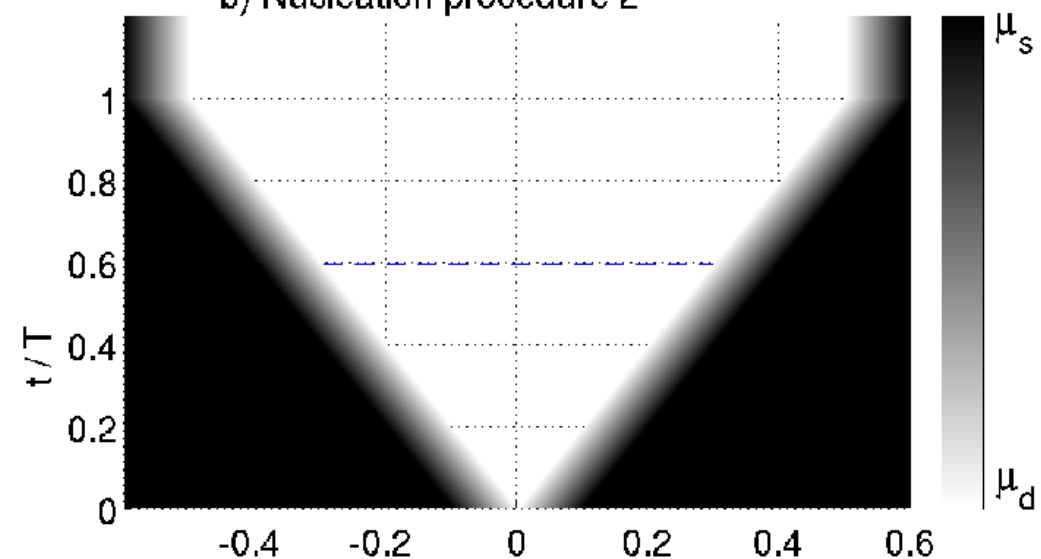
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b) Nucleation procedure 2



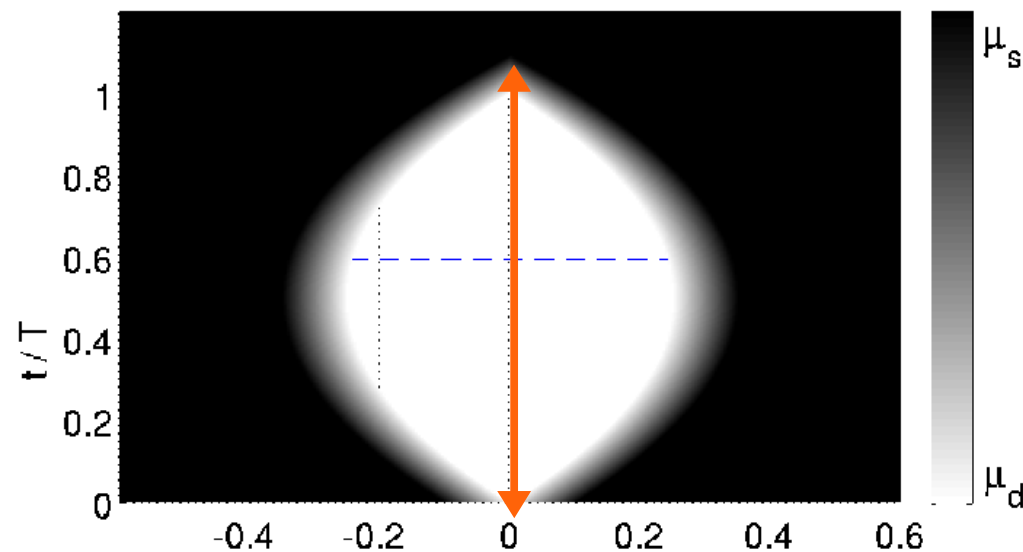
- Self-healing time-weakening**  
(Andrews and Ben-Zion,97)
- Non-healing time-weakening**  
(Andrews)

# Model setup

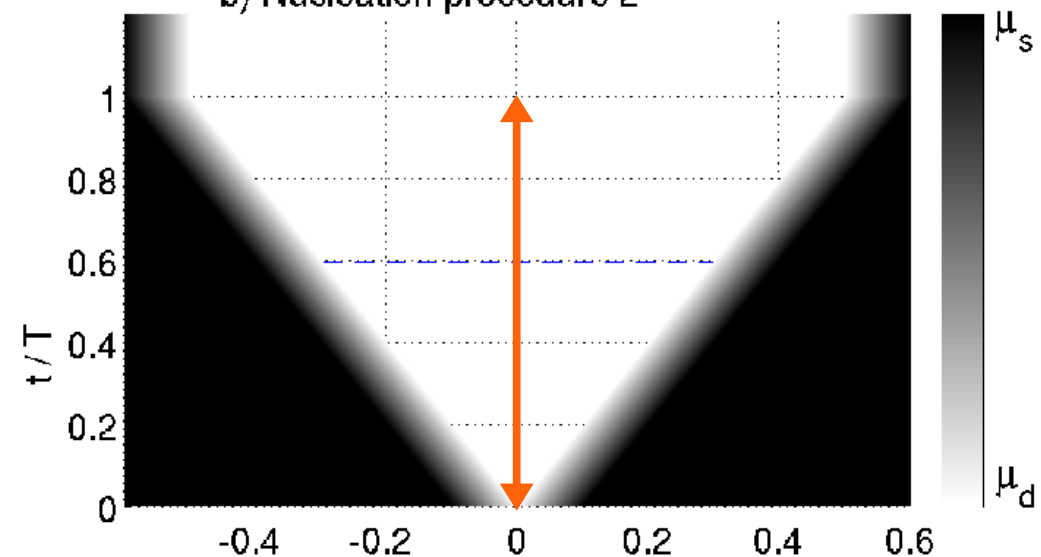
- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)  
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Prescribed time-dependent friction coefficient  $\mu_f$

a) Nucleation procedure 1



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Nucleation duration  $T$ : Will be varied

- Self-healing time-weakening  
(Andrews and Ben-Zion, 97)
- Non-healing time-weakening  
(Andrews)

# Model setup

- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)
- + **2 Nucleation procedures**: representing 2 extreme cases of frictional behavior
- + **Rate-and-state dependent friction law with fast velocity-weakening**  
(Ampuero, Ben-Zion (2008))

$$\mu_f = \mu_s + a \frac{V}{V + V_c} - b \frac{\Theta}{\Theta + D_c} \qquad \dot{\Theta} = V - \Theta \frac{V_c}{D_c}$$

# Model setup

- 2D spectral element method **SEM2DPACK** (Ampuero, 2008)
  - + **2 Nucleation procedures**: representing 2 extreme cases of frictional behavior
  - + **Rate-and-state dependent friction law with fast velocity-weakening**  
(Ampuero, Ben-Zion (2008))
- **Parameter space** study :
- Nucleation procedure and duration ( $T$ ) / background shear stress ( $S$ )**

# General rupture modes

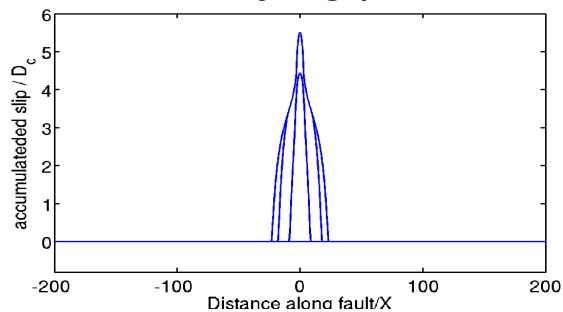
- In elastic media rupture approaches distinct (Stable) self-similar and (sensitive) transitional regimes

# General rupture modes

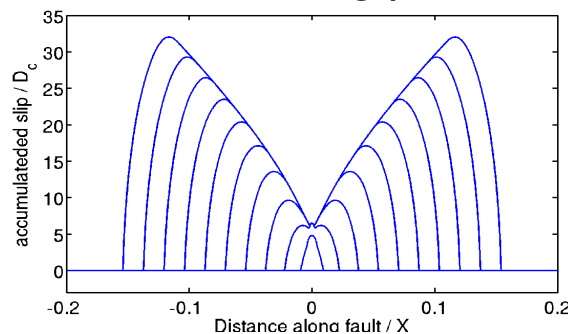
- In elastic media rupture approaches distinct **(Stable) self-similar** and **(sensitive) transitional** regimes

*Increasing shear stress-  
Decreasing  $S$*

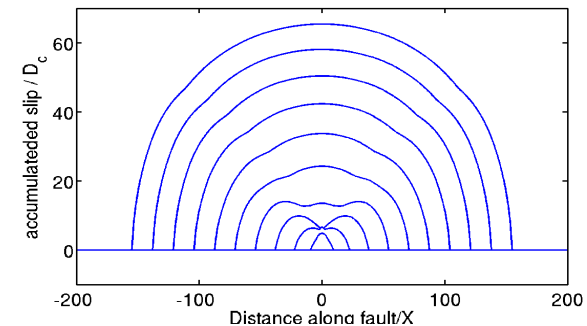
*Decaying pulse*



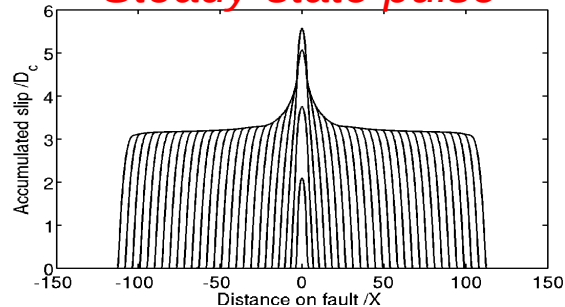
*Growing pulse*



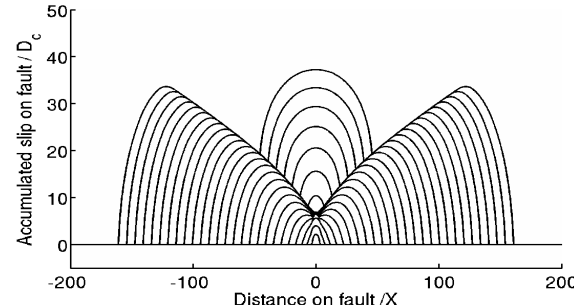
*Crack-like*



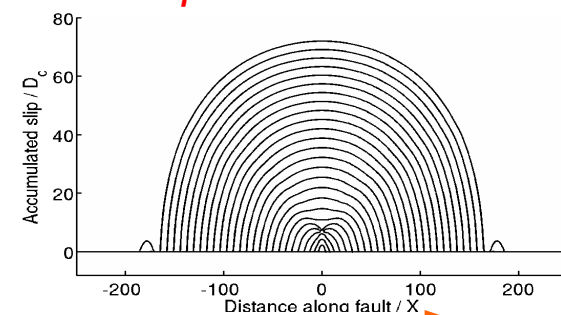
*Steady-state pulse*



*Pulse-crack transition*



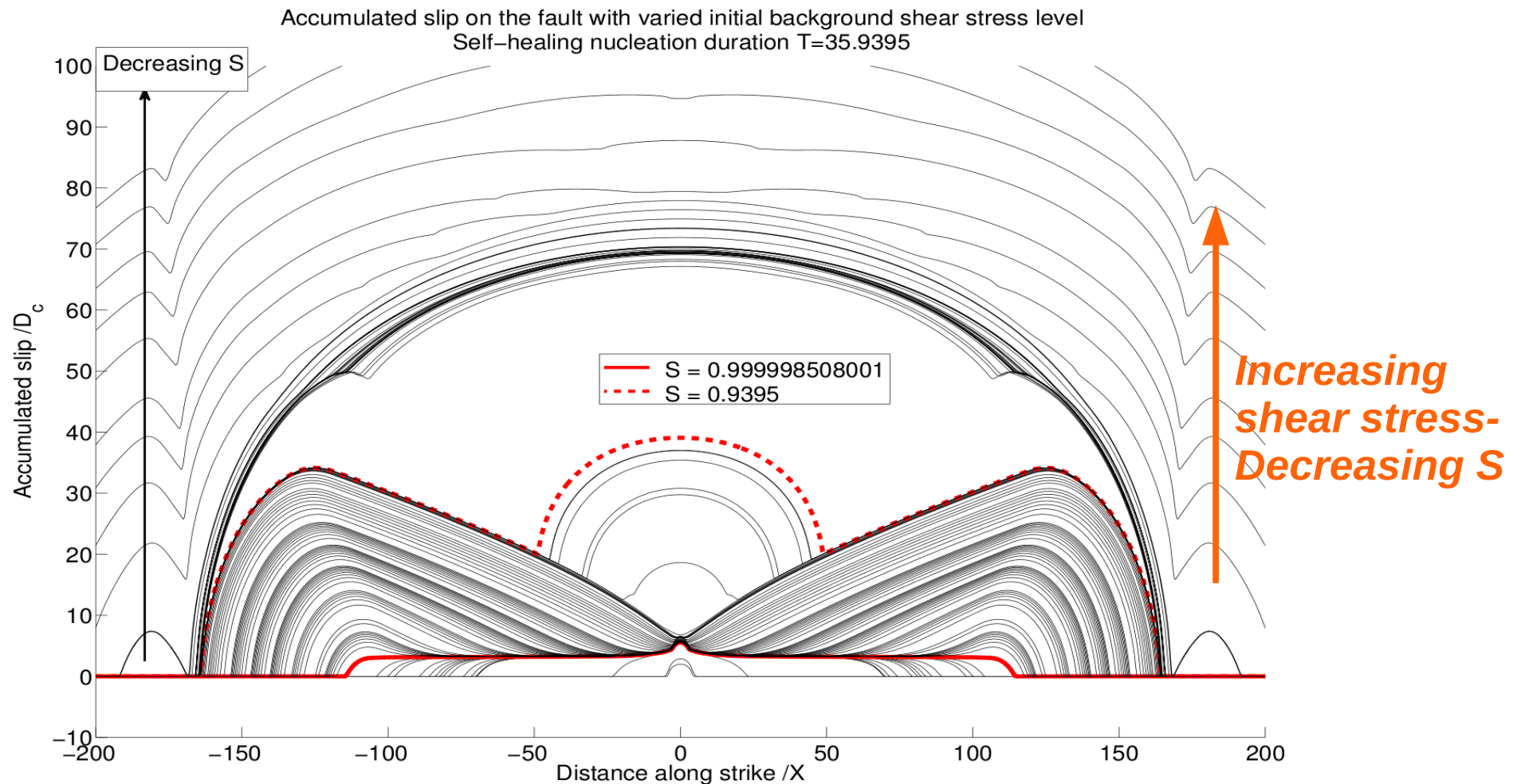
*Supershear transition*



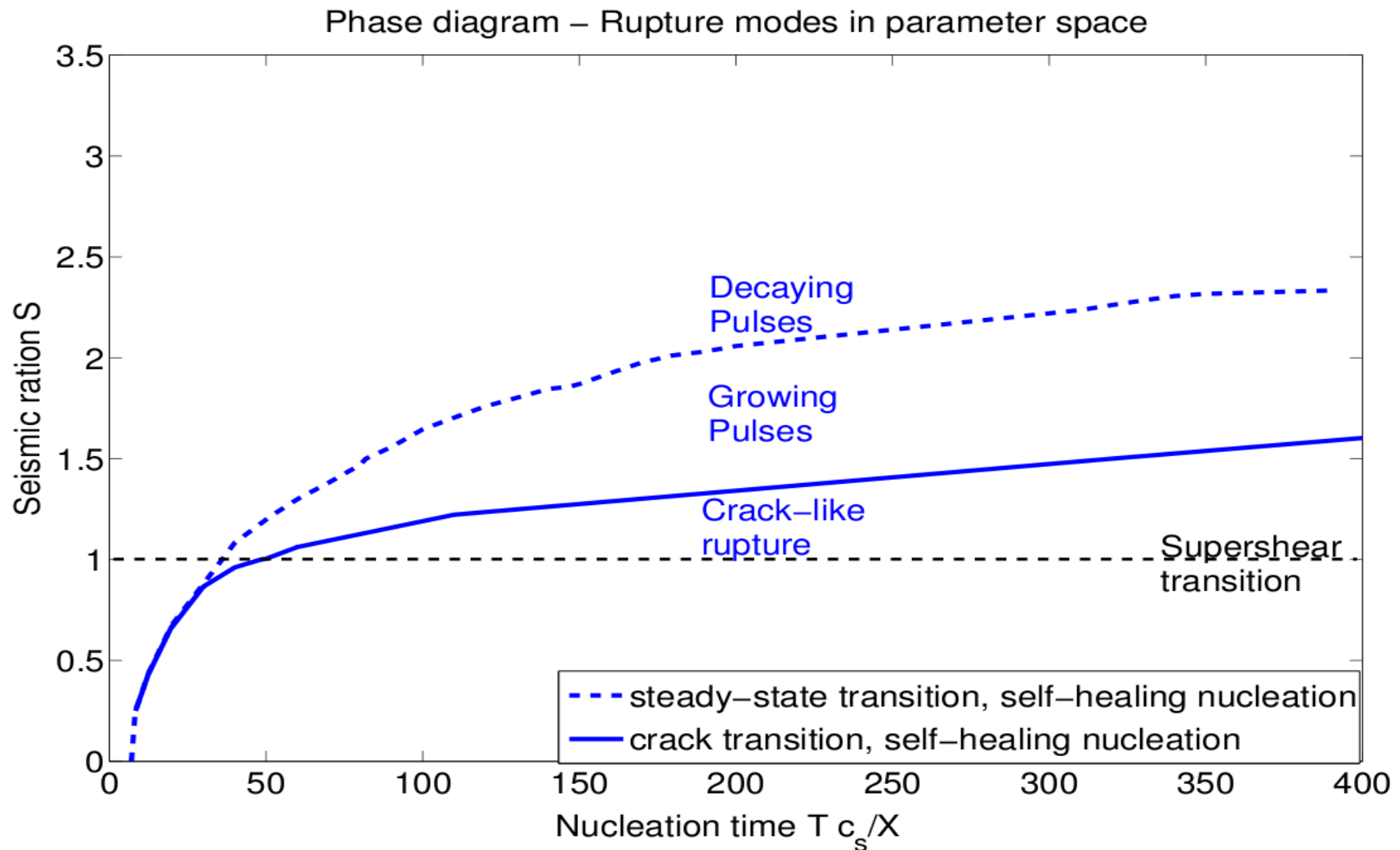
*Increasing Nucleation duration  $T$*

# General rupture modes

- In elastic media rupture approaches distinct **(Stable) self-similar** and **(sensitive) transitional** regimes

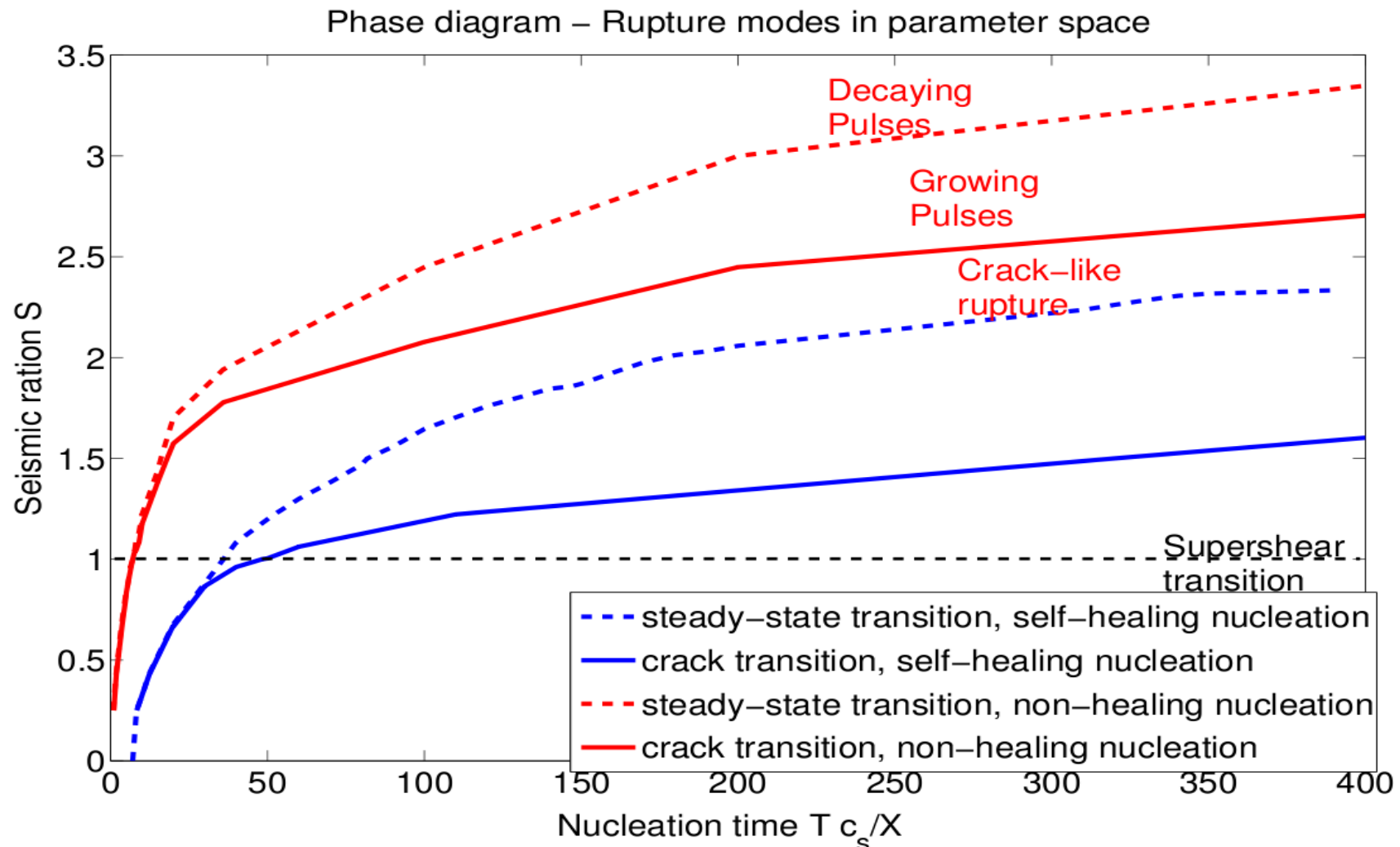


# Phase diagram – S, T



- Changes in initial stress state and nucleation **shift** rupture modes
- Higher stress states  $\Leftrightarrow$  shorter nucleation  
 $\Leftrightarrow$  smaller range of growing pulses

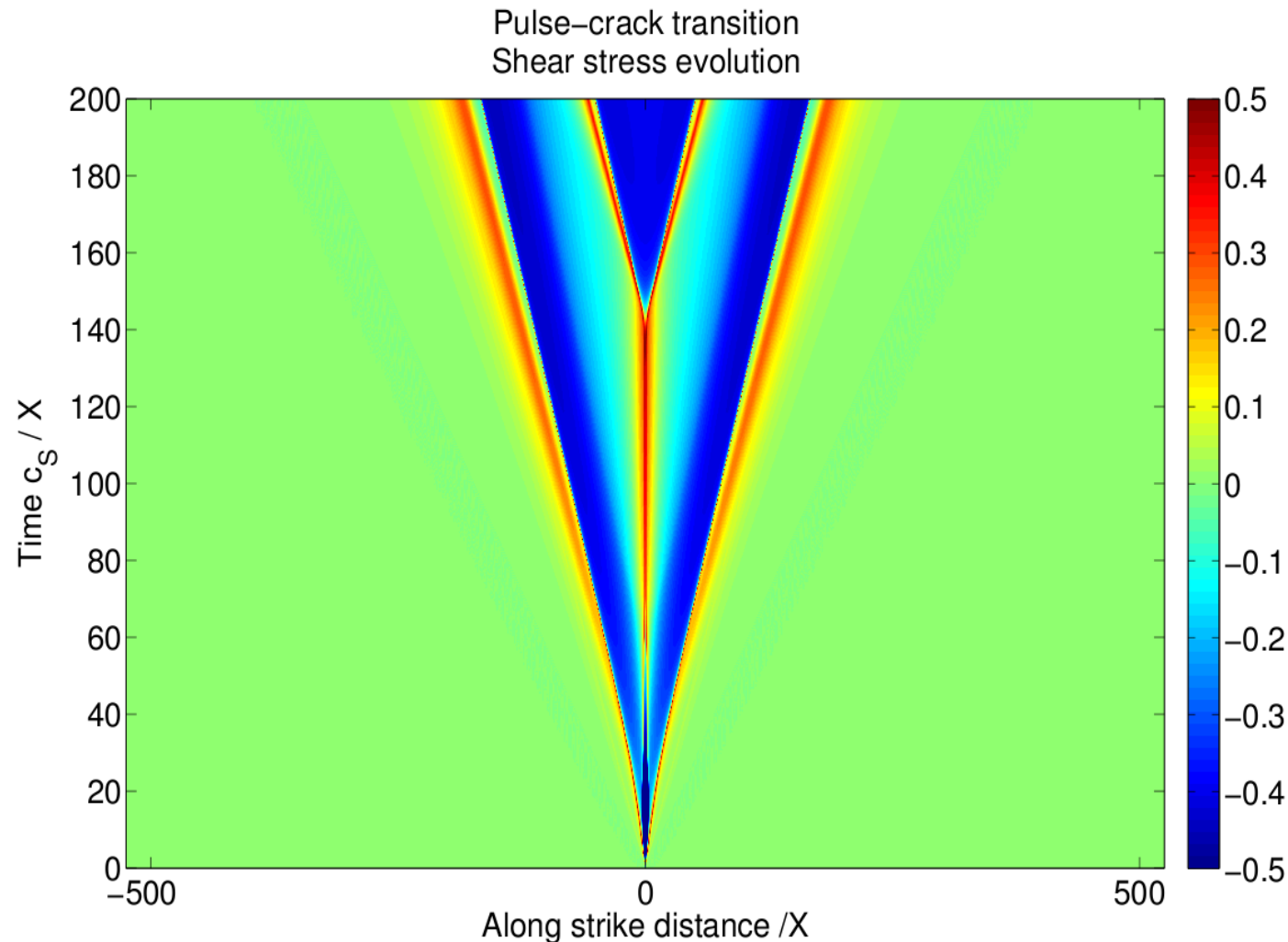
# Phase diagram – S, T



- Change in nucleation procedure **shifts** rupture modes
- Non-healing nucleation  $\Leftrightarrow$  shorter nucleation  
 $\Leftrightarrow$  lower initial stress state

# Transitional rupture modes

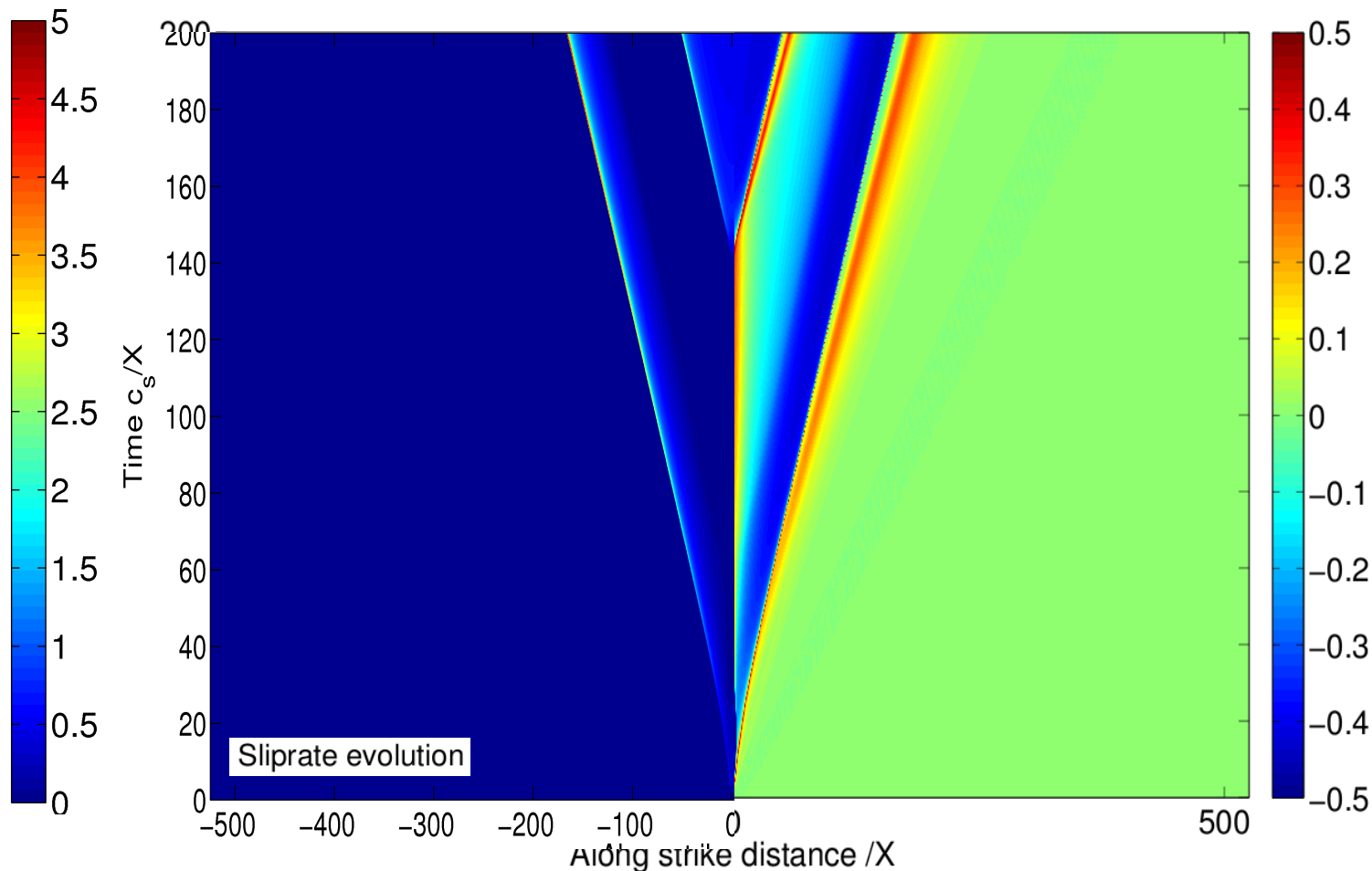
**Pulse-crack transition** → Gradual stress build-up at hypocenter  
(Madariaga&Nielsen,2003)



# Transitional rupture modes

**Pulse-crack transition** → Gradual stress build-up at hypocenter  
(Madariaga&Nielsen,2003) → Renucleation of secondary rupture

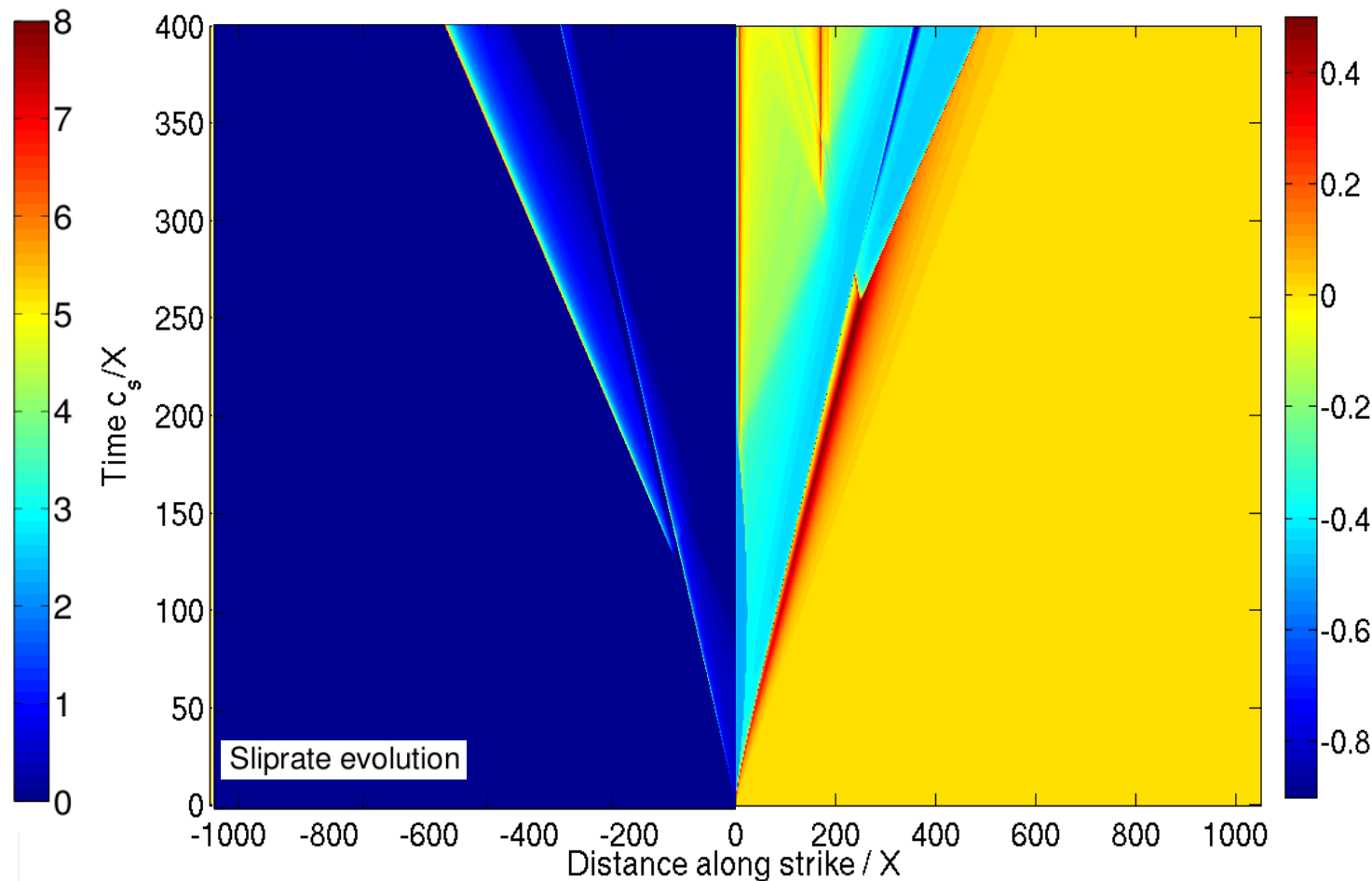
Pulse-crack transition



# Transitional rupture modes

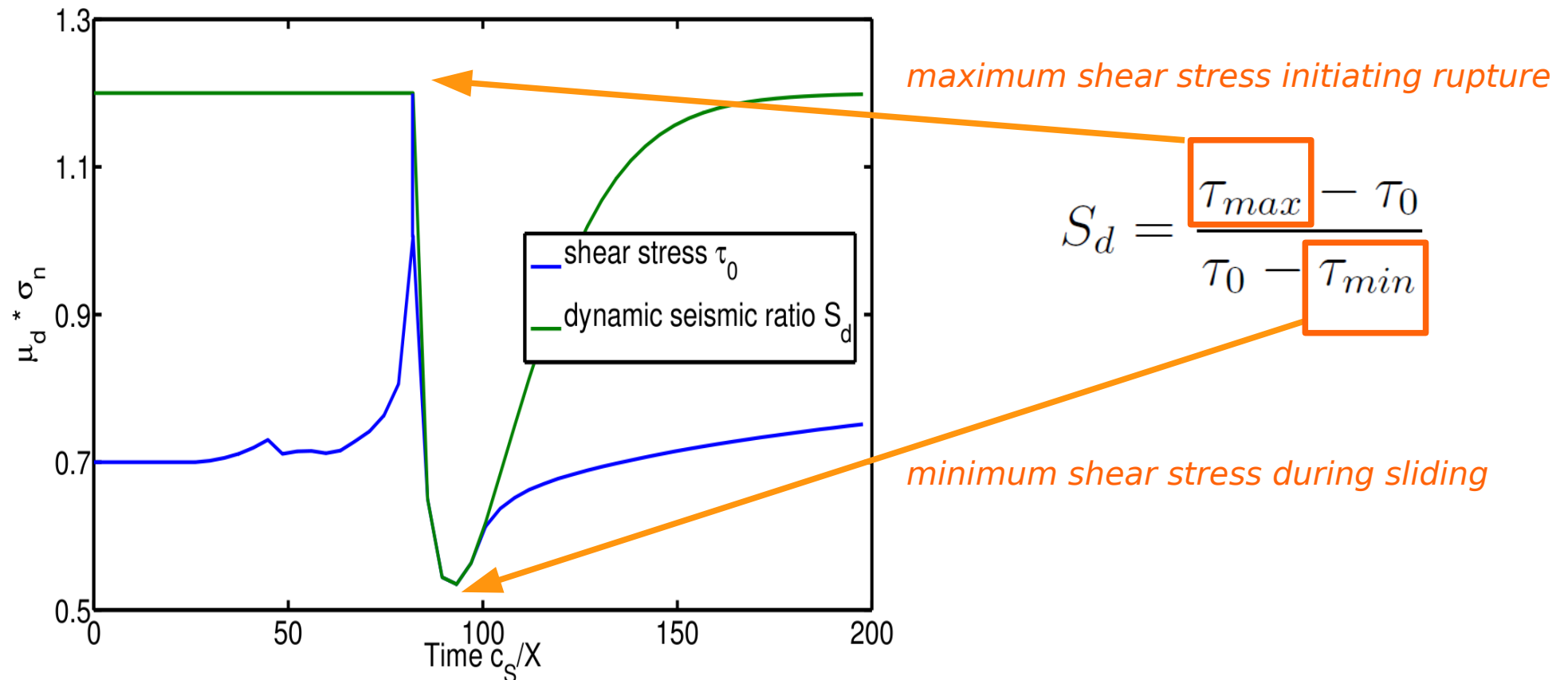
**Pulse-crack transition** vs **Supershear transition**  
→ stress build-up at rupture front (Burridge-Andrews-Mechanism)

Supershear pulse



# Dynamic seismic ratio $S_d$

- **Quantification** of closeness of rupture to Transitional Modes
  - **Dynamic strength excess** as part of solution
  - potentially **summarizing nucleation, initial stress & frictional** parameters

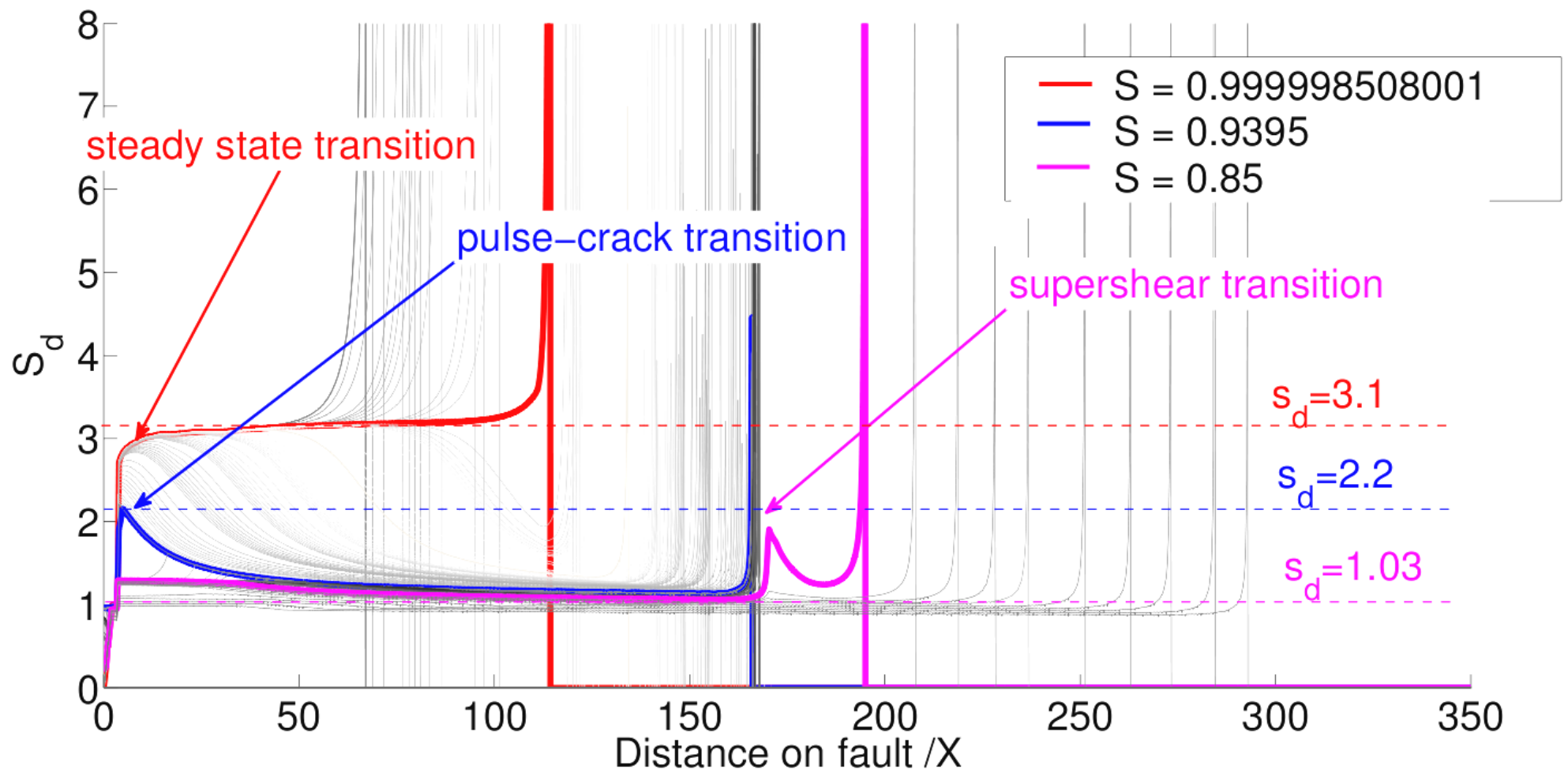


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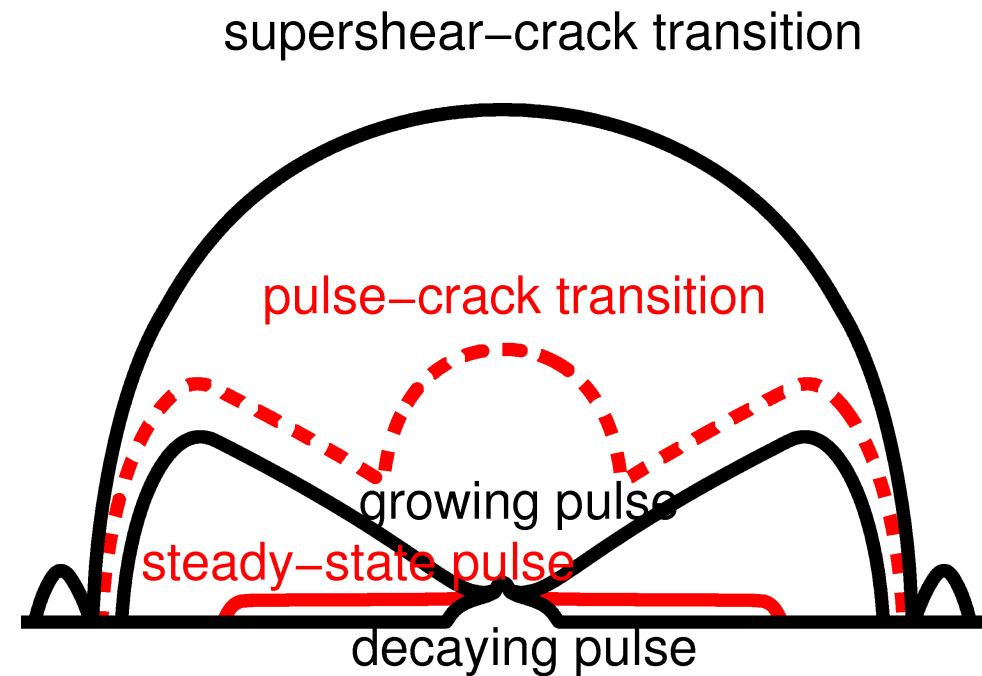
Dynamic strength excess  $S_d$

Self-healing nucleation  $T=35.9395$



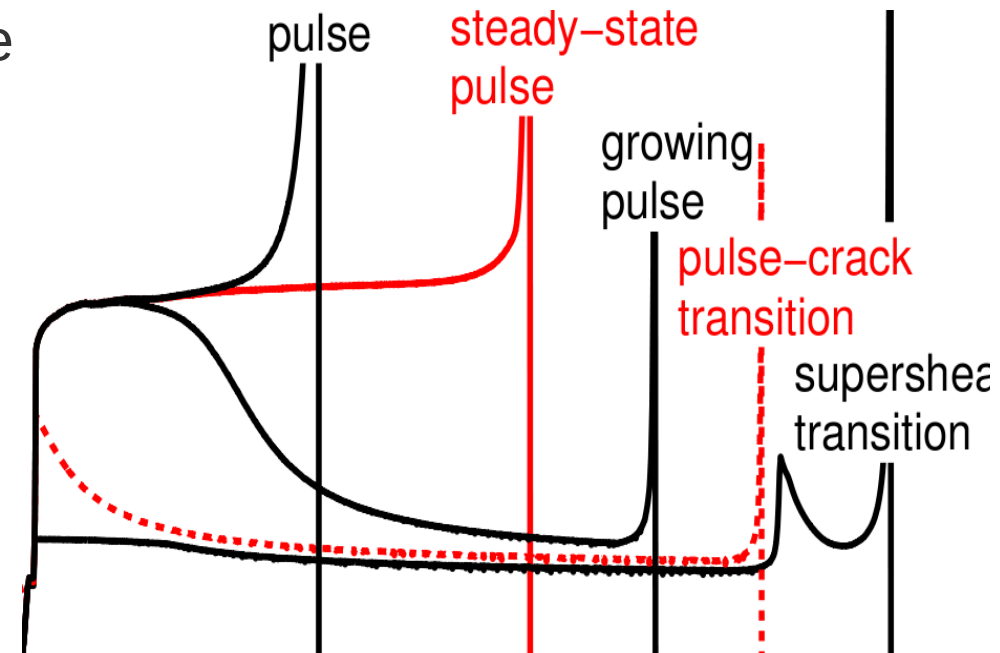
# Summary

- Generalized dynamic rupture behavior in wide parameter space  
in self-similar and transitional zones of rupture between decaying, steady state, growing and crack-like ruptures in sub- and supershear regimes
- The asymptotic behavior of self-similar areas seems independent of the initial parameters, unlike the details of the transient approach to that asymptotic solution



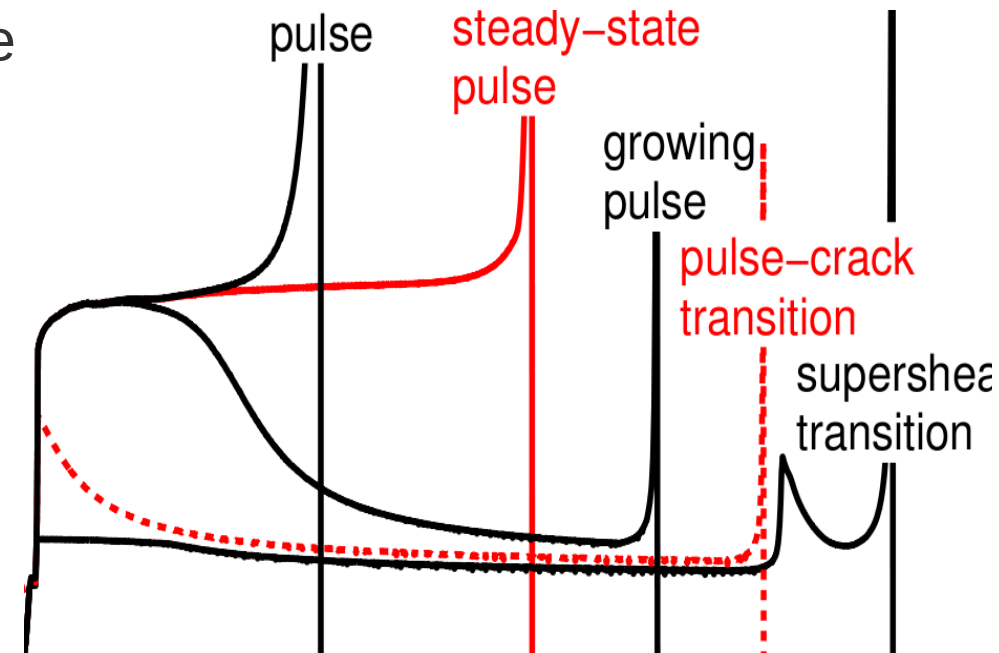
# Summary

- **Transitional modes** are highly sensitive to initial conditions and nucleation procedure and depend on competing critical propagation length scales
- **Dynamic seismic ratio  $S_d$**  is quantifying the closeness of rupture mode to (supershear) transition



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- **Transitional modes** are highly sensitive to initial conditions and nucleation procedure and depend on competing critical propagation length scales
- **Dynamic seismic ratio  $S_d$**  is quantifying the closeness of rupture mode to (supershear) transition



→ Under natural, non-homogeneous stress conditions, earthquakes can rupture in any dynamically stable rupture regime, or in combination of those, at sub- or supershear rupture velocities: depending on the actual **dynamical stress state of the fault**.

# Thank you!

→ [alice@sed.ethz.ch](mailto:alice@sed.ethz.ch)

→ For the effects of **off-fault plasticity on rupture modes and macroscopic source properties**

→ POSTER: XY499 Friday 10.30  
EGU2011-11806

*“Macroscopic Source Properties  
From Dynamic Rupture Simulations  
With Off-Fault Plasticity”*

