

**IRSN**

INSTITUT  
DE RADIOPROTECTION  
ET DE SÛRETÉ NUCLÉAIRE

*Faire avancer la sûreté nucléaire*

# The Fukushima releases: an inverse modeling approach to assess the source term by using gamma dose rate

O.SAUNIER, A.MATHIEU, D.DIDIER, M.TOMBETTE,  
D.QUELO, M.BOCQUET, V.WINIAREK

Anne.mathieu@irsn.fr

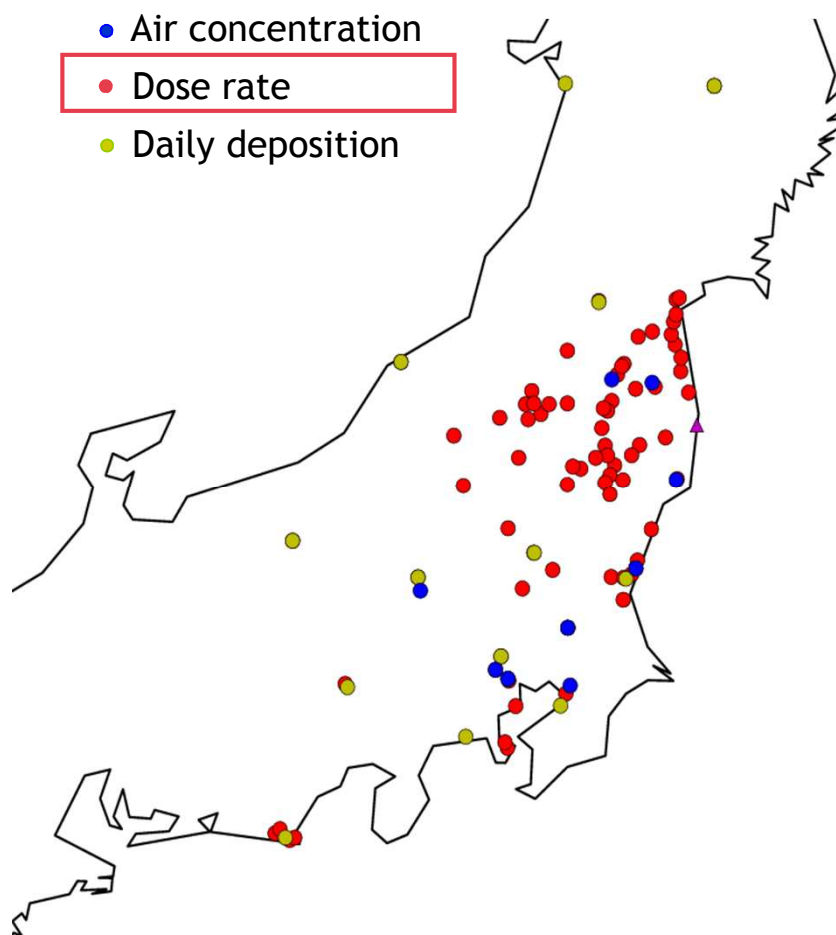


Centre d'Enseignement  
et de Recherche  
en Environnement  
Atmosphérique



- Chernobyl and Fukushima accidents proved that it can be tricky to estimate the releases in the atmosphere.
- The strong uncertainties of the release prevent
  - to have a complete understanding of the nuclear accident
  - to assess the actual impact on the population.
- To assess the emissions: Inverse modeling approach by using observations in the environment.

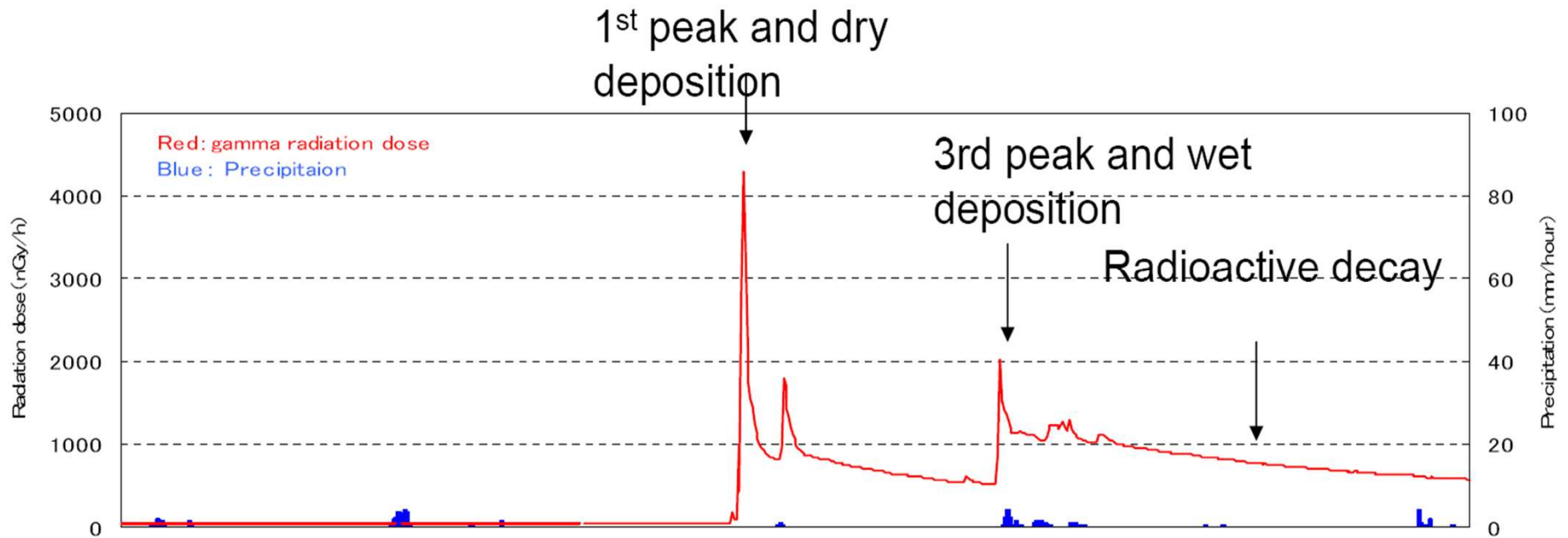




Observations	+	-
Air concentration	Easy to use (Model parameter & Isotopic composition)	Number & frequency (Very few data & Time averaged)
Deposition	Easy to use (Model parameter & Isotopic composition)	Number & frequency (Very few data during the release & Time integrated)
<b>Dose rate</b>	Number & Frequency	Difficult to use (Not a model parameter & Aggregate all the gamma radiations emitted by any radionuclides present on the ground and in the air)

- Inverse modeling approach : the novelty of the method is the use of dose rate observations (70 stations and 381 time steps between 11<sup>st</sup> and 27<sup>th</sup> March).

## Gamma dose rate observations



The signal is mainly due to 8 radionuclides:  $^{134}\text{Cs}$ ,  $^{136}\text{Cs}$ ,  $^{137}\text{Cs}$ ,  $^{137\text{m}}\text{Ba}$ ,  $^{132}\text{Te}$ ,  $^{132}\text{I}$ ,  $^{131}\text{I}$ ,  $^{133}\text{Xe}$   
 Secular equilibrium ( $^{137}\text{Cs}/^{137\text{m}}\text{Ba}$ ,  $^{132}\text{Te}/^{132}\text{I}$ ) & Constant ratio ( $^{134}\text{Cs}/^{137}\text{Cs}$ )

➤ **Objective: estimate the release rate of 5 radionuclides:  $^{134}\text{Cs}$ ,  $^{136}\text{Cs}$ ,  $^{132}\text{Te}$ ,  $^{131}\text{I}$  and  $^{133}\text{Xe}$**

### How to use dose rate signal ?

- ❑ Plume detection when it blew over the station ➡ timing of the release events.
- ❑ The slope due to the radioactive decay of the deposit ➡ isotopic composition.
- ❑ The value of the observed dose rate ➡ quantities released.

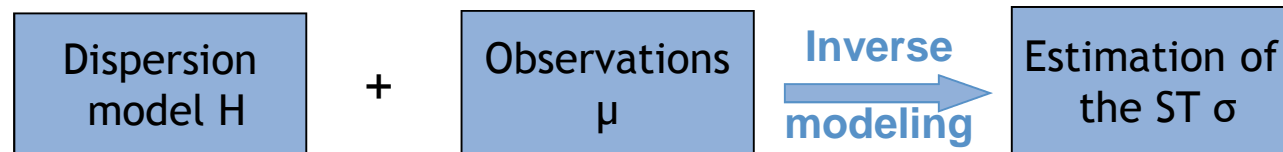
■ The **inverse problem** to solve can be formalized by:

Source term (ST): temporal evolution of the release rate + distribution between radionuclides

$$\text{Vector of errors} \rightarrow \varepsilon = H\sigma - \mu \leftarrow \text{Vector of measurements}$$

Source receptor matrix  
computed with the forward atm. model (Abida et al. 2011)

Estimator of the ST



■ The objective is to assess the ST  $\sigma$  so that the error  $\varepsilon$  is minimized.

**Cost function** (minimized by using L-BFGS-B algorithm)

$$J(\sigma) = \frac{1}{2}(\mu - H\sigma)^T R^{-1}(\mu - H\sigma) + \frac{1}{2}(\sigma - \sigma_b)^T B^{-1}(\sigma - \sigma_b)$$

■ **Hypothesis**

- No prior knowledge of the ST ( $\sigma_b = 0$ )
- Simple parameterizations (Winiarek et al., 2011):  $R = B = I$



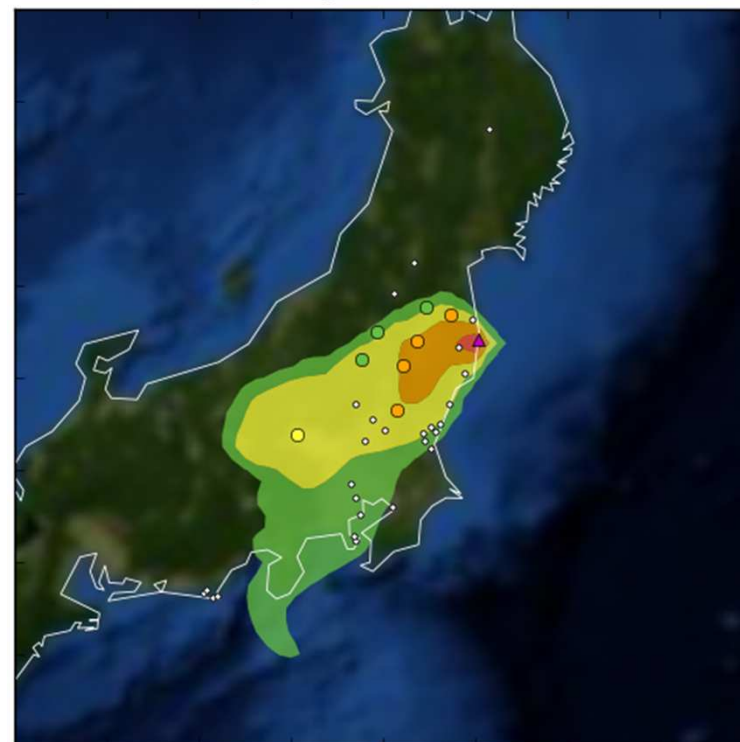
## ■ Eulerian dispersion model Id $\chi$ from the operational C3 $\chi$ platform.

- Dry deposition:  $v_{\text{dep}} = 2 \cdot 10^{-3} \text{ cm/s}$
- Wet deposition:  $\Lambda_s = a p_o^b$ , with  $a = 5 \cdot 10^{-5}$  and  $b = 1$
- Vertical diffusion: Troen and Mahrt scheme
- Radioactive decay + filiation

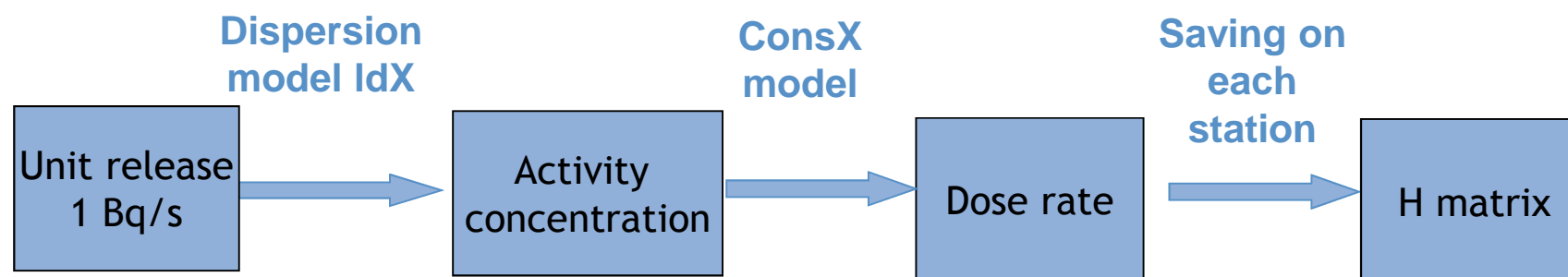
Met. data: ECMWF ( $0.125^\circ$ )

Spatial resolution:  $0.125^\circ \times 0.125^\circ$

Time resolution: 1 hour



## ■ Consequences model : cons $\chi$ from C3 $\chi$



## ■ Inverse modeling method

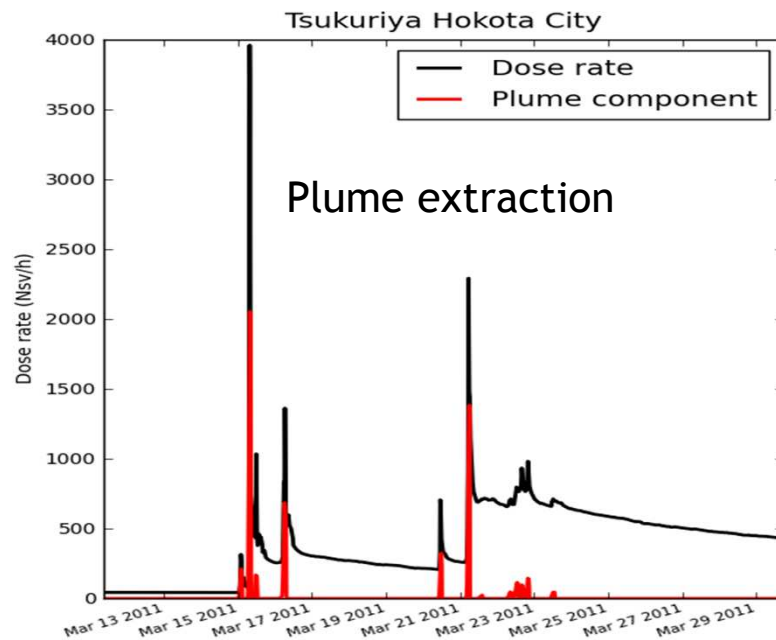
Raw dose rate measurements cannot be used directly: inverse problem not sufficiently constrained

➤ **Solution to solve the inverse problem: reduce the number of parameters + limit the solution space**

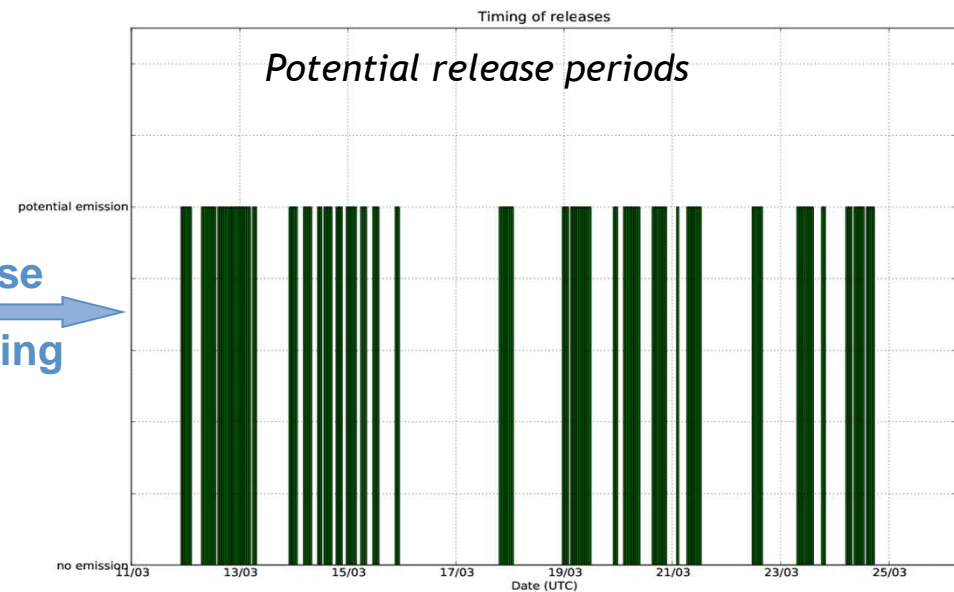
- ❑ **Isotopic composition of the ST: only 5 radionuclides**
- ❑ **A two steps method**
  1. Identify the potential release periods
  2. Assess the release rates during periods identified in step 1
- ❑ **Add isotopic constraints: radionuclides released in proportions that depends on their physicochemical properties + the core inventory**

## Step 1: Inverse modeling to identify the potential release periods

Measurements: dose rate due to the plume component for 70 stations



Inverse  
modeling



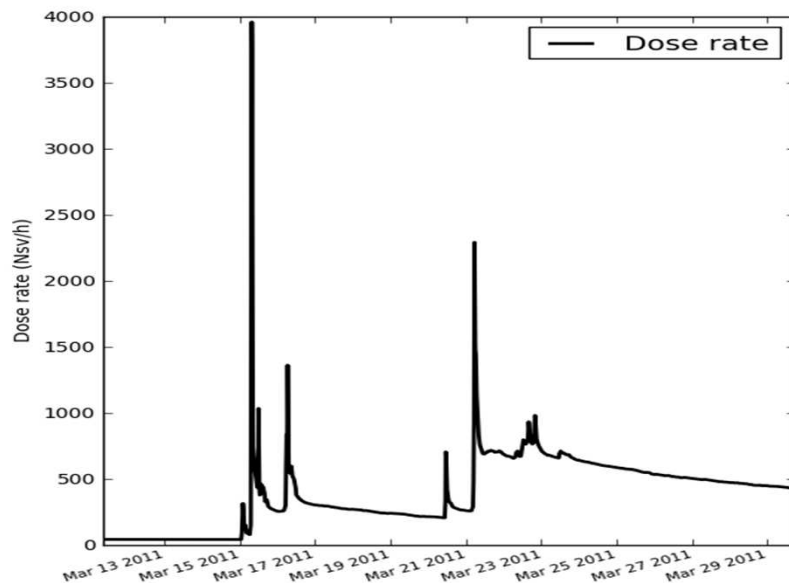


## Step 2: Inverse modeling to assess the release rates during periods identified in step 1

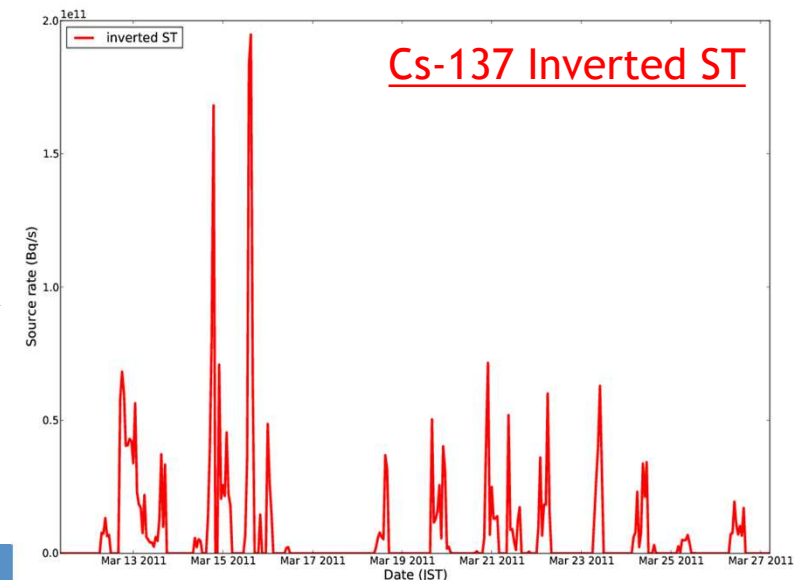
- ❑ Measurements: the complete dose rate signal on 70 stations
- ❑ Soft constraints on isotopic ratio are imposed (based on analysis of core reactor and air concentrations measurements in Japan)

- ❑ The cost function to minimize uses a regularization function which contains information about isotopic ratios

$$(\quad) - (\quad) \quad (\quad) - (\quad) \quad (\quad)$$



Inverse  
modeling



## Comparisons with other ST

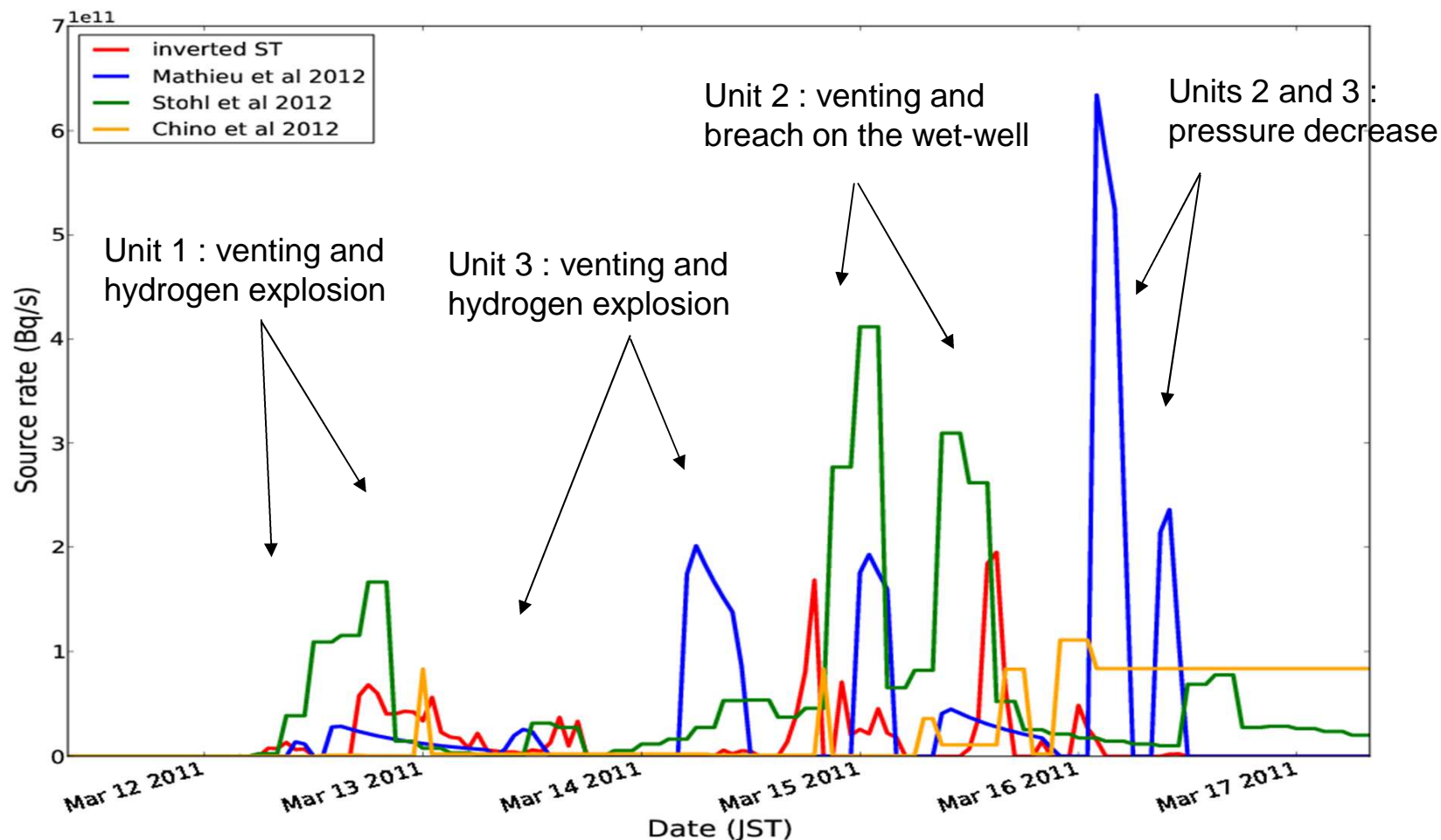
Source Term (PBq)	$^{133}\text{Xe}$	$^{131}\text{I}$	$^{132}\text{I}$	$^{137}\text{Cs}$	$^{136}\text{Cs}$
<b>Inverted ST</b>	<b>12100</b>	<b>103</b>	<b>35.5</b>	<b>15.5</b>	<b>3.7</b>
<b>Mathieu et al. (2012)</b>	<b>5950</b>	<b>197</b>	<b>56.4</b>	<b>20.6</b>	<b>9.8</b>
Winiarek et al. (2012)	-	190-380	-	12-19	-
Terada et al. (2012)	-	150	-	13	-
Stohl et al. (2012a)	13400-20000	-	-	23.3-50.1	-
TEPCO (2012)	500	500	-	10	-

Inverted quantities are **consistent with the other estimations**.

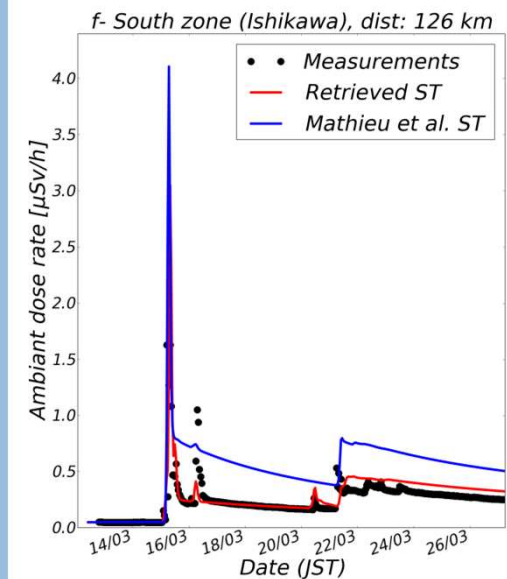
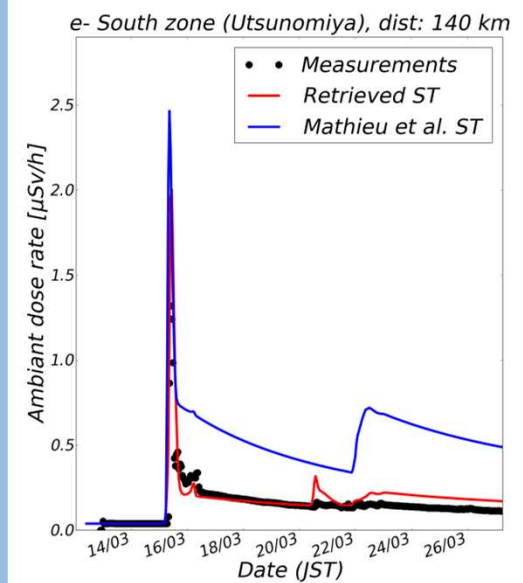
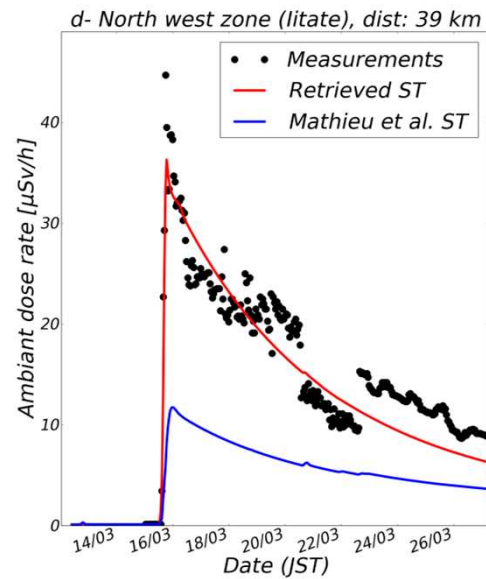
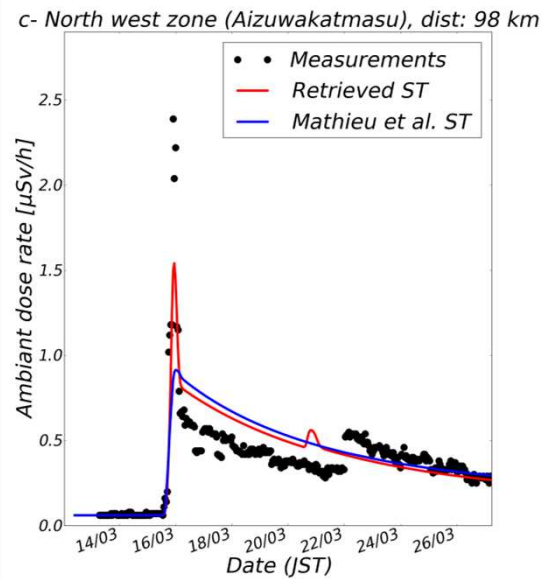
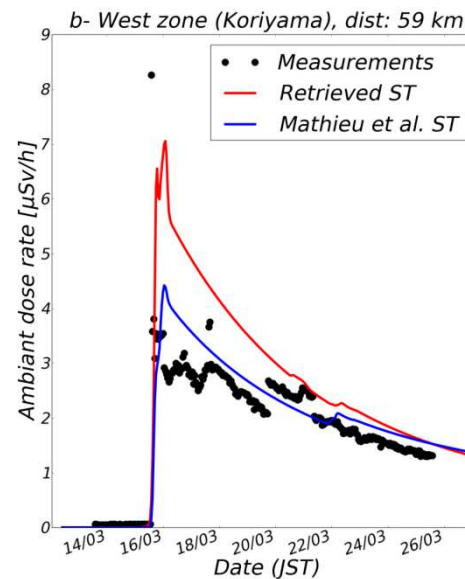
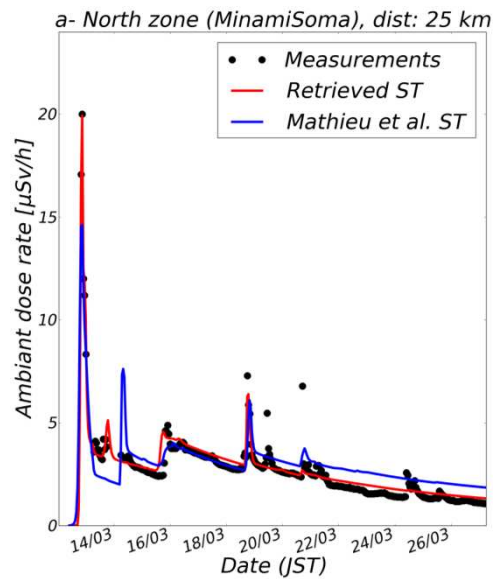
Underestimation in iodine and cesium in comparison with Mathieu et al ST (several events are not identified by inversion).

Amount of noble gases is similar to Stohl et al estimation: probably overestimated

## Comparisons with other ST



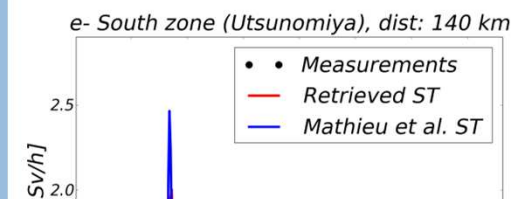
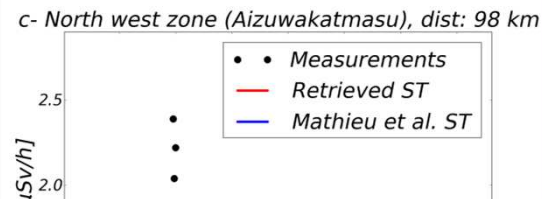
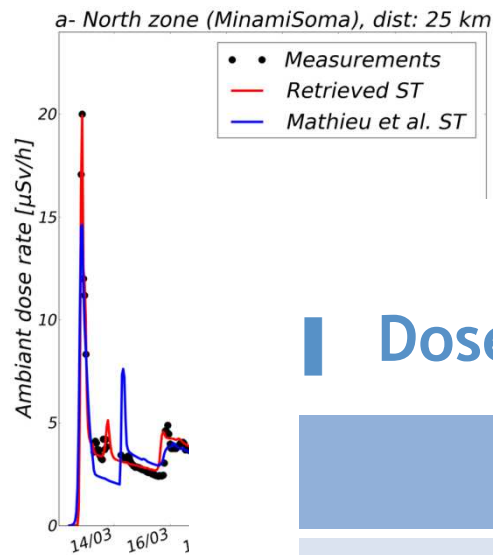
- The main release events are well reproduced by the inverted source.
- Events occurred on the reactors 1 and 3 are uncertain (too few observations).
- Amounts of radionuclides are quite different depending on the source term.



Good agreement between model and observations.

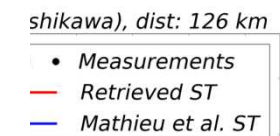
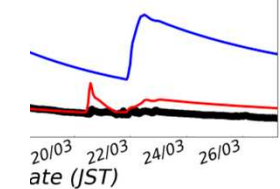
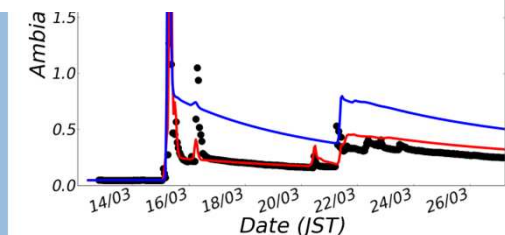
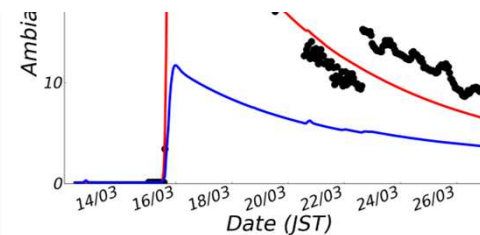
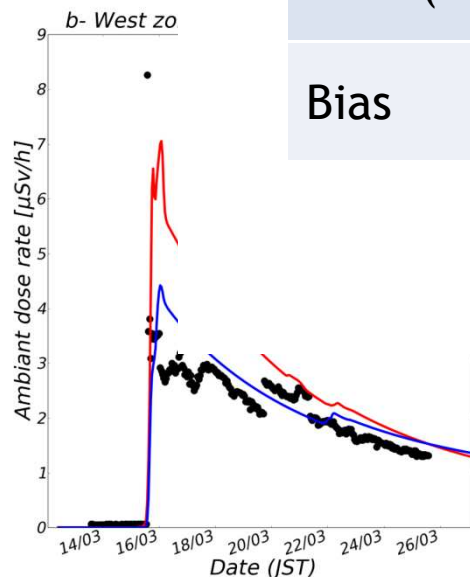
Additional releases are identified with the inverse modeling method.

Discrepancies are due mainly to inaccurate meteorological fields.



## Dose rate

	Inverted ST	Mathieu et al. ST
Fac2 (%)	79.8	60.0
Bias	0.42	0.59

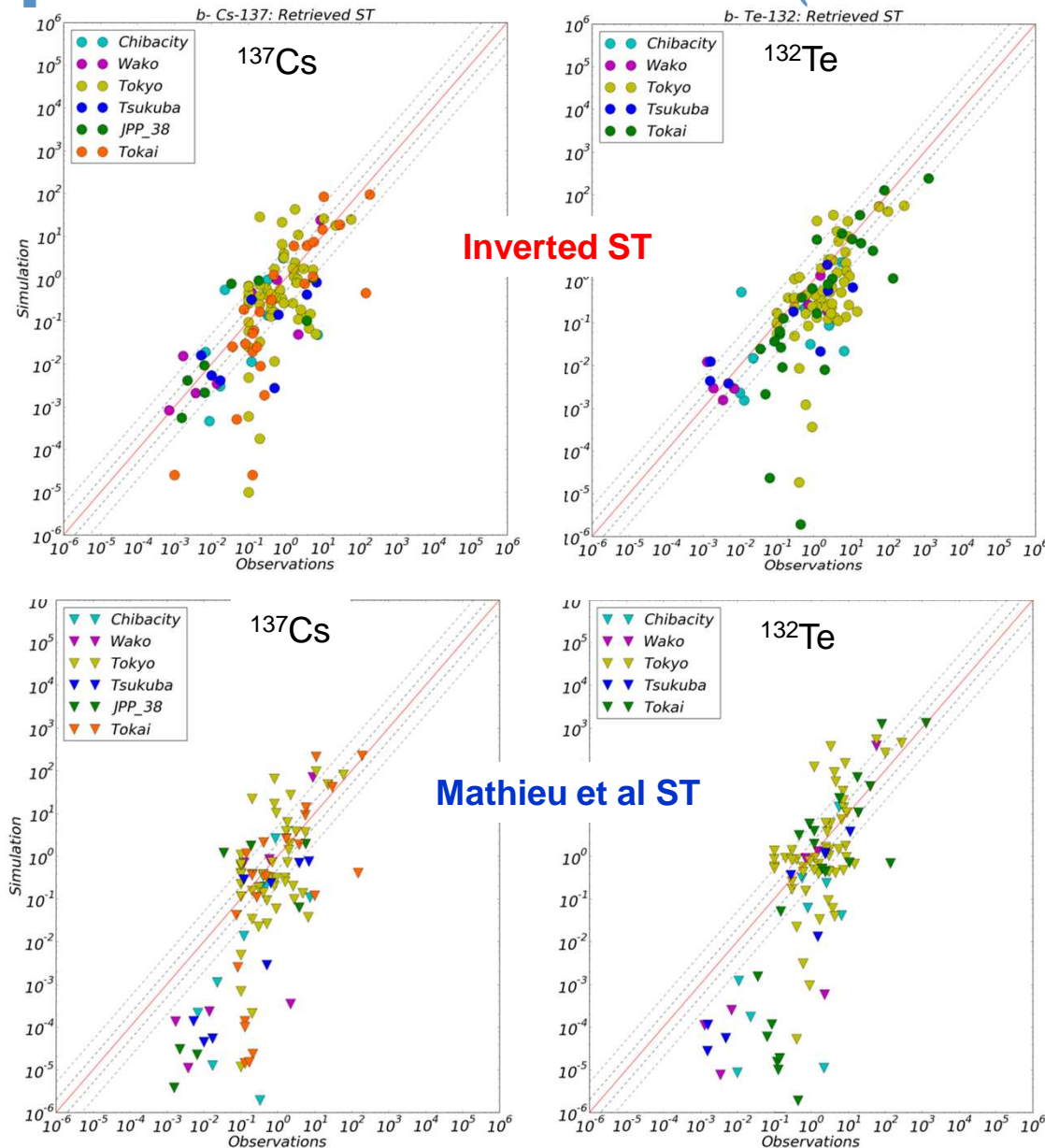


Good agreement between model and observations.

Additional releases are identified with the inverse modeling method.

Discrepancies are due mainly to inaccurate meteorological fields.

# Air concentration measurements (not used in the inverse process)



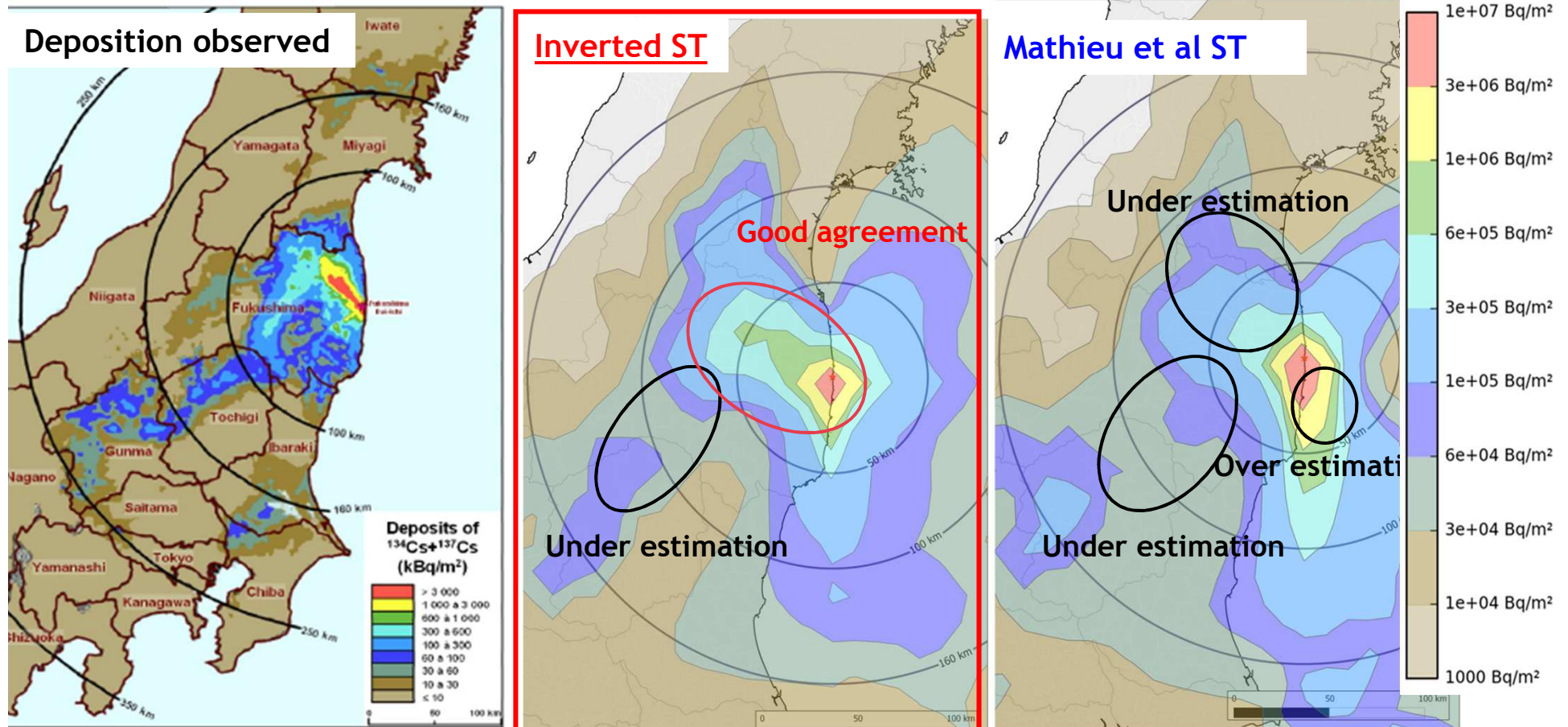
Good enough agreement between model (with inverted ST) and observations.

Realistic isotopic composition.



## Reconstruction of the Fukushima source term

### Total Cs-137+ Cs-134 deposition (not used in inversion)



- In the north-west of the plant, good agreement between model (with inverted ST) and observations (not used to assess the ST).
- The agreement is not perfect in some areas (Tochigi and west Fukushima prefectures).
- Differences are due mainly to inaccurate meteorological fields (precipitation, wind) and deposition scheme.

### Reliable inversed modeling method to assess the source term by using dose rate measurements

### Performances

- ❑ Good results achieved on the Fukushima accident.
- ❑ The quality of the meteorological forecast is a key point to retrieve a realistic source term.

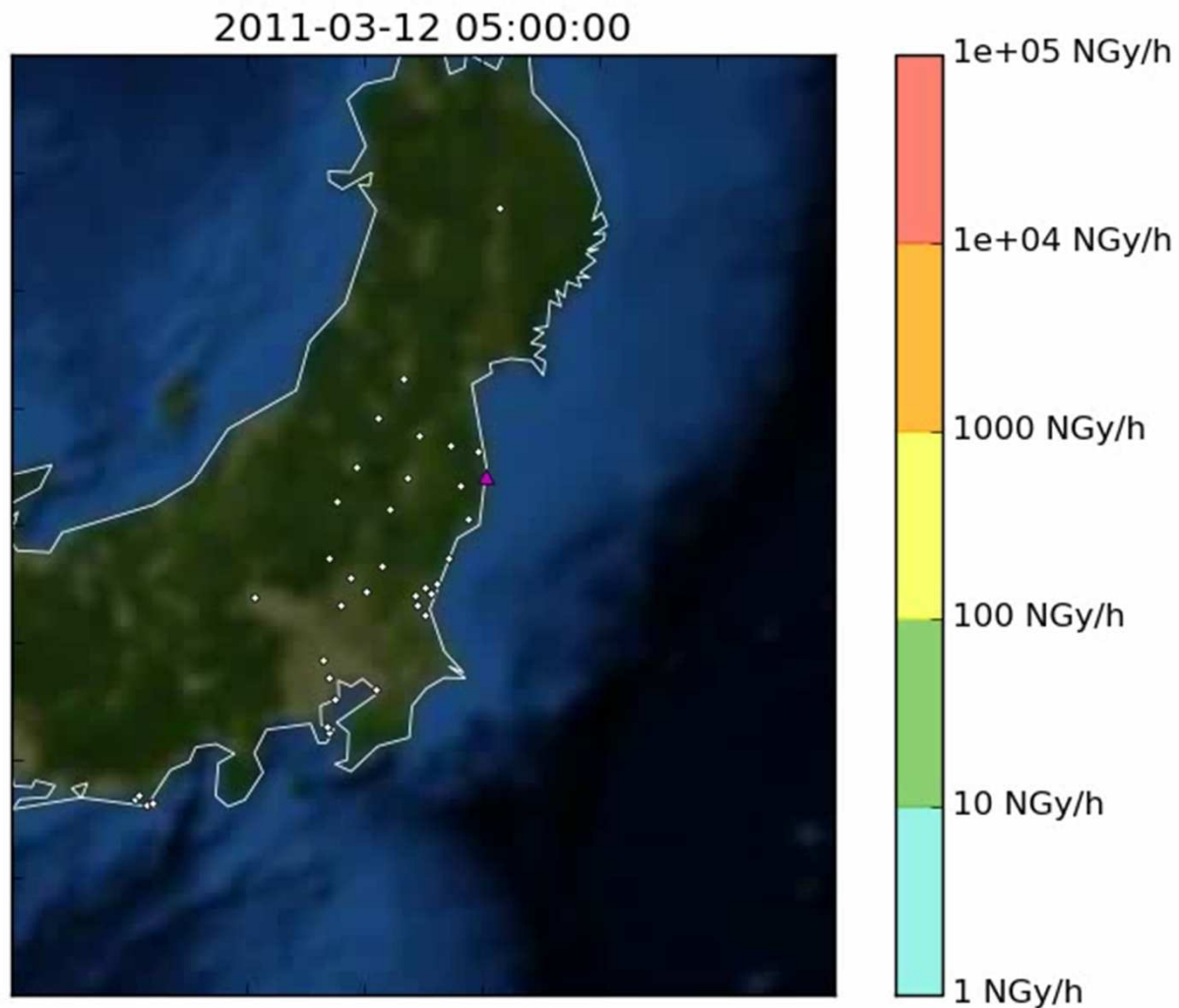
### Use

- ❑ Perfectly suited to crisis management.
- ❑ Efficient tool to improve the understanding of an accident.

### Perspectives

- ❑ Improve the reconstruction of the isotopic composition (Iodine 132): air concentration, deposition and dose rate observations.
- ❑ Extend the method to all spatial scales.

# Thank you for your attention



■ Model to data comparisons (dose rate - plume component)