

# *Synthetic Hydrograph Generator for Reservoirs: Options and Limitations*

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- ⇒ Introduction
  - ⇒ Backgrounds of this presentation
  - ⇒ Synthetic hydrographs
- ⇒ Simulation of design hydrographs following the German Dam Standard
- ⇒ Limitations of this method
- ⇒ Conclusion

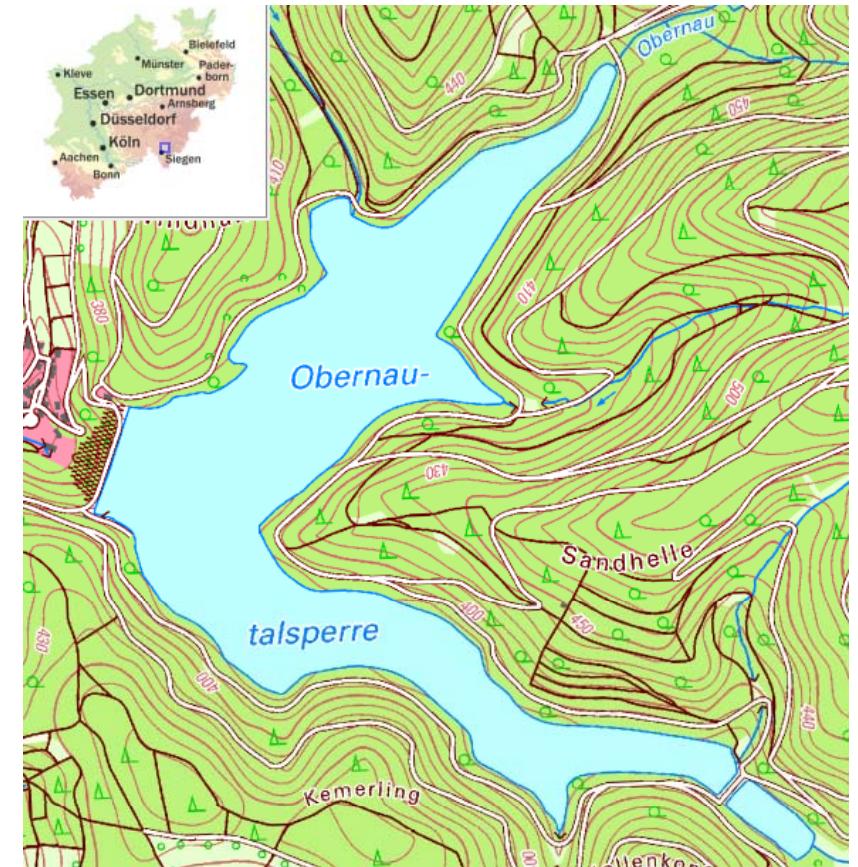
# Introduction

The presented results are obtained from master thesis:

*"Development of a stochastic reservoir management tool"*

Case study: Obernau Reservoir

- ⌚ Catchment: 21,5 km<sup>2</sup>
- ⌚ Volume: 14,8 Mio. m<sup>3</sup>
- ⌚ Dam height: 46,0 m
- ⌚ Purpose: Drinking water supply and flood control



The German Dam Standard (DIN 19700 (2004)) postulates for the design of reservoirs and flood control basins the use of hydrographs instead of peak flows

## Advantages

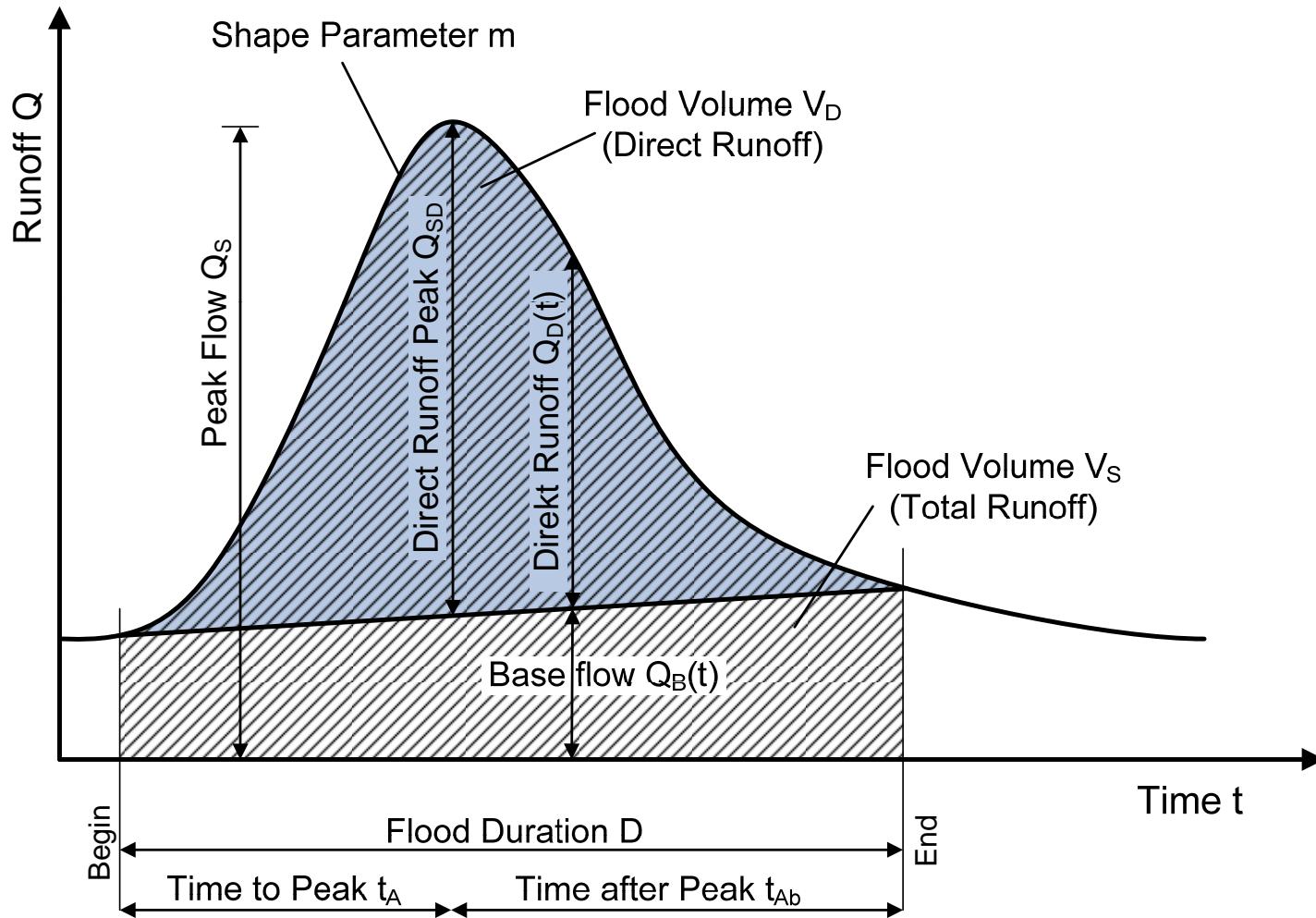
- ⌚ Consideration of lake retention and empty flood control storage
- ⌚ Detailed information about storage maximizing events

## Disadvantages

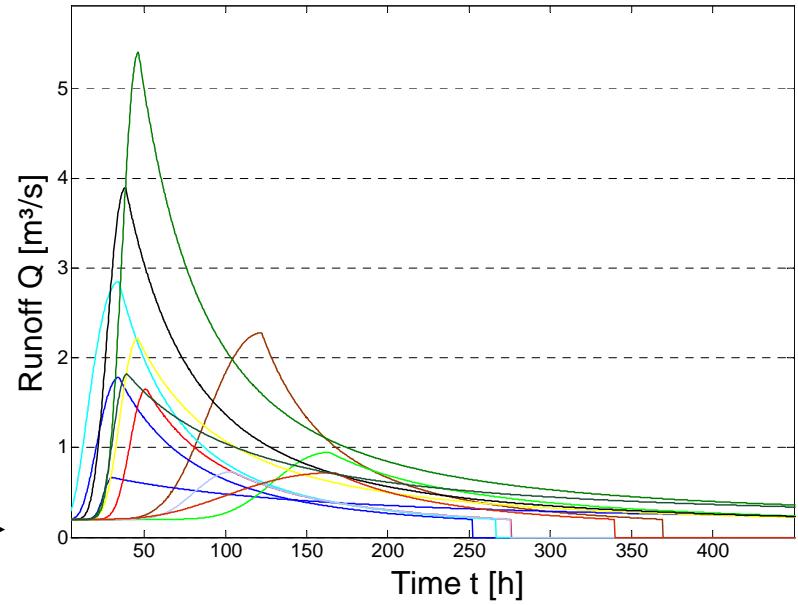
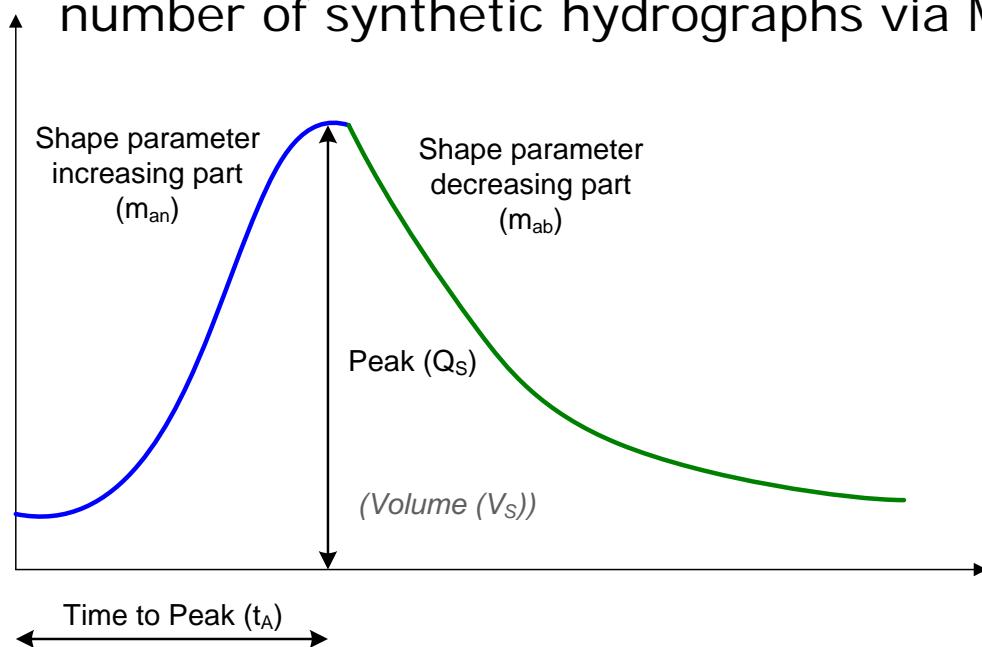
- ⌚ Mostly no information about extreme hydrographs available
- ⌚ Hydrographs are substantially more complex than peak flows

→ **Stochastic methods required!**

## Specific parameters of flood waves



- ⇒ German guideline “Generation of design hydrographs following DIN 19700 in North Rhine-Westphalia” MUNLV (2004)
- ⇒ Stochastic-deterministic method to simulate design hydrographs for reservoirs as an alternative to rainfall-runoff modells
- ⇒ Determination of parameter sample based on recorded hydrographs
- ⇒ Fitting distribution functions to samples allows for generating any number of synthetic hydrographs via Monte-Carlo method



## **Kozeny-function (Gamma-distribution) by DYCK (1980)**

$$Q_D(t) = (Q_S - Q_B(t)) \cdot \left( \left( \frac{t}{t_A} \right)^m \cdot e^{m \cdot \left( 1 - \frac{t}{t_A} \right)} \right) + Q_B(t)$$

With

$Q_D(t)$ : Runoff at time  $t$  [ $m^3/s$ ]

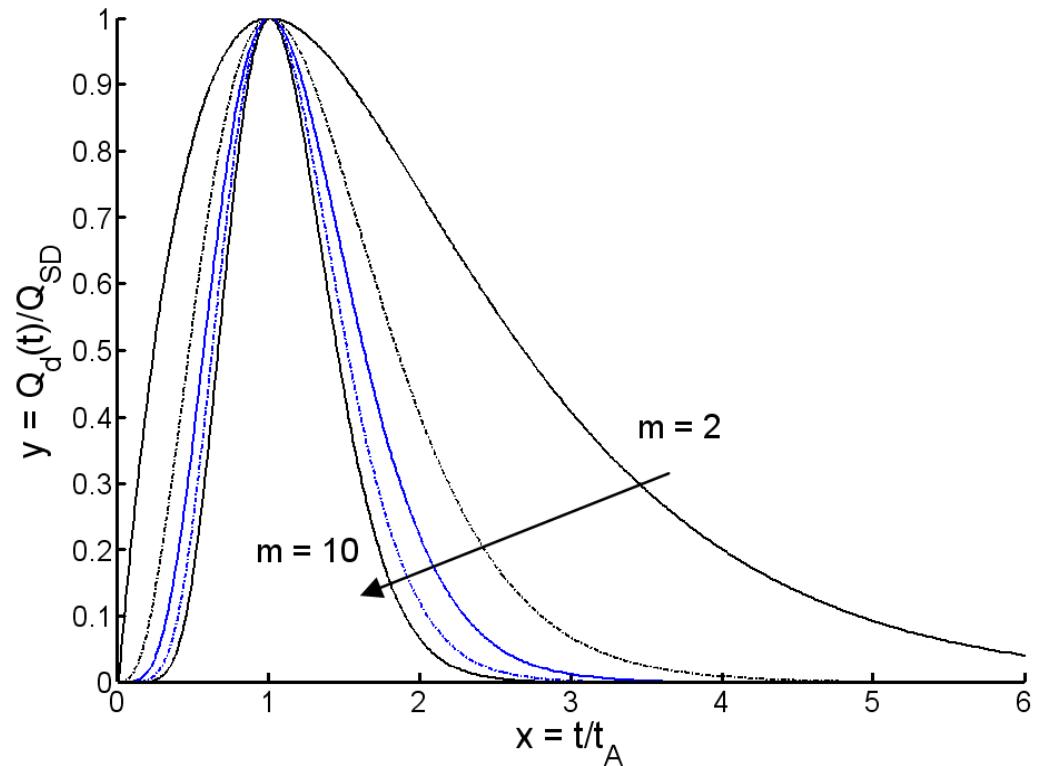
$Q_S$ : **Peak flow** [ $m^3/s$ ]

$m$ : **Shape parameter** [-]

$t_A$ : **Time to peak [h]**

$t$ : Time [h]

$Q_B(t)$ : Baseflow [ $m^3/s$ ]



## *Hyperbolic function by LEICHTFUSS & LOHR (1999)*

$$Q_D(t) = Q_0 \cdot \left( 1 - \left( \frac{(e^k)^a - (e^{-k})^a}{(e^k)^a + (e^{-k})^a} \right) \right)$$

With

$Q_D(t)$ : Runoff at time  $t$  [ $\text{m}^3/\text{s}$ ]

$Q_S$ : **Peak runoff [ $\text{m}^3/\text{s}$ ]**

$m_{ab}$ : **Shape parameter [-]**

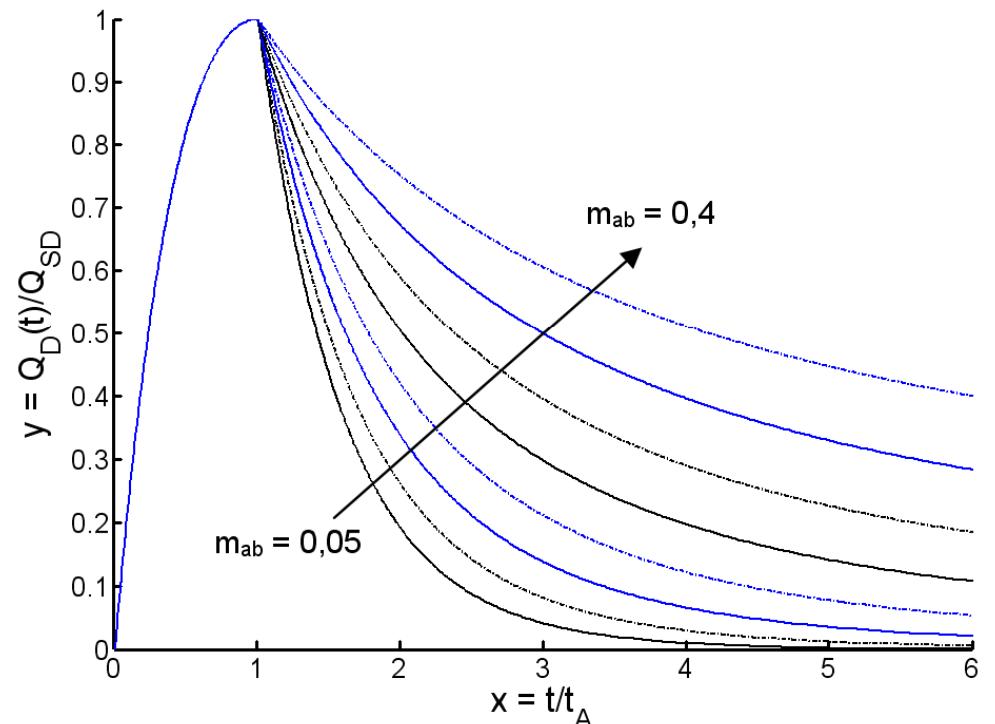
$t$ : Time [ $1\text{d} = 1$ ]

$t_S$ : Start time of decreasing

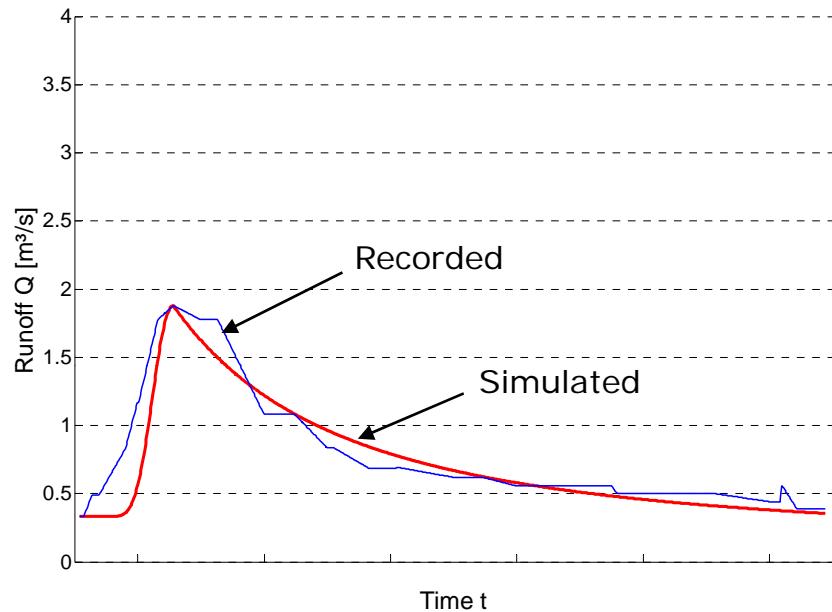
$Q_0$ : Defined max. runoff [ $\text{m}^3/\text{s}$ ]  
e.g. PMF

$a$ : Compression ( $0,95 < a < 1$ ) [-]

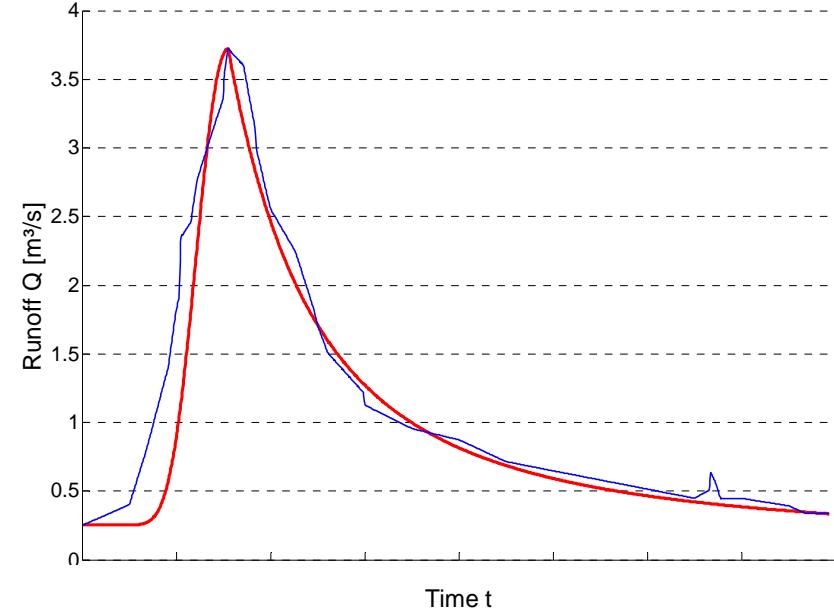
$b$ : Intercept (usually  $b=1$ ) [-]



## *Examples of recorded and simulated flood events*



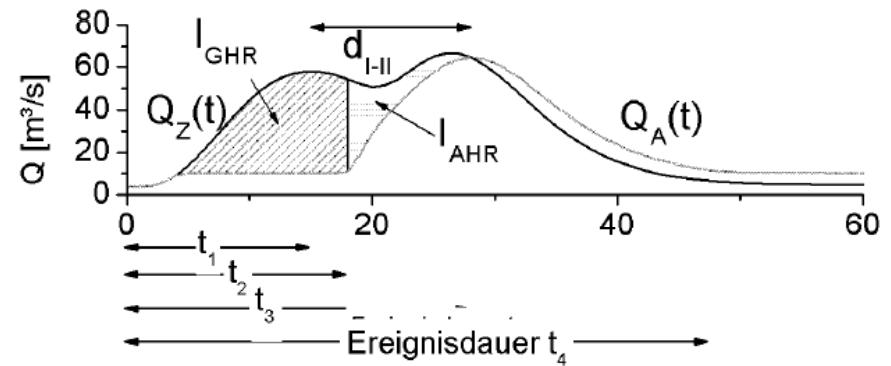
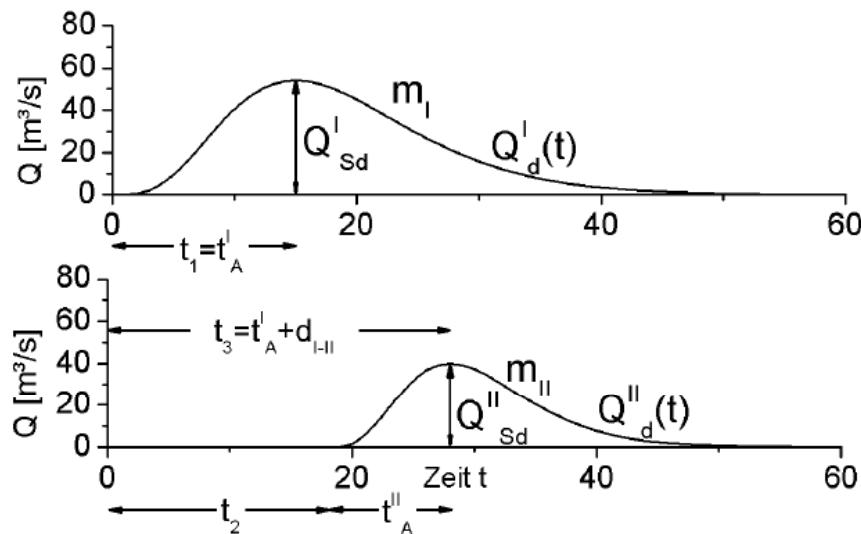
Peak flow $Q_S$ [ $\text{m}^3/\text{s}$ ]:	1,88
Baseflow $Q_B$ [ $\text{m}^3/\text{s}$ ]:	0,33
Time to peak $t_A$ [h]:	36,0
Shape parameter bef. peak $m_{an}$ [-]:	5,1
Shape parameter aft. peak $m_{ab}$ [-]:	0,27



Peak flow $Q_S$ [ $\text{m}^3/\text{s}$ ]:	3,72
Baseflow $Q_B$ [ $\text{m}^3/\text{s}$ ]:	0,25
Time to peak $t_A$ [h]:	74,25
Shape parameter bef. peak $m_{an}$ [-]:	8,7
Shape parameter aft. Peak $m_{ab}$ [-]:	0,27

## Multi-peak hydrographs

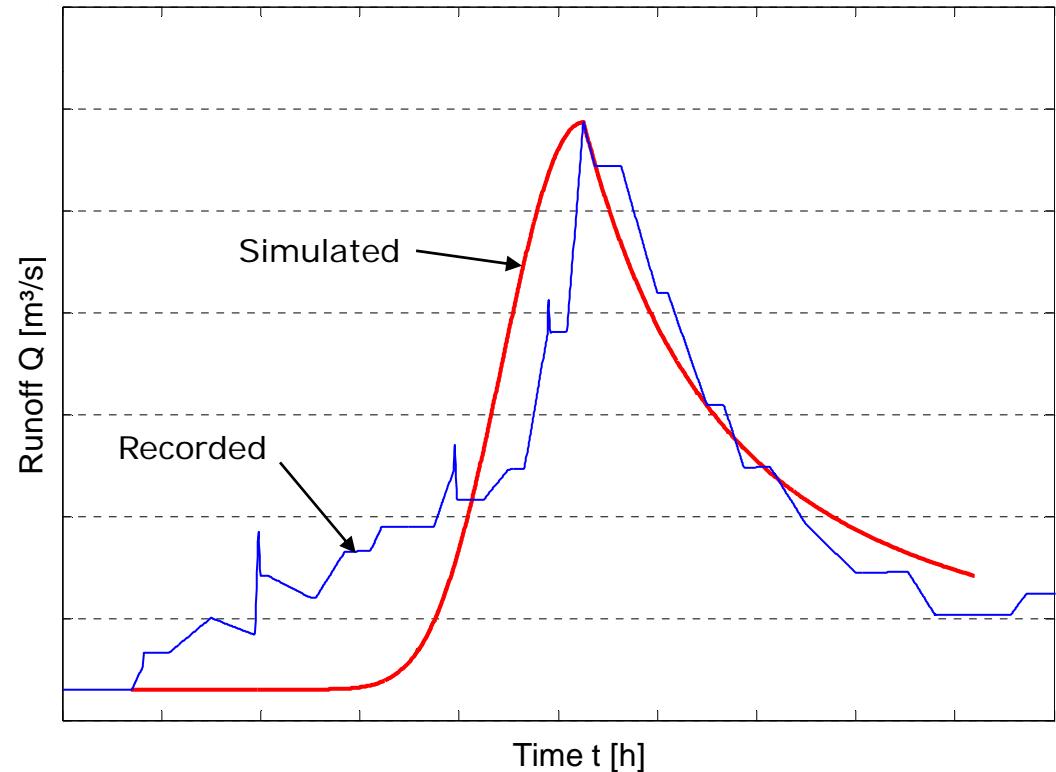
- ⌚ Multi-peak events can not be simulated
- ⌚ These events mostly cause maximum water levels ( $\rightarrow$  structural failure)
  - ⌚ Approach of overlapping multiple Kozeny-functions (KLEIN 2009)



Source: KLEIN(2009)

## *Slowly rising hydrographs*

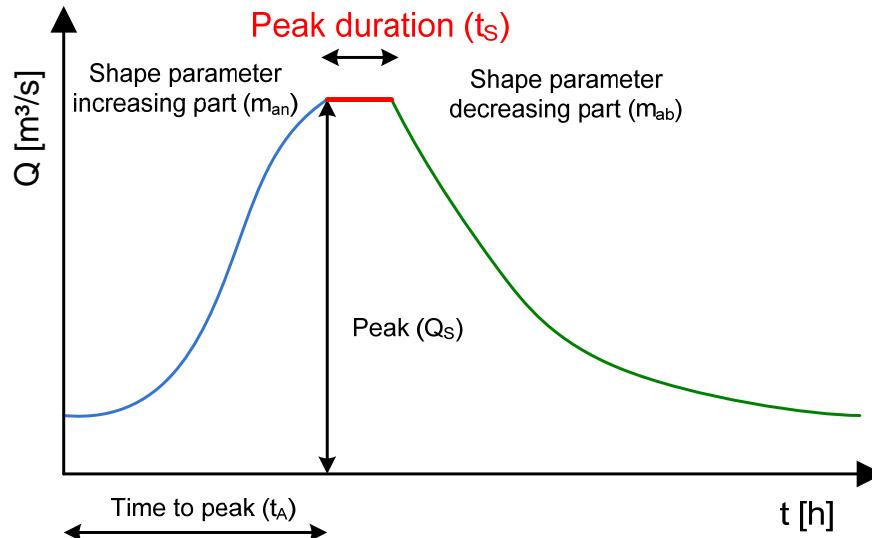
- ⌚ Slowly rising hydrographs can not be simulated with Kozeny-function
- ⌚ Resulting in high m-value
- ⌚ No existing solution!



## ***Peak flow duration***

- ⇒ Constantly remaining peak flows can not be simulated
- ⇒ Result: Exposure time of maximum load must be neglected
  - ⇒ Extending the method by a fifth parameter:

Peak flow duration  $t_s$  (Study in progress)



- Method is applicable for simple (single peak) shaped hydrographs
- Forms an alternativ method to rainfall-runoff modelling
- Not applicable for catchments where:
  - Multi-peak hydrographs
  - Slowly rising hydrographs
  - Long peak flows
- Can be expected
- **Still need for further research existing!**

*Thank you very much for your attention!*

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