

# Risk management with probabilistic advective-dispersive well vulnerability criteria

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# Challenges in Water Supply Systems

„Drinking-water quality is an issue of concern for human health in developing and developed countries world-wide.“

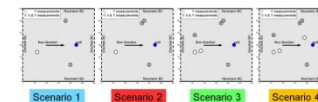
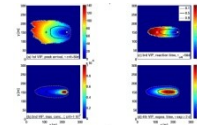
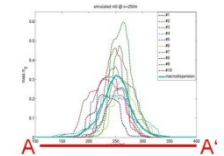
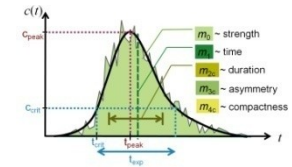
WHO 3<sup>rd</sup> edition, Guidelines for Drinking Water Quality, 2004, Introduction

„The most effective means of consistently ensuring the safety of a drinking-water supply is through the use of a **comprehensive risk assessment** and **risk management approach** that encompasses all steps in water supply from catchment to consumer.“

WHO 3<sup>rd</sup> edition, Guidelines for Drinking Water Quality, 2004, Chapter 4 Water Safety Plans



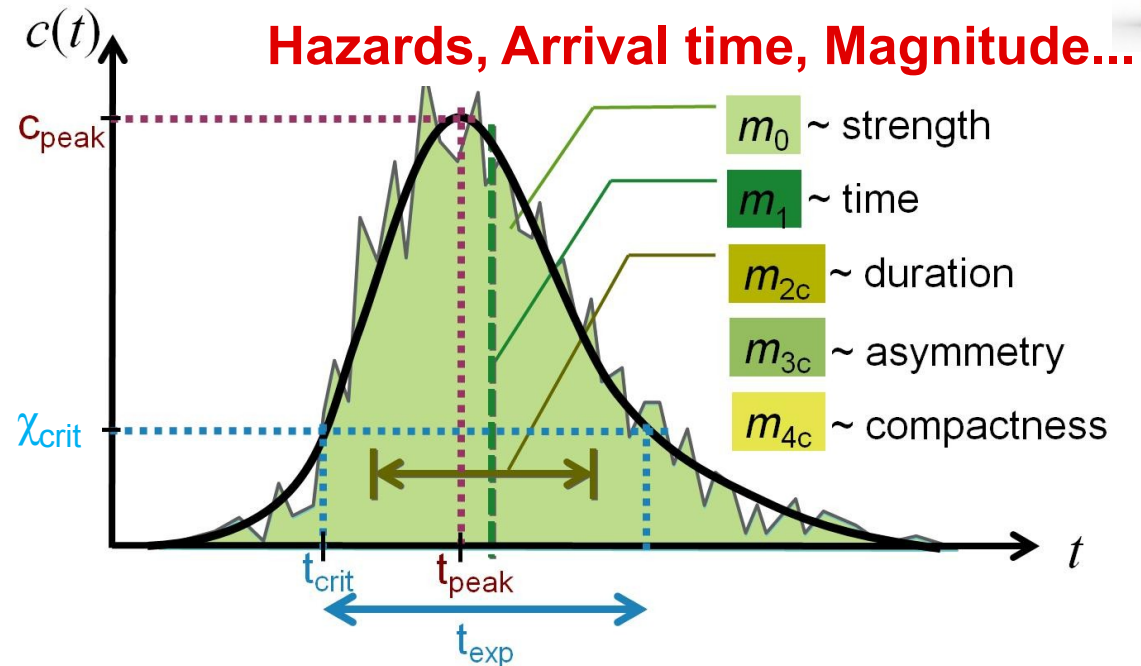
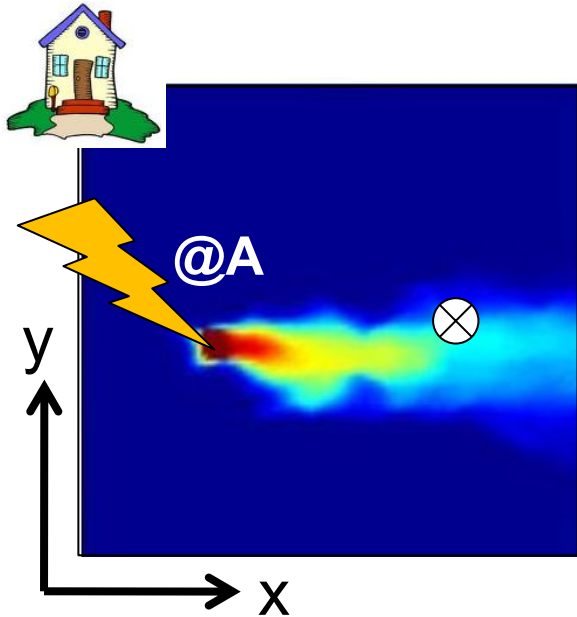
# Outline



- 1 What kind of information is needed for risk management?
- 2 Why probabilistic risk assessment approaches?
- 3 Our probabilistic risk assessment approach!
- 4 Risk management under financial constraints?
  - ➔ Uncertainty reduction
  - ➔ Alternative risk treatment costs
- 5 Conclusions



# Well Vulnerability Criteria (WVC)



- 1) Time of peak arrival:  $t_{\text{peak}}$
- 2) Max. concentration:  $c_{\text{peak}}$
- 3) Time to react:  $t_{\text{crit}}$  (threshold level  $\chi_{\text{crit}}$ )
- 4) Exposure time:  $t_{\text{exp}}$

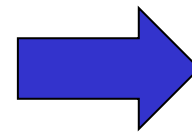
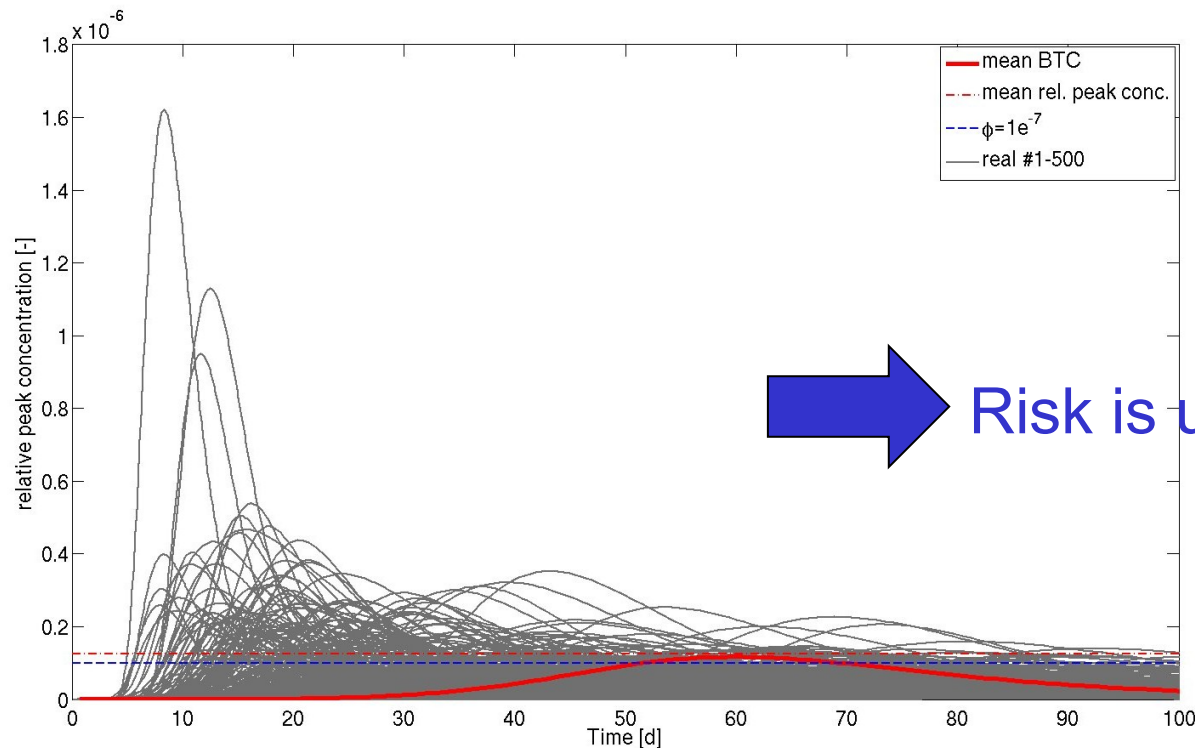
(Frind et al., 2006)

## Probabilistic Risk Framework

(Enzenhöfer et al., 2010)

# Why probabilistic risk assessment I

- Peak concentrations too small (averaging different peak times)
- Arrival of contamination is underestimated (uncertain first arrival)

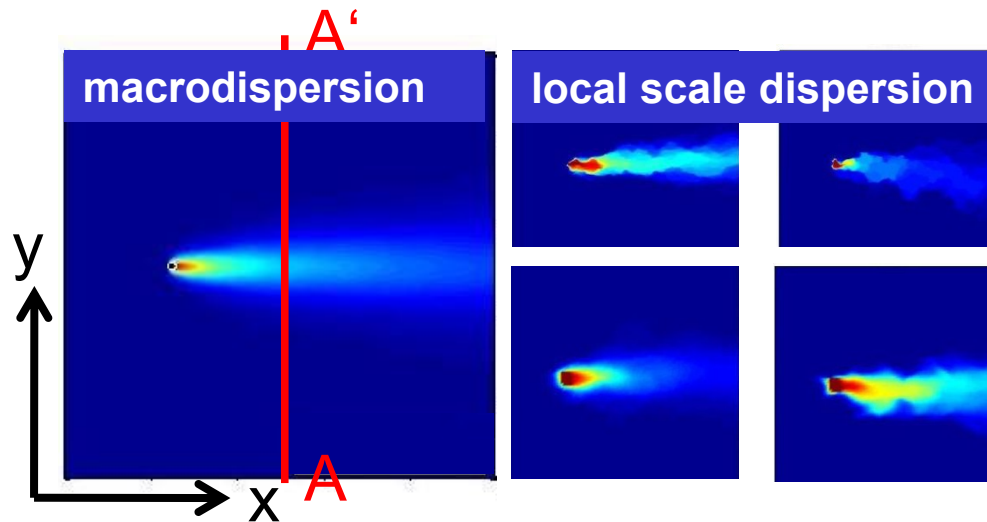


Risk is underestimated !!!

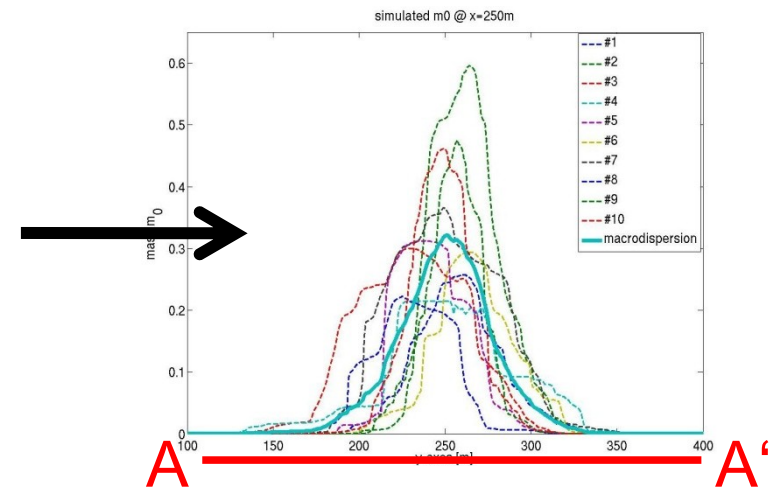


# Why probabilistic risk assessment II

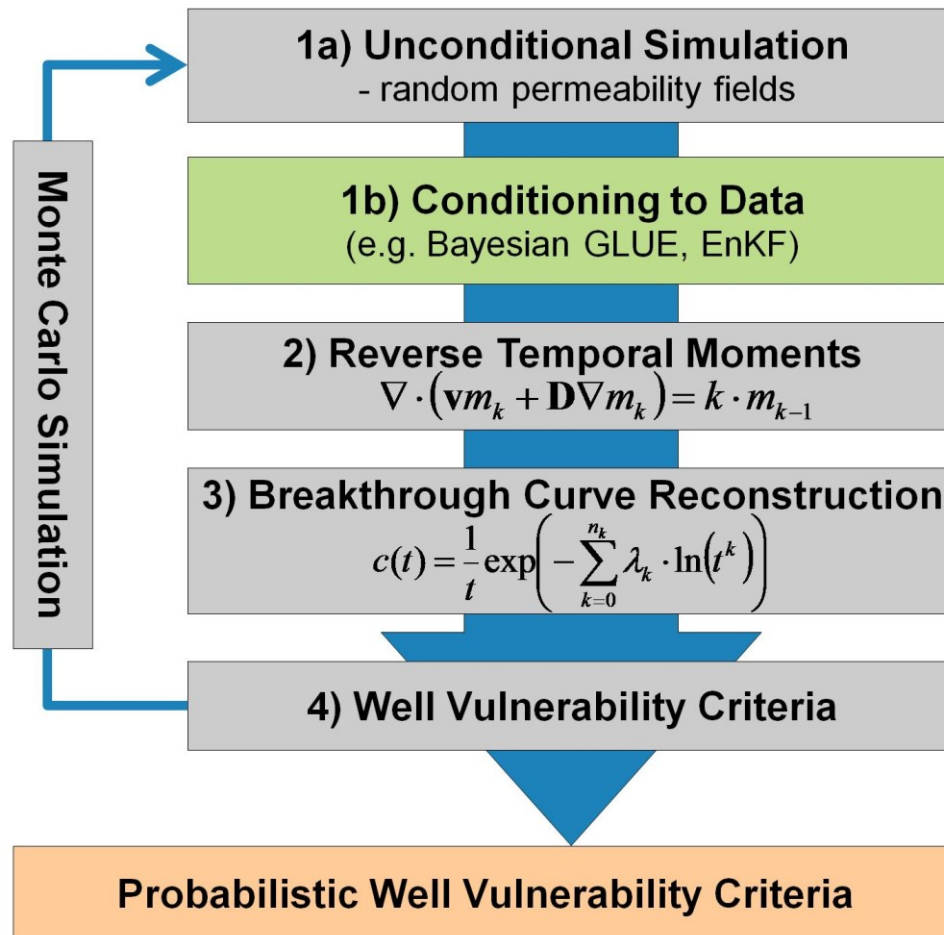
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- 
- Concentrations are assumed where there is none (variability in space)



➡ Risk is underestimated



# Our probabilistic risk concept



$n$  = 500 realizations

$Y$  =  $\ln(\mu)$

$\mu$  =  $[-7.5 \quad -5.5]$

$\sigma^2$  =  $[1 \quad 3]$

$\kappa$  =  $[0.5 \quad 5]$  (Matérn)

$\lambda_x$  =  $[10 \quad 25]$  m

$\lambda_x$  =  $[5 \quad 15]$  m

$$P(t \geq t_0 \mid \mathbf{x} = \mathbf{x}_i) \approx \frac{1}{n} \sum_{j=1}^n w_j \cdot I_j(\mathbf{x}_i)$$

# Conditioning on log(Y) and h

- Bayesian GLUE approach
- Synthetic truth ( $\mathbf{d}_0$ : 15 measurements)
- Conditioned probabilistic WVC

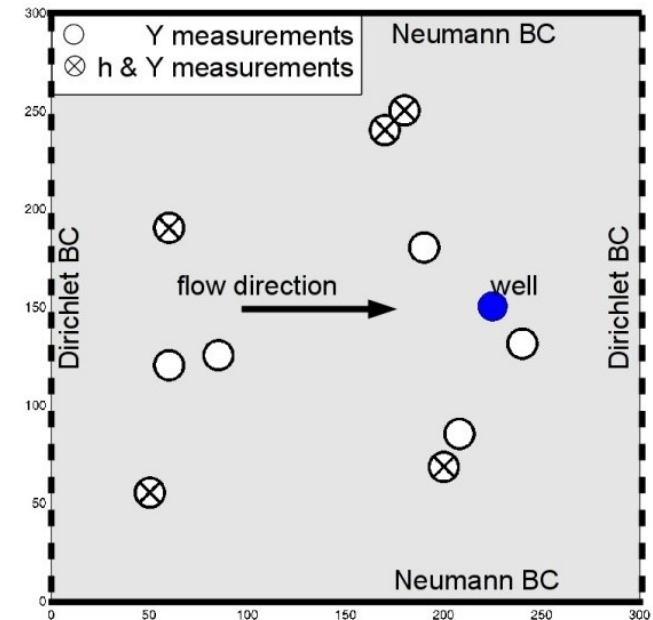
$$\tilde{P}(t \geq t_0 | \mathbf{x}_i, \mathbf{d}_0) \approx \frac{1}{n} \sum_{j=1}^n w_j \cdot I_j(\mathbf{x}_i)$$

- Weight per realization j:  $w_j = L_j / \sum L_j$

$$L(\mathbf{s}_j, \boldsymbol{\theta}_j, \boldsymbol{\beta}_j | \mathbf{d}_0) = \left( \frac{1}{2\pi \|\mathbf{R}\|} \right)^{m/2} \exp \left[ -\frac{1}{2} (\mathbf{d}_0 - \mathbf{d}_{sim}(\mathbf{s}_j))^T \mathbf{R}^{-1} (\mathbf{d}_0 - \mathbf{d}_{sim}(\mathbf{s}_j)) \right]$$

- $\mathbf{R}$ : error covariance matrix (e.g., measurement & model error)
- Fast Kriging-like conditioning of direct point-scale measurements

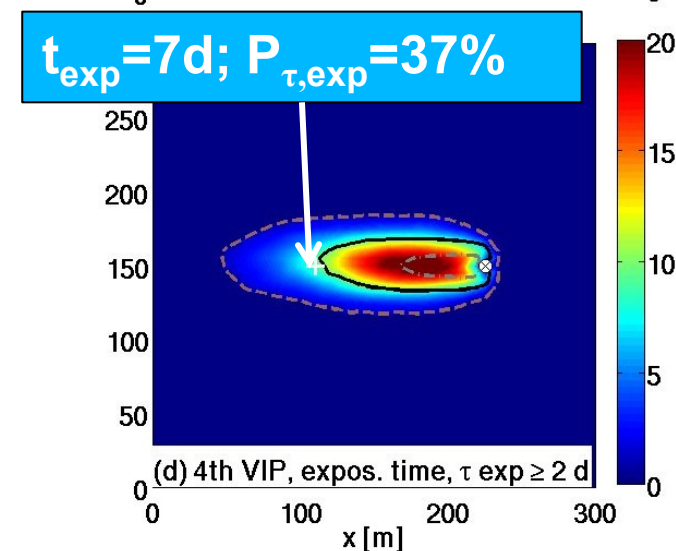
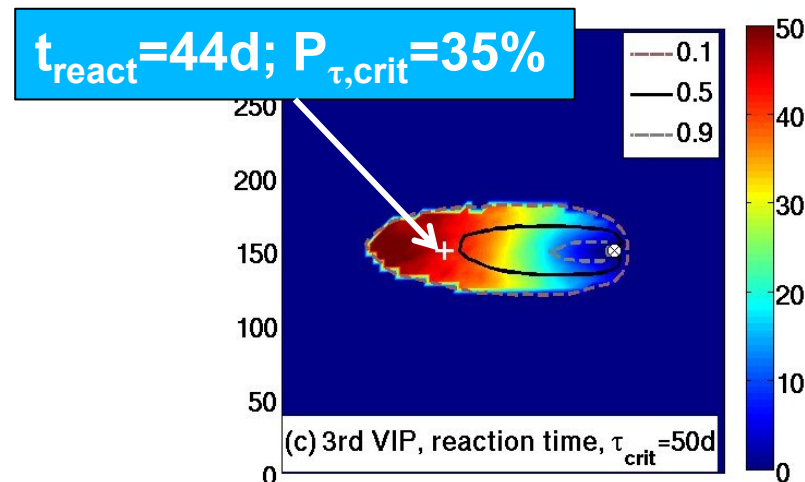
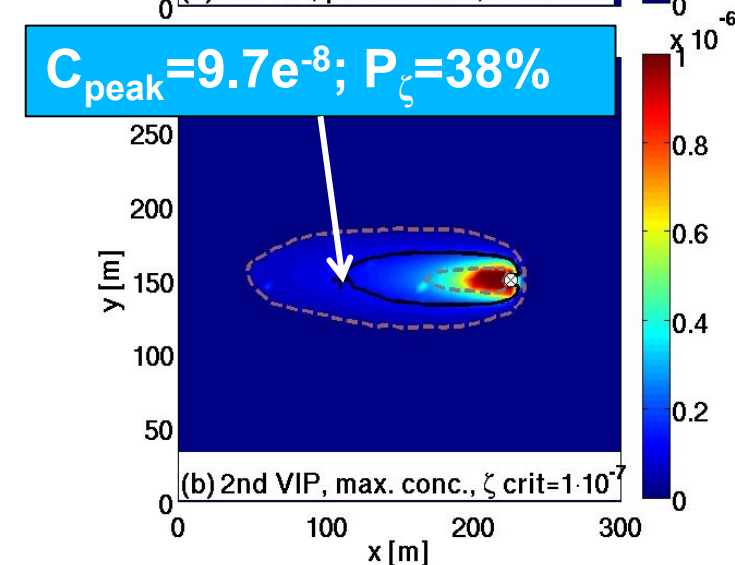
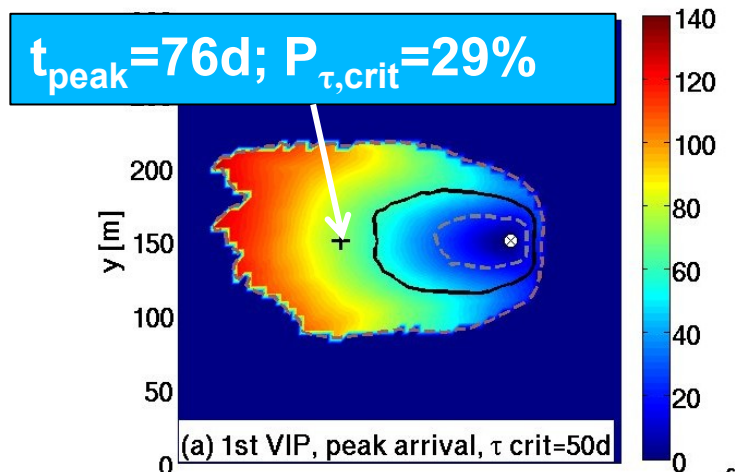
- Rejection Sampling  $\frac{L_j}{L_{\max}} > r \begin{cases} \text{true,} & w_j = 1 \\ \text{false,} & w_j = 0 \end{cases}$



(Enzenhöfer et al., in Review)

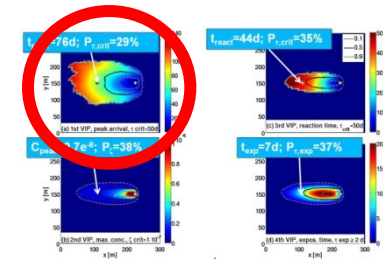
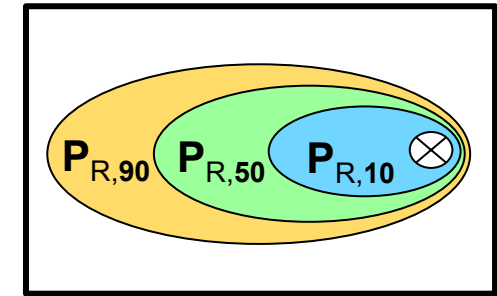
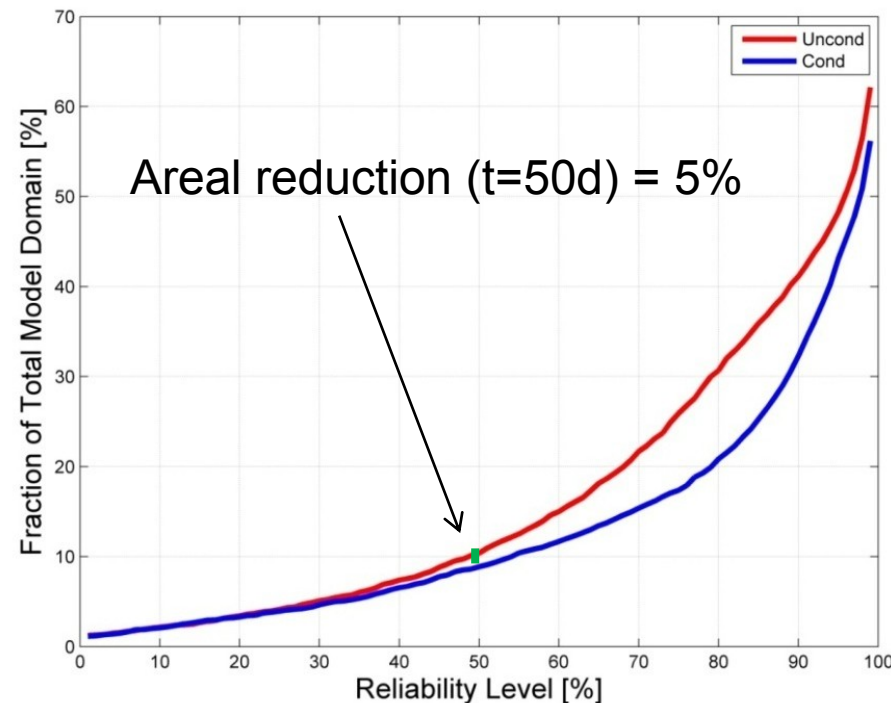


# Risk mapping results (conditional)



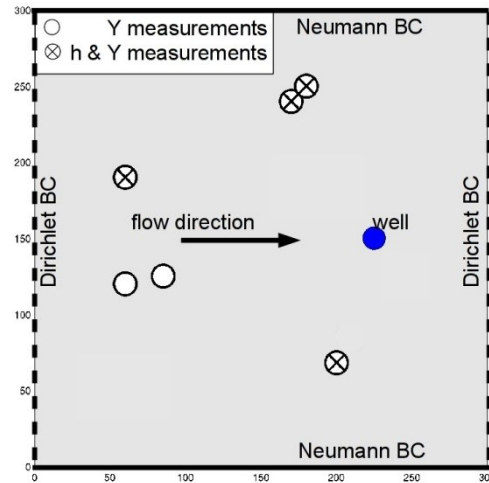
# Probabilistic Risk Management by financial means

1. Risk aversion
2. Uncertainty reduction by sampling
3. Alternative risk treatment methods
4. Areal demand costs in early-alert systems



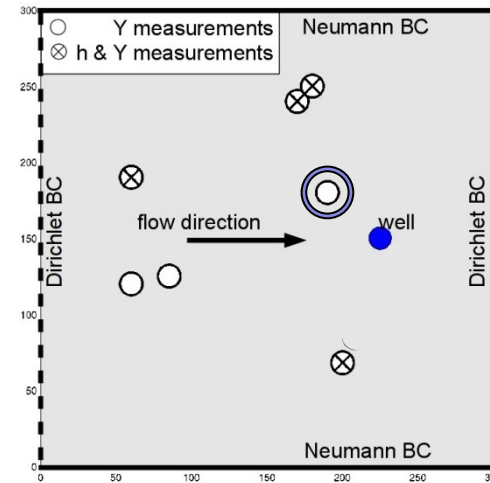
## 2) Cost reduction by areal uncertainty reduction

- Where to sample?
- How valuable is the investment?
- How many samples?



**Design 1**

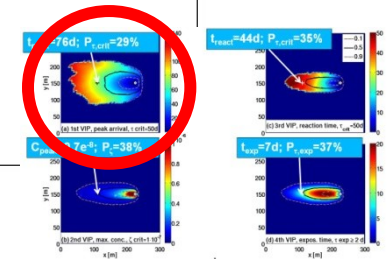
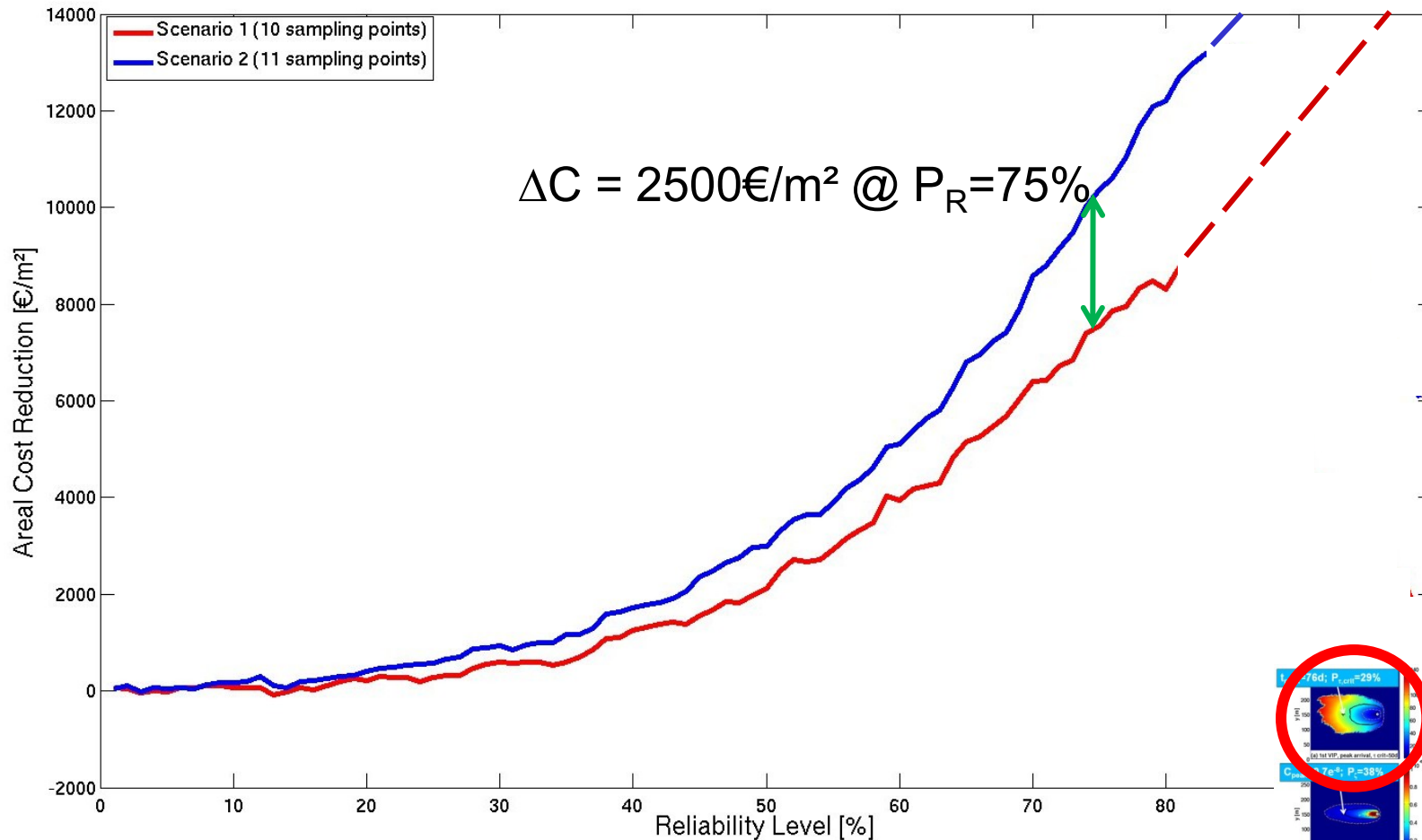
10 samples  
(6/4)



**Design 2**

11 samples  
(7/4)

## 2) Areal Cost Reduction by sampling



### 3) What is the Damage? – Choosing Alternatives

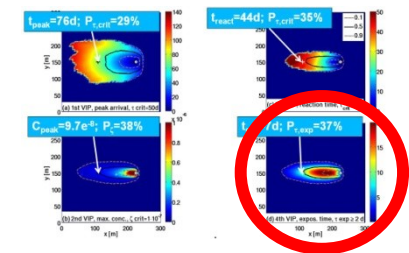
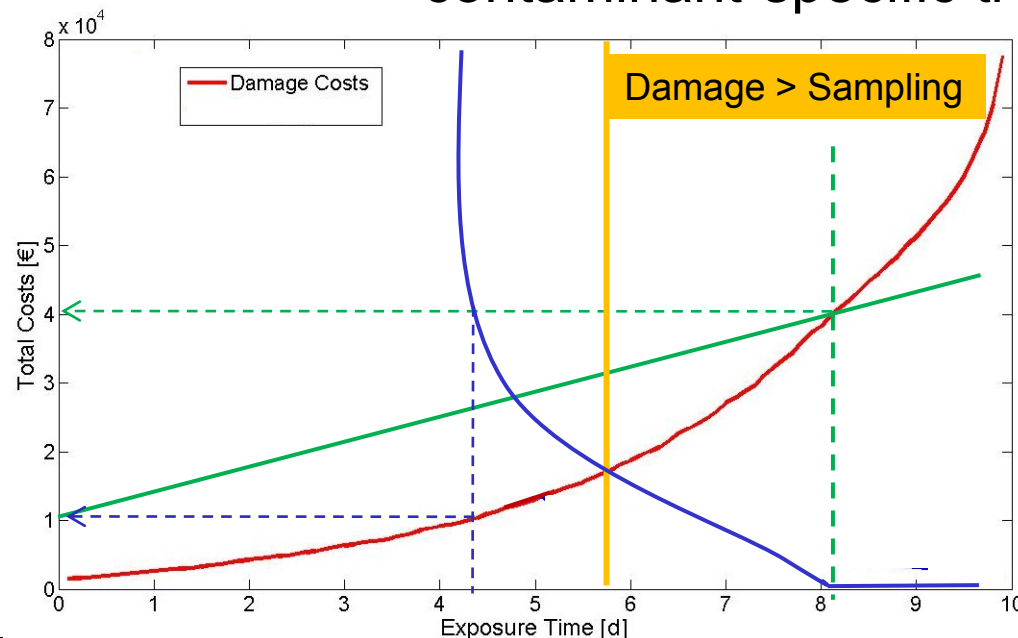
- Replacement Cost Method: Damage  $D_i$  [€]:

$$D_i = t_{\text{exp},i} \cdot Q_P \cdot \gamma_i$$

- $\gamma$  = cost function (e.g., water price [1.30€] or contaminant-specific treatment costs)

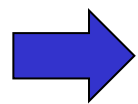
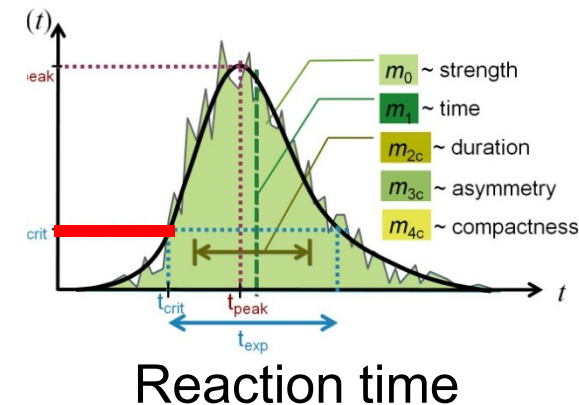
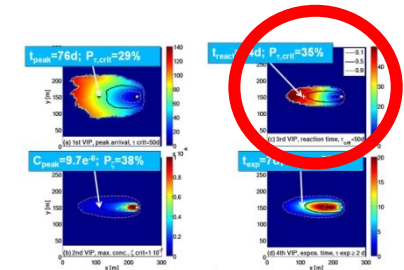
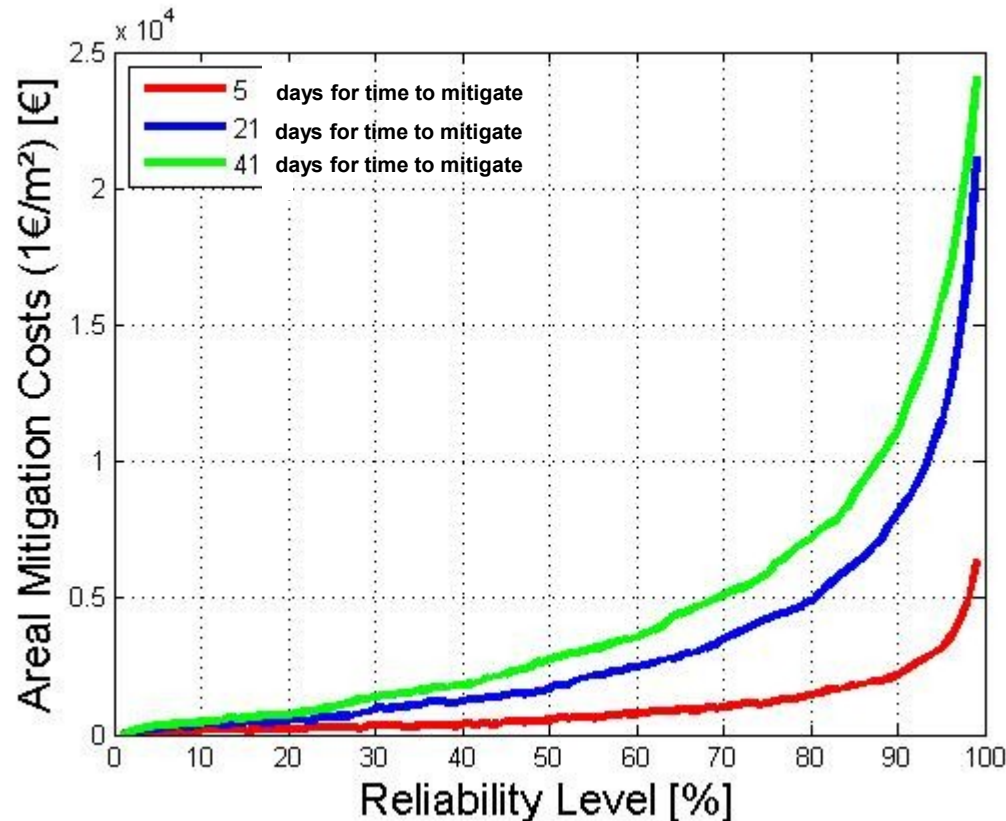
**Alternativ II:** Sampling  
@ location A,  
 $P_R = 90\%$

**Alternativ I:**  
Treatment





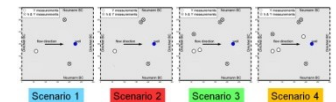
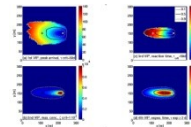
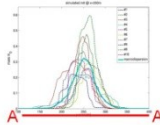
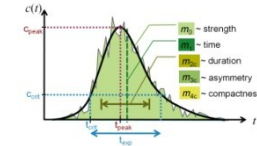
## 4) Areal costs until mitigation measures are installed



With increasing early-alert respond time the areal demand increases

# Summary

- 1 WVC are adequate for risk management
- 2 Separation between dilution, location and uncertainty
- 3 Indispensible information for risk management
- 4 The higher the risk aversion, the more expensive is RM
  - ➔ Sampling and uncertainty reduction pays back
  - ➔ Damage and alternative risk treatment
  - ➔ Fast early-alert respond can pay itself



## Thanks to ...



Independent Junior Research Group “Stochastic modelling of hydrosystems”  
within the DFG cluster of excellence in Simulation Technology (EXC 310/1)