



## From dilatancy to contraction: Stress-dependent failure mode progression in two porous sandstones subjected to true triaxial testing

Xiaodong Ma and Bezalel Haimson

University of Wisconsin, Madison, United States (bhaiinson@wisc.edu)

Porous sedimentary rocks such as sandstones are typical oil-bearing formations in which failure due to high stress concentration is likely to occur during wellbore drilling and subsequent operations. The objective of this research was to investigate the effect of  $\sigma_2$  on strength, failure-plane angle, and failure mode under realistically simulated field conditions ( $\sigma_1 \geq \sigma_2 \geq \sigma_3$ ). A series of true triaxial compression tests were conducted on two representative porous sandstones: Coconino (17.5% porosity, 99% quartz, with rounded and well-sorted 0.1 mm grains that are bonded by suturing and some quartz overgrowth), and Bentheim (24% porosity, 95% quartz, with sub-rounded 0.3 mm grains that are bonded exclusively by suturing).

Square cuboidal specimens (19 x 19 x 38mm) were subjected to independent loads in three principal directions, using the University of Wisconsin testing apparatus, creating a true triaxial state of stress ( $\sigma_1 \geq \sigma_2 \geq \sigma_3$ ). In all tests,  $\sigma_3$  and  $\sigma_2$  were maintained constant at predetermined levels, while  $\sigma_1$  was raised monotonically until failure occurred. The magnitude of  $\sigma_3$  varied between 0 and 150 MPa, covering the range of brittle behavior, brittle-ductile transition, and the threshold to the ductile zone in the weaker Bentheim sandstone. It was found that in both rocks the compressive strength ( $\sigma_{1,peak}$ ) for a given  $\sigma_3$  increases as the preset  $\sigma_2$  is raised between tests, and reaches a peak (15% over  $\sigma_{1,peak}$  when  $\sigma_2 = \sigma_3$  in the Coconino, and less than 10% in the Bentheim), beyond which it gradually drops, such that when  $\sigma_2 \approx \sigma_{1,peak}$ , the strength is approximately the same as when  $\sigma_2 = \sigma_3$ . This strengthening effect is considerably lower than that in previously tested crystalline rocks, such as Westerly granite and KTB amphibolite (more than 50%, Haimson, 2006). Plotting the test data in the  $\tau_{oct}$  vs.  $\sigma_{oct}$  domain, where the two stress invariants  $\tau_{oct}$ , the octahedral shear stress, and  $\sigma_{oct}$ , the mean normal stress, are both taken at failure), Coconino shows a monotonically rising  $\tau_{oct}$  with increasing  $\sigma_{oct}$ . In the Bentheim, on the other hand, the initially rising  $\tau_{oct}$  forms a 'cap' at about  $\sigma_{oct} = 200$  MPa, an indication of localized compaction, followed by a sharp decrease for larger magnitudes of  $\sigma_{oct}$ .

Failure characteristics in Coconino sandstone subjected to  $\sigma_3 = \sigma_2$  evolve from a dilatant mode, expressed by a single shear band, or fault, dipping steeply from 80° at  $\sigma_3 = 0$  MPa, to 60° at  $\sigma_3 = 100$  MPa; to a diminishing dilatant mode, signaled by multiple parallel and conjugate shear bands (a characteristic of brittle-ductile transition) dipping at nearly 50°, at  $\sigma_3 = 120$ -150 MPa. At low preset  $\sigma_3$ , failure plane dip increases by as much as 15° as  $\sigma_2$  is raised, but the increase gradually drops at higher  $\sigma_3$ . The role of  $\sigma_2$  in retarding the progression of the failure mode is noted, for example, at  $\sigma_3 = 100$  MPa, where characteristics of brittle-ductile transition are gradually reversed as  $\sigma_2$  is raised. The more porous Bentheim sandstone is generally weaker. When subjected to  $\sigma_3 = \sigma_2$  between 0 to 60 MPa, its failure mode is dilatant, leading to a single fault dipping 80° at  $\sigma_3 = 0$  MPa, to 50° at  $\sigma_3 = 60$  MPa. For a constant  $\sigma_3$ , failure-plane angle rises with  $\sigma_2$ , but the increase is typically under 10°, somewhat less than in the Coconino. In the range of 60 <  $\sigma_3$  < 80 MPa, dilatancy disappears and failure takes the form of multiple parallel and conjugate shear bands, dipping at nearly 45°. At  $\sigma_3 = 80$ -120 MPa, the Bentheim undergoes contraction, evidenced by stress-strain behavior and induced by the emergence of localized shear-enhanced compaction bands (less than 45° dip), evolving into pure compaction bands at  $\sigma_3 = 150$  MPa (dip approximately 0).