



# A Scalable Lagrangian Approach to Model Soil Water Dynamics in Structured Soils

a link between observables and hydrological process modelling from single macropores to the lower mesoscale

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# Motivation

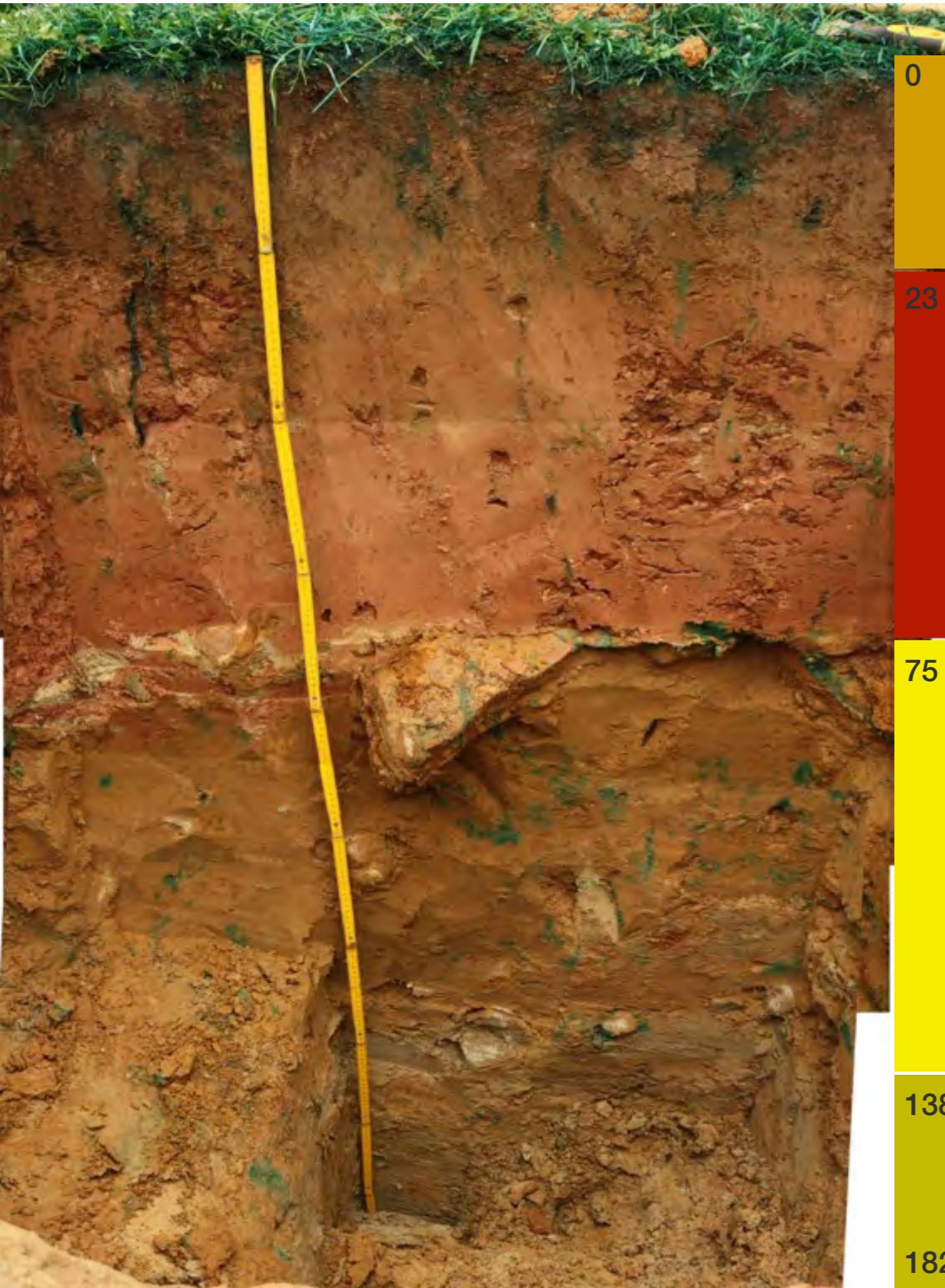


Example: Hoevelange, Attert, Luxembourg



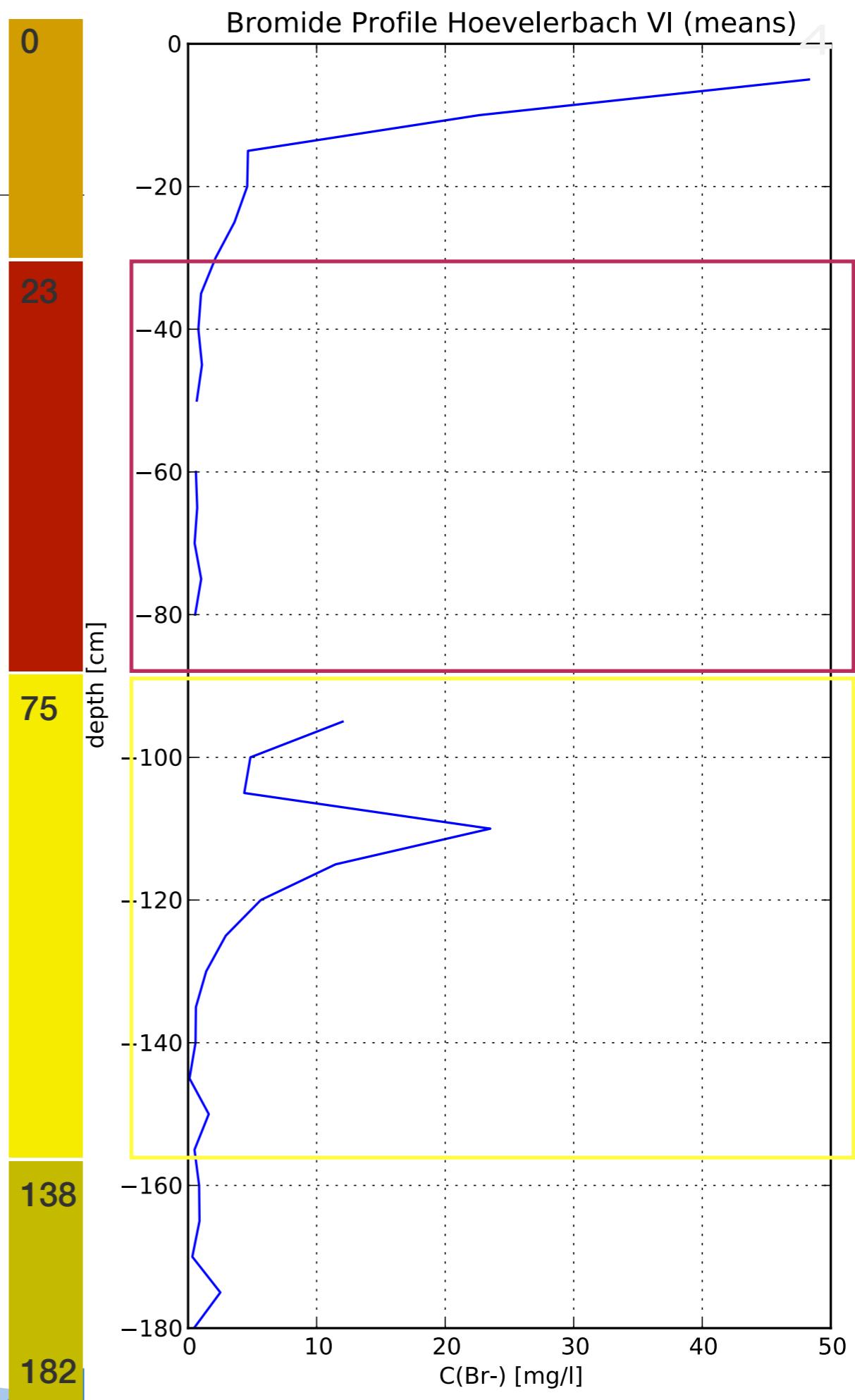
Example: Weißenitz, Saxony, Germany

- Soil has organised structures (earth worms, cracks, roots, rodents...)
- Preferential flow occurs virtually anywhere and across scales
- „Heterogeneity“ is intrinsic (domain, processes, states)
- Need to look at interactions within the whole system



# Irrigation Experiment

Hoevelange, Attert,  
Luxembourg  
50mm, 1h, 1.2m<sup>2</sup>  
Brilliant Blue + Br<sup>-</sup>



# Main Preceptions

Physical description of hydrological processes as dissipation of energy<sup>1</sup>.  
Observability of potential „parameters“  
Scalability of plot to lower mesoscale

- this requires some central conceptual revisions

(1) Kleidon, A., Zehe, E., Ehret, U. and Scherer, U.: Thermodynamics, maximum power, and the dynamics of preferential river flow structures at the continental scale, *Hydrol. Earth Syst. Sci.*, 17(1), 225–251, doi:10.5194/hess-17-225-2013, 2013.

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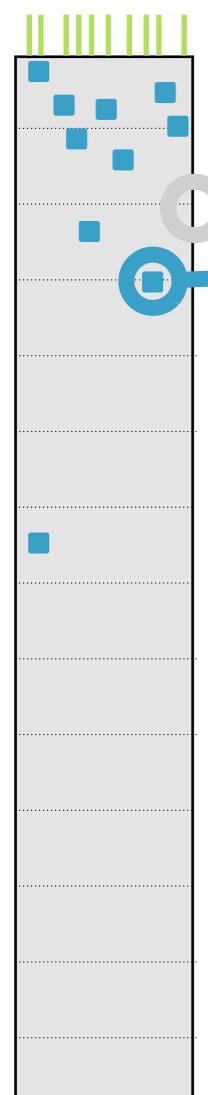
## Outline

Present Lagrangian model concept  
Results of 1D model  
Pore-centred abstraction and 1.5D model  
Discussion of Interfaces

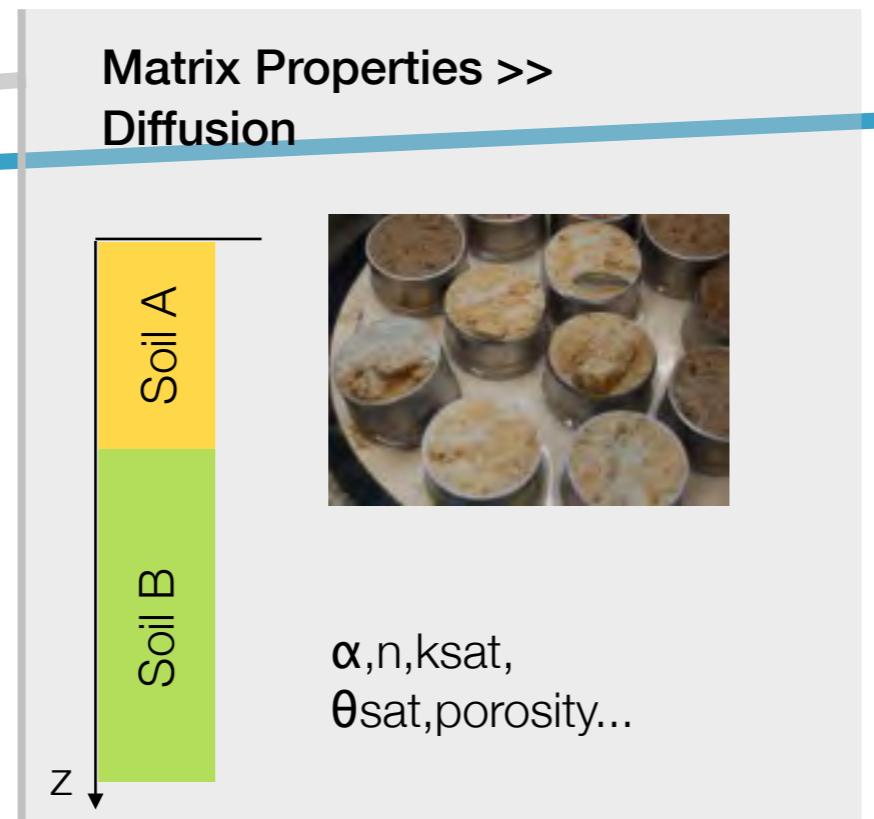
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# General Concept

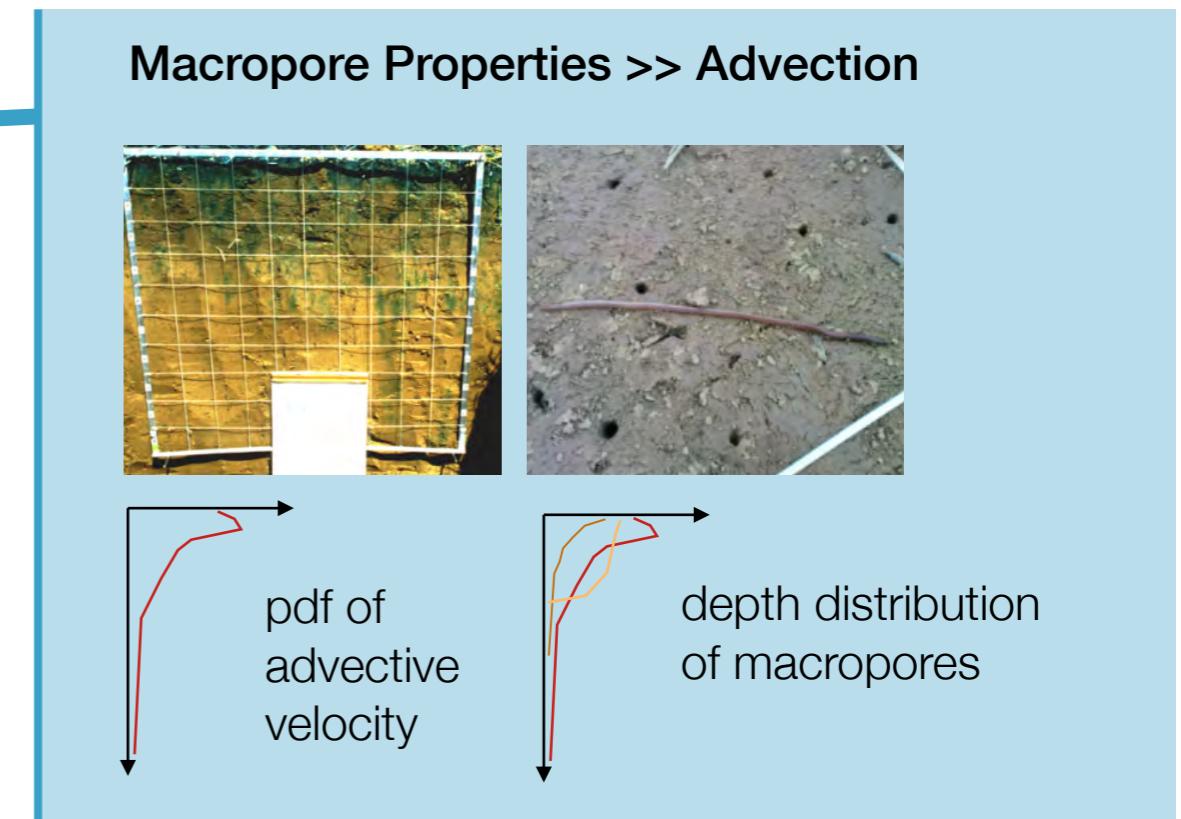
Soil Column



Eulerian grid for REV concepts (e.g. psi) of the „static“ domain

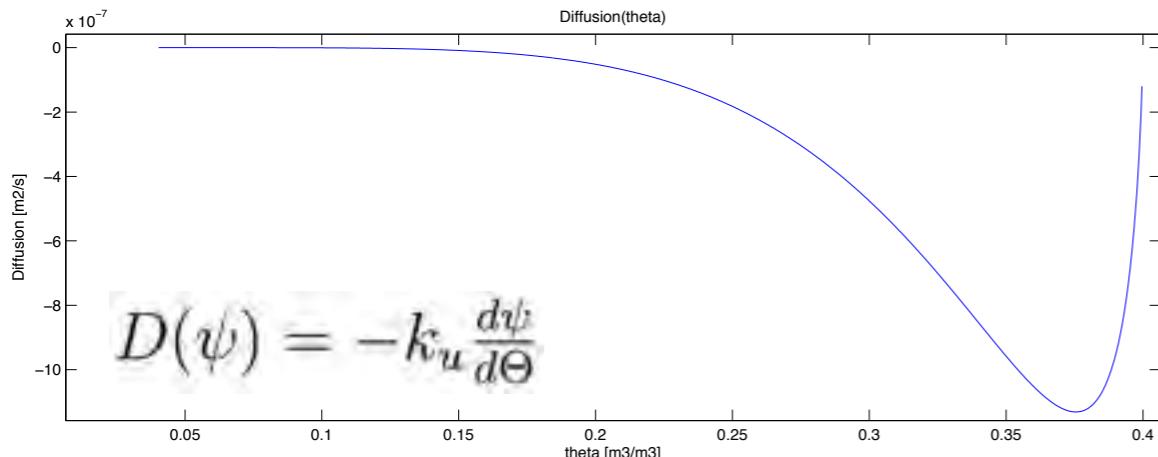


Lagrangian representation of the water (particles)



# Model Core

Diffusion → Random Walk



Random Walk Step:

$$x_i + \xi_{-1}^1 * \sqrt{6D_i dt}$$

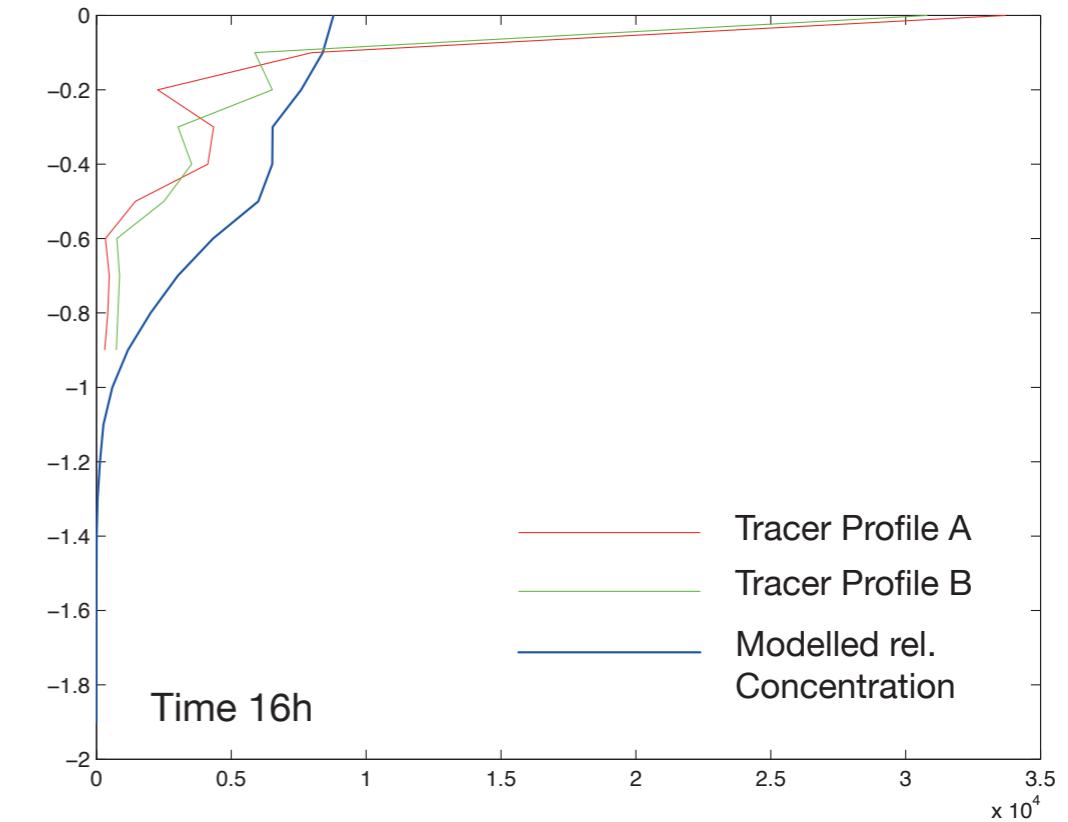
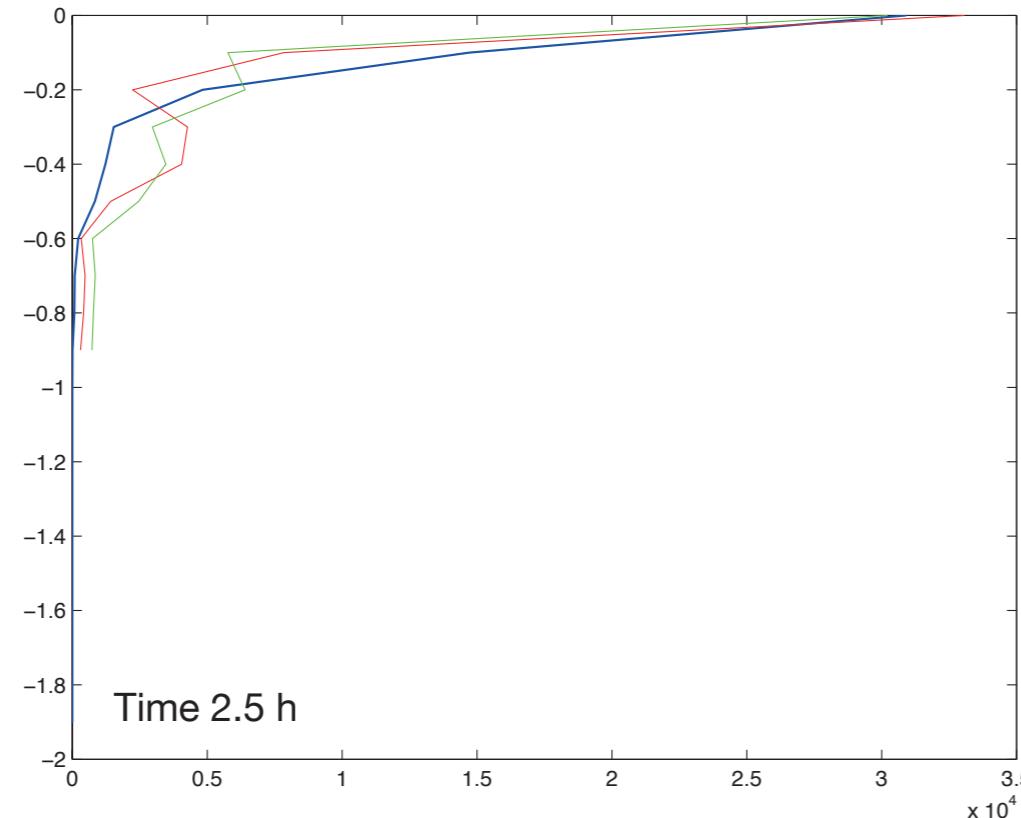
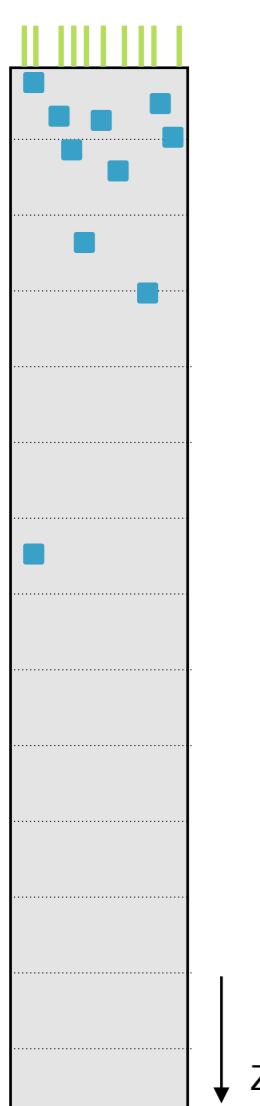
Advection → Deterministic Step

$$x_i + v_{adv} dt$$

# Particle Approach 1D

Soil Column

particle approaches for tracer and heat transport > so use it directly

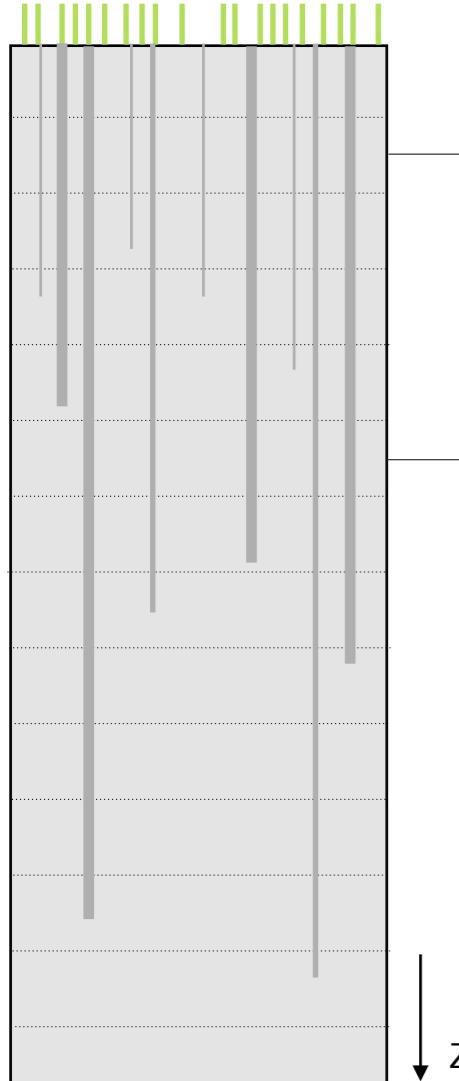


We can mimic observed tracer profiles (advection, contaminant transport)

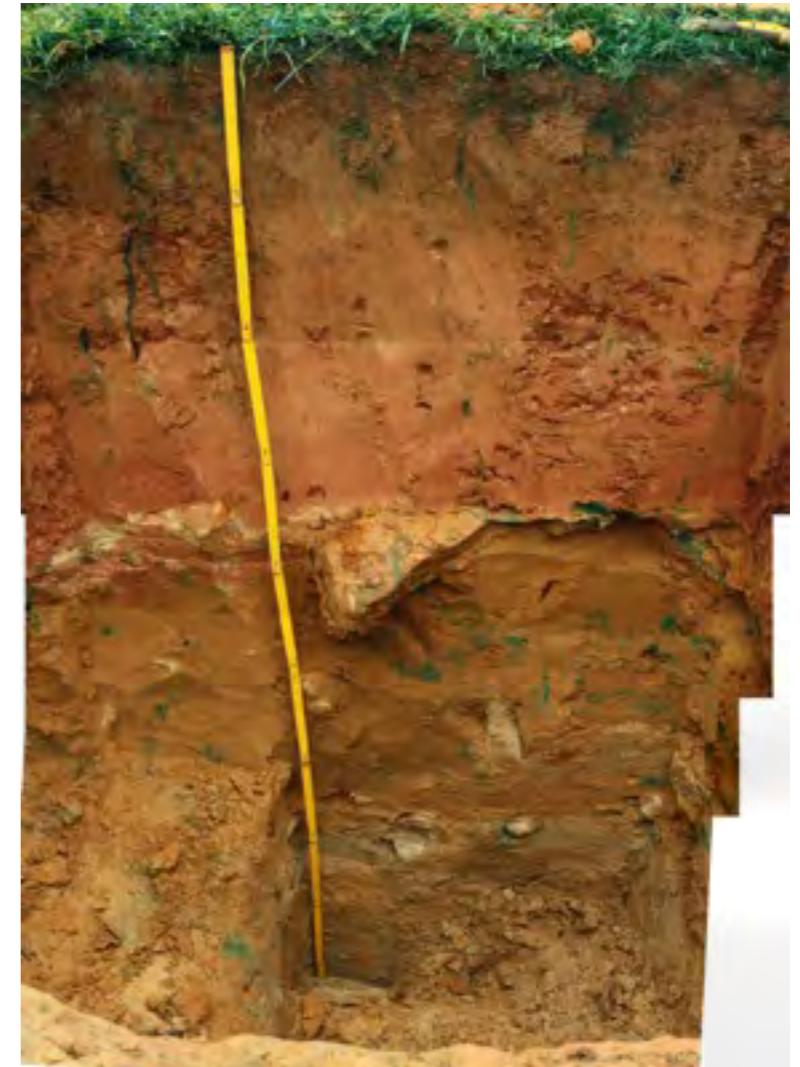
BUT we lack macropore-matrix interaction, the timing when advection ends and skewed lateral moisture distributions

# Prototype 1.5D

Pore-centered abstraction  
from areal share of macropores  
and given radius distribution with  
assumed circular shape

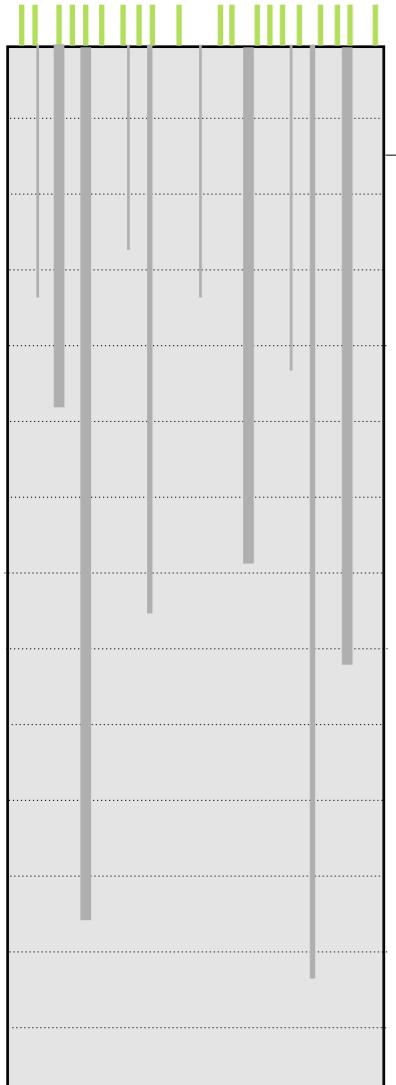


- area/volume of macropores
- min | mean | max radius
- coating factor
  
- share & density of macropores
- distance distribution from macropores



# Prototype 1.5D

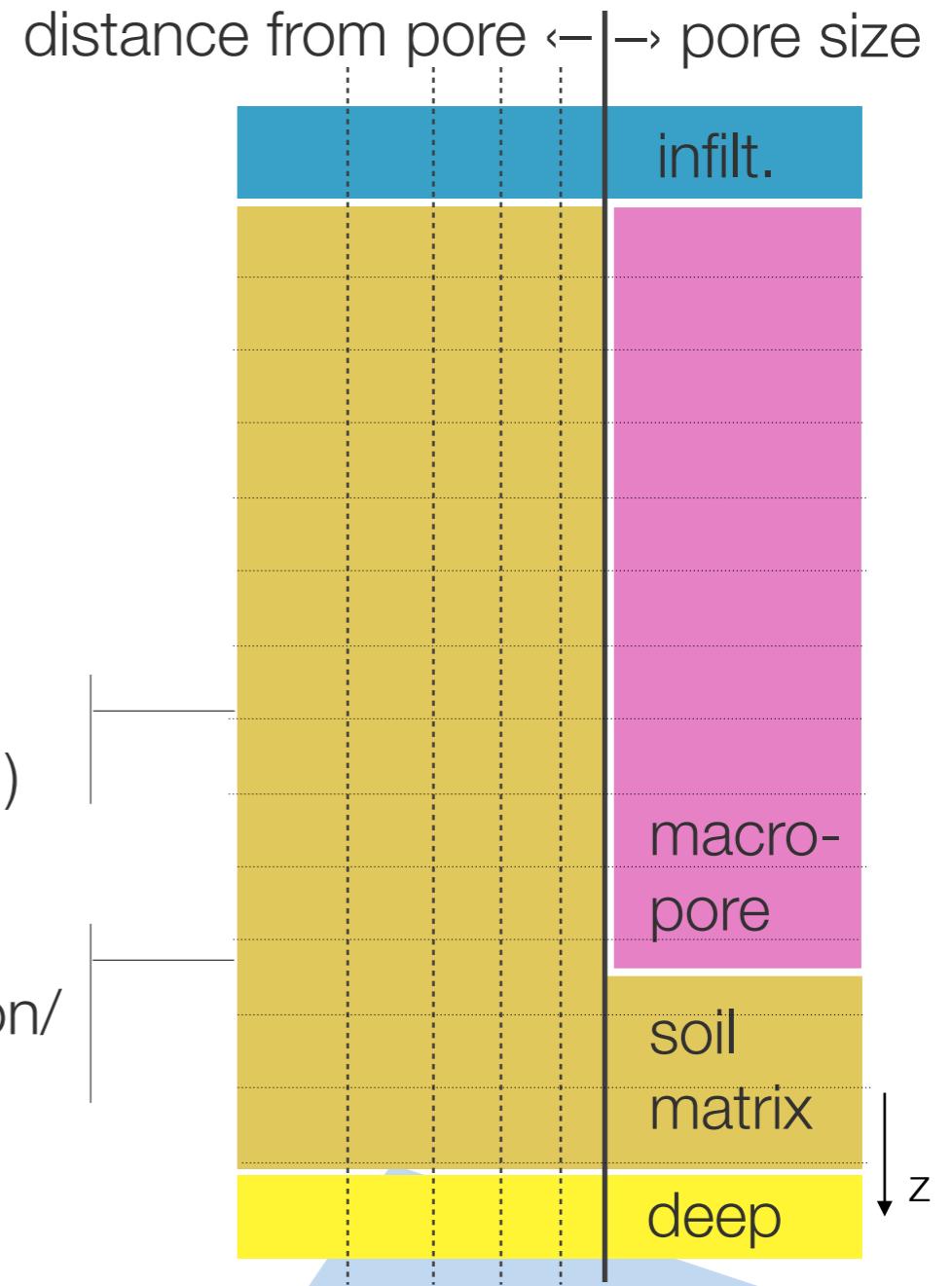
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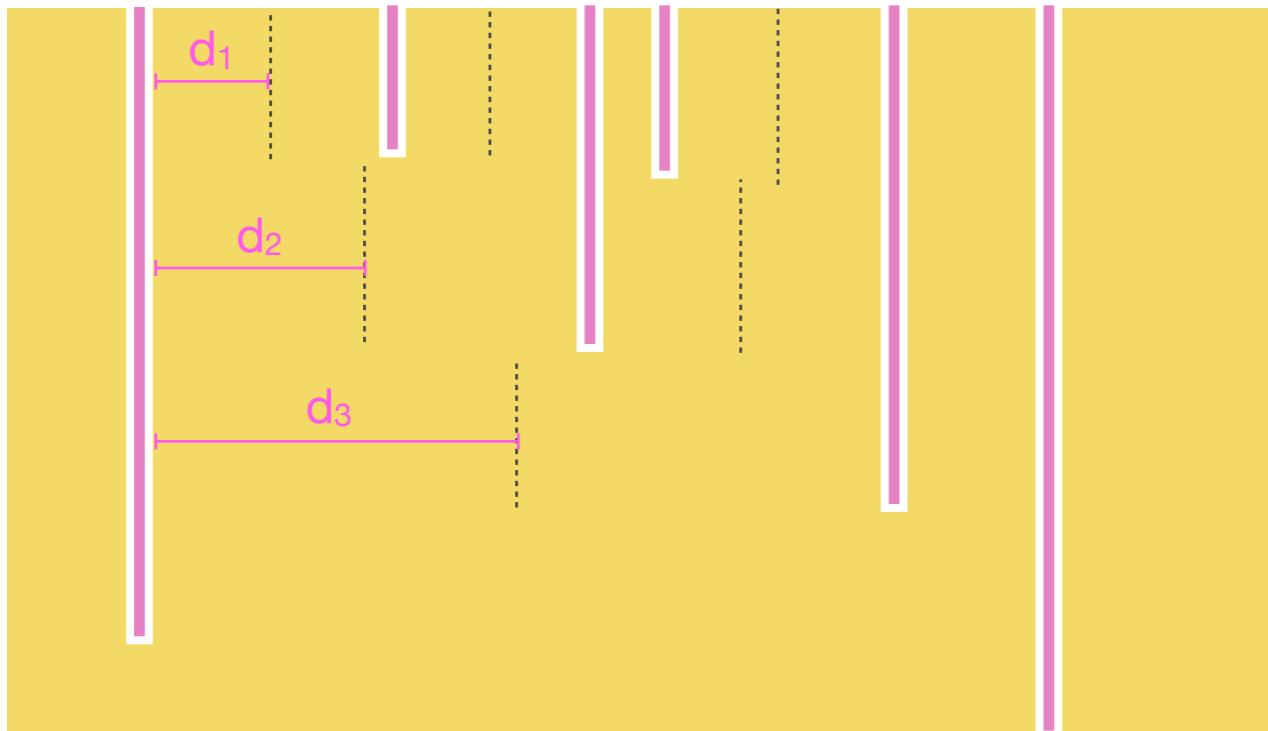
Eulerian (grid):  
▸ REV properties (psi...)

Lagrangian (free):  
▸ water particle diffusion/  
advection

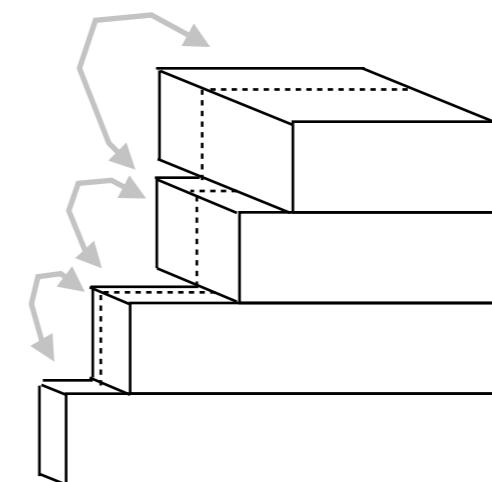
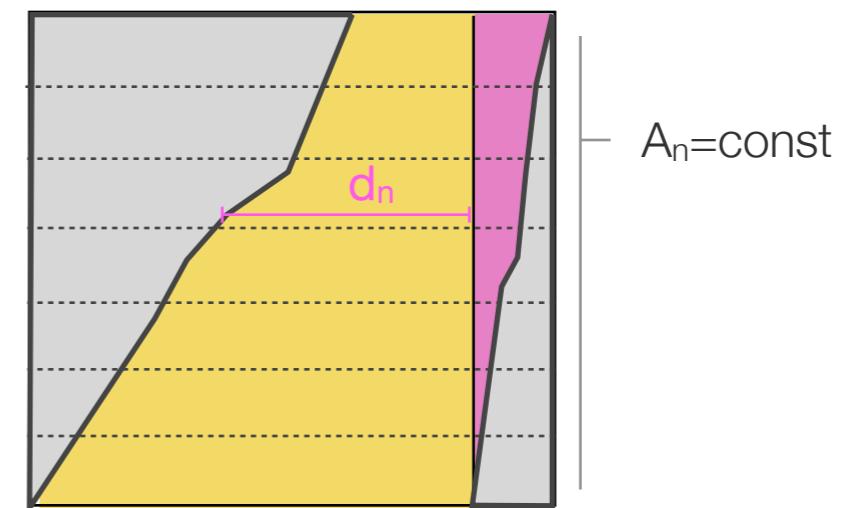


# Prototype 1.5D Virtual 3rd Dimension

abstraction with many macropores



virtual 3rd dimension



random  
distribution  
to tails

# Prototype 1.5D Macropore-Matrix Interaction

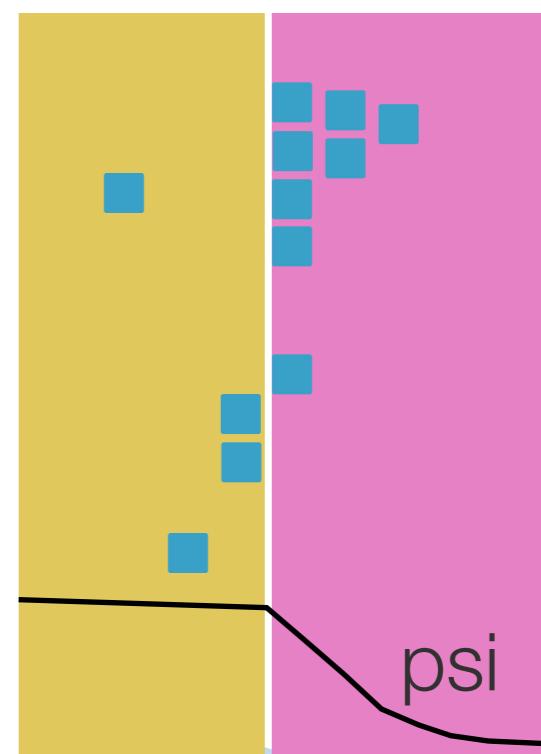
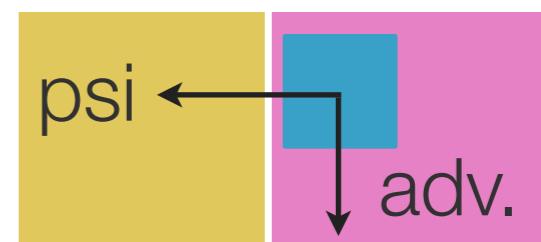
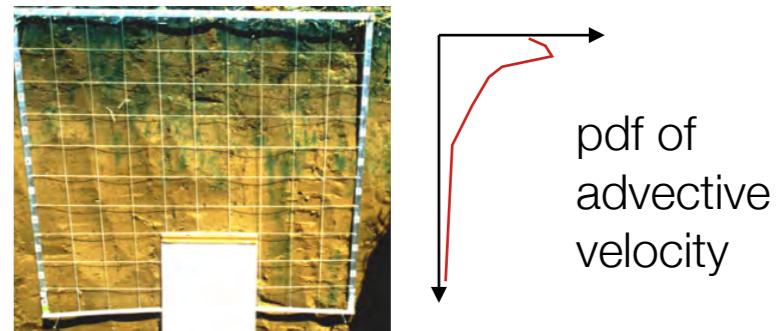
Macropores allow advection

- once a particle enters the domain, its adv. velocity is drawn from pdf (tracer experiment)
- retardation of advection through:

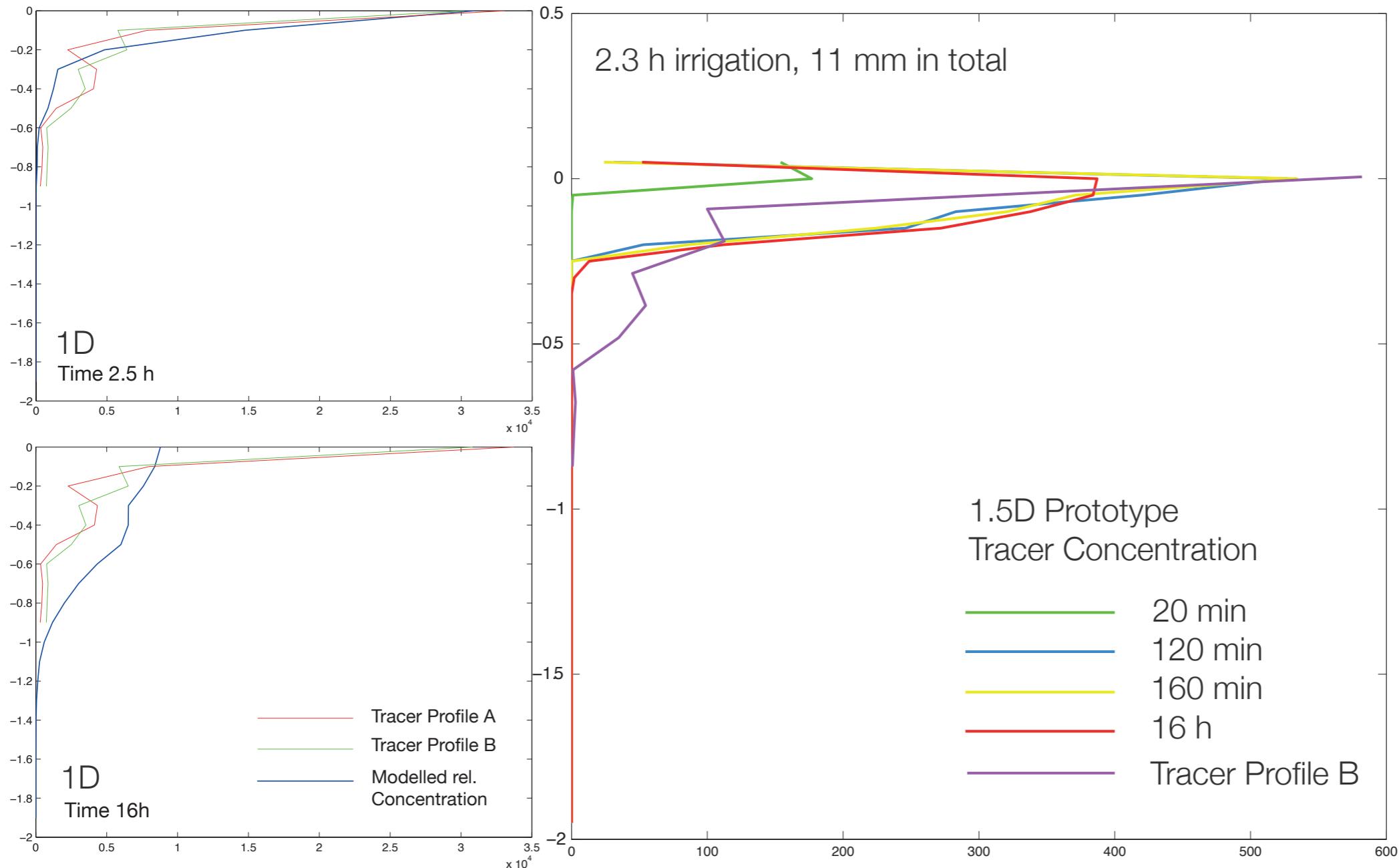
$$r = \frac{E_{binding}}{E_{kin}} = \frac{\psi_{exp} * g}{\frac{m}{2} * v_{adv}^2}$$

Particles „stick“ to pore wall

- distance from pore wall is a function of local filling
- infilt./exfilt. possible and governed through diffusion + coating factor



# Results

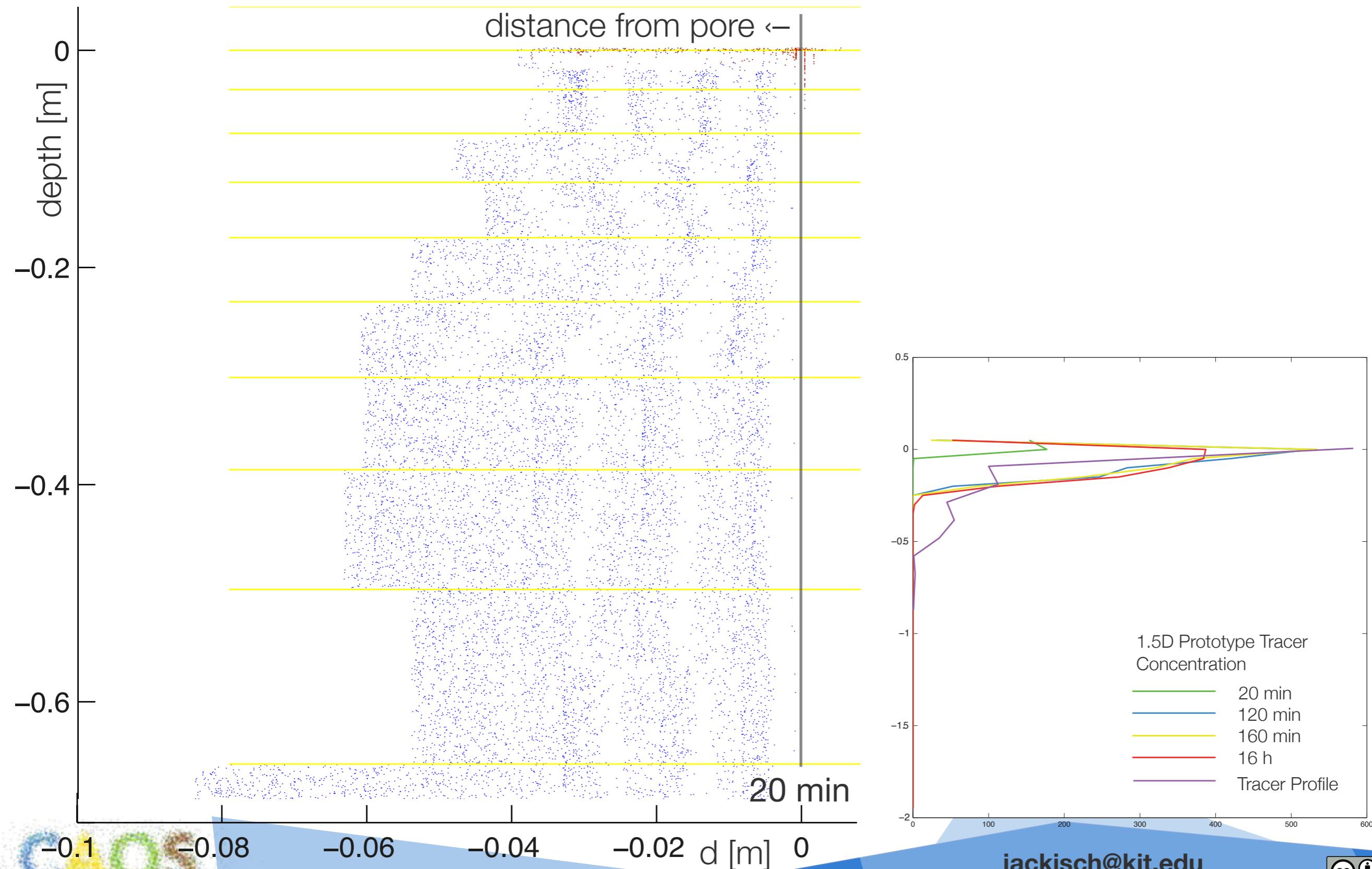


Advection stops at reasonable time.

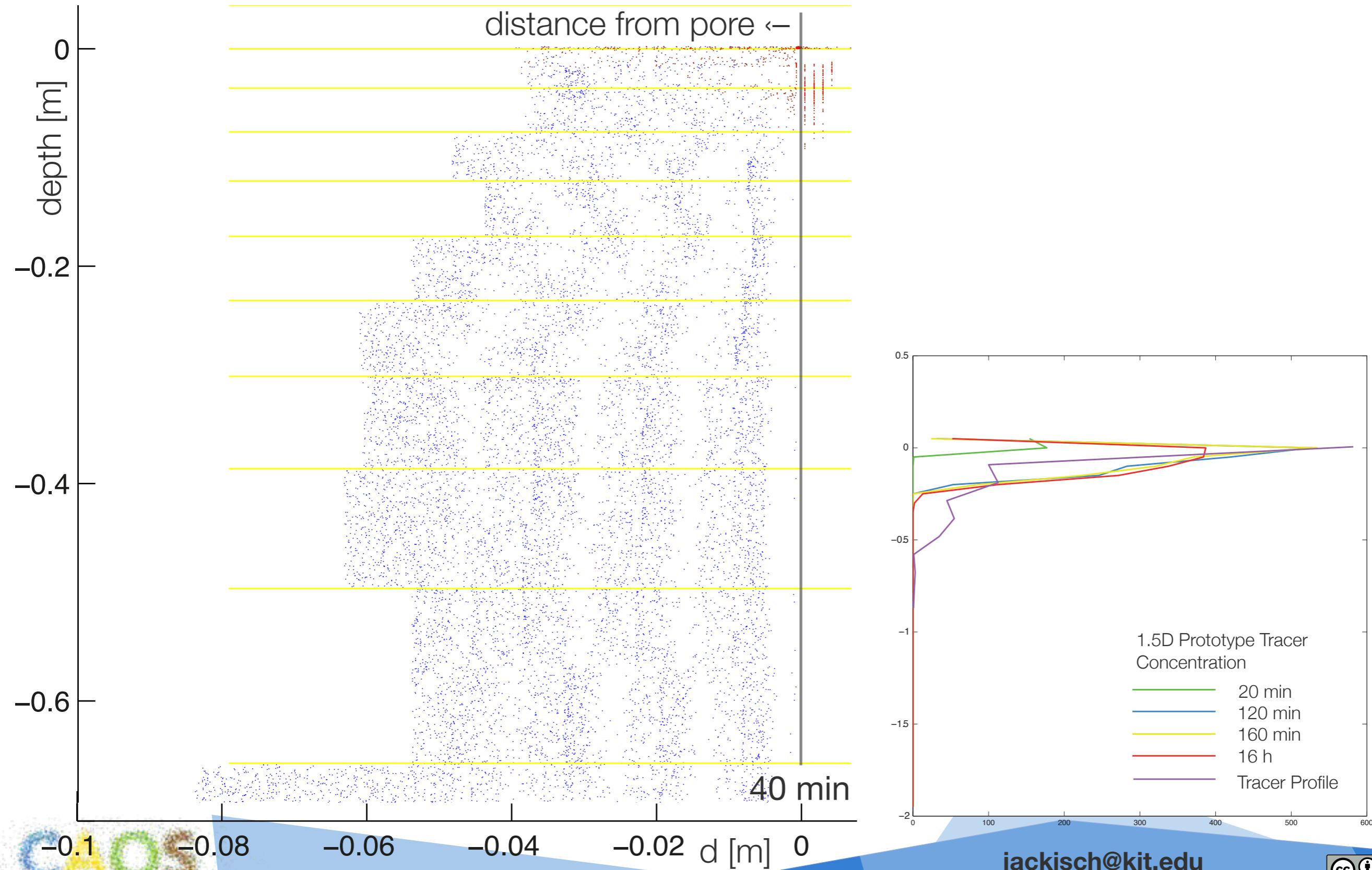
However, too low fast advection.

But far more properties.

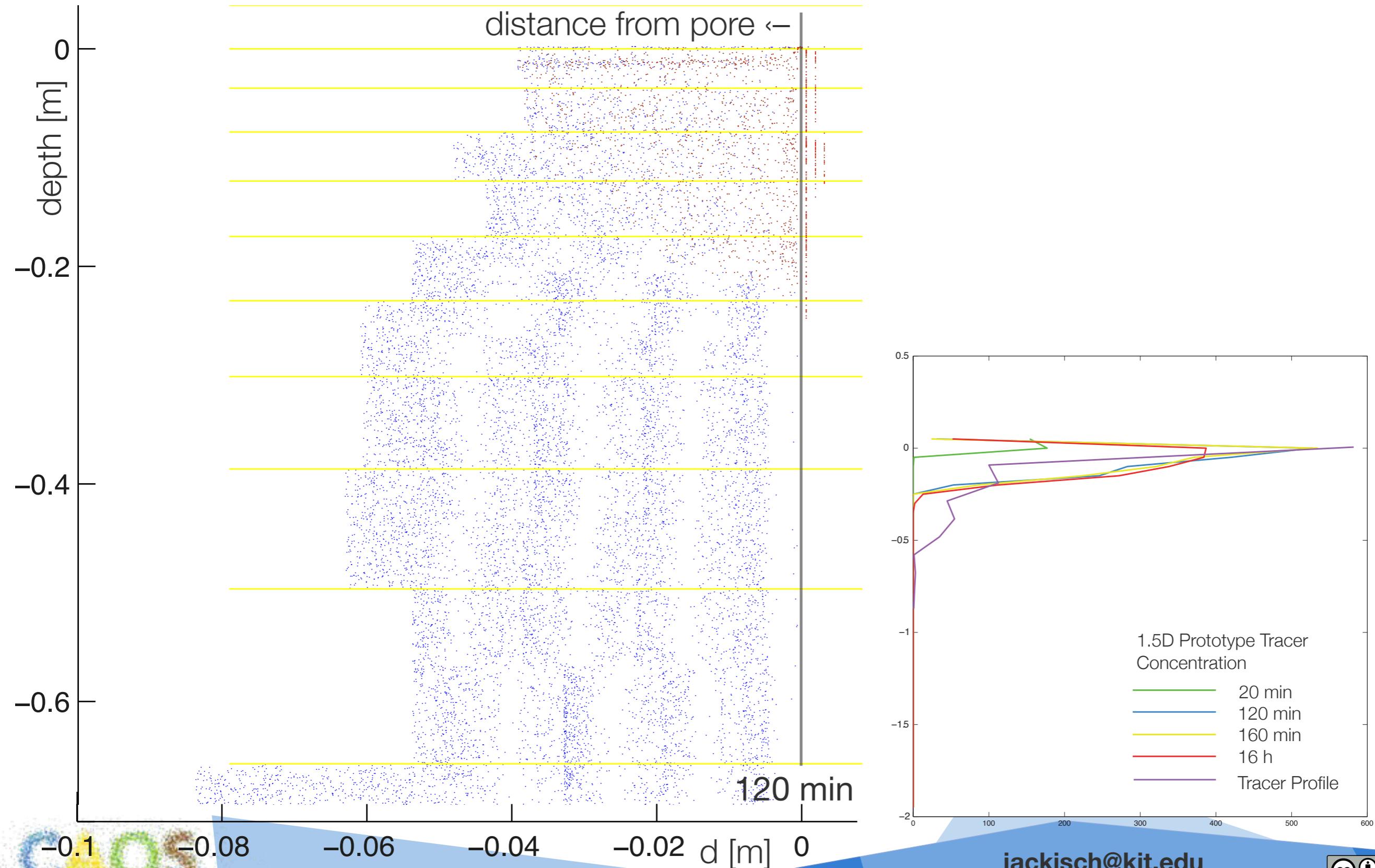
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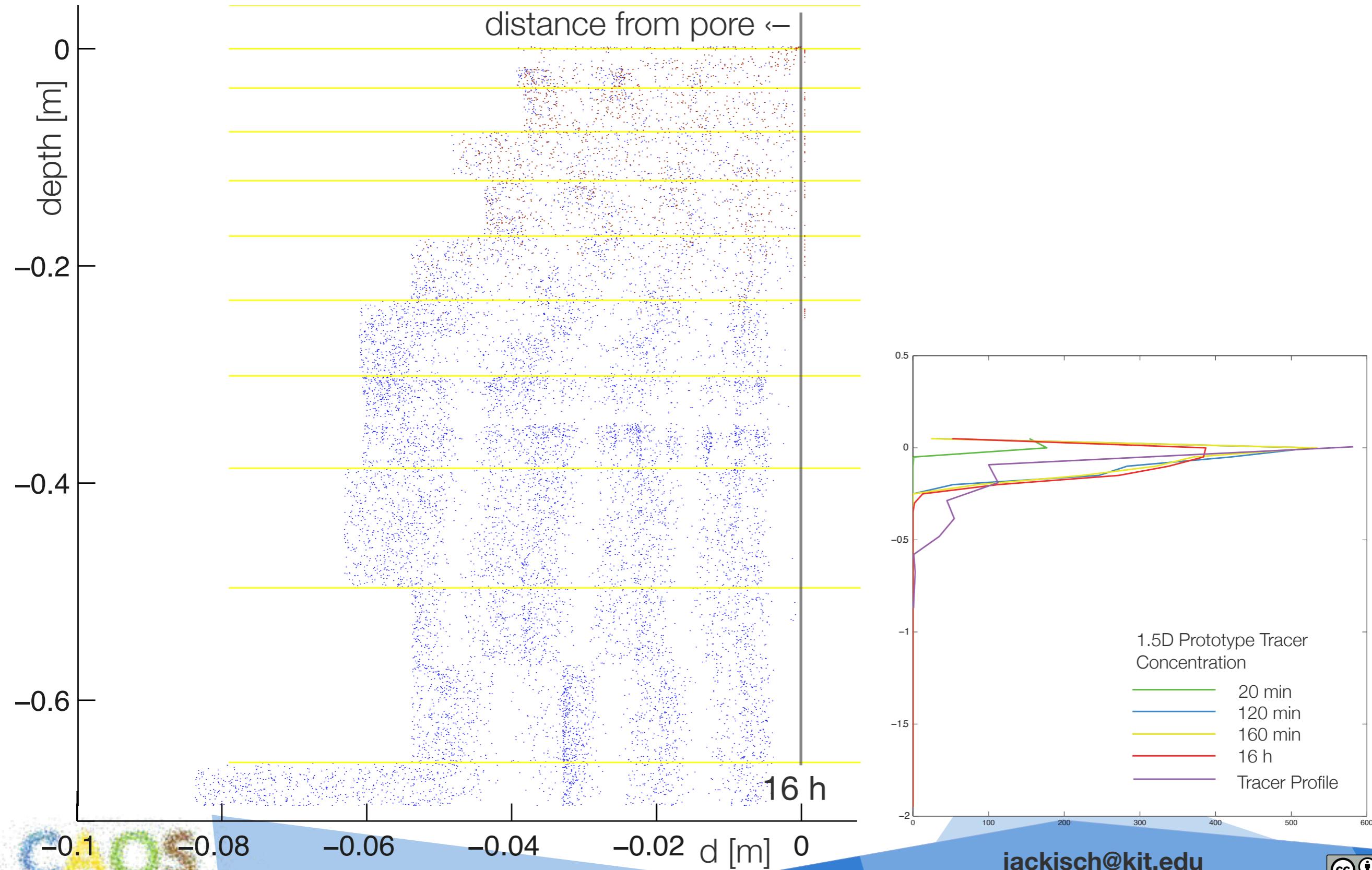
# Results



# Results



# Results



# Discussion

Not limited to earth worms/cracks! A pdf of the preferential flow domain and advective velocities suffices. → Scalable to lower Mesoscale

The domain is not static over time! Its parameters can be updated based on more experimental findings. → Link to ecology, seasonal activity...

Intrinsic definition of occurrence of advection through macropore matrix interaction.

BUT

Now, interfaces matter - coating, diffusion needs new definition, ...  
Original idea of capturing fingering problematic due to abstraction

# Conclusion

- Particle Model opens up exciting possibilities
- 1D is not enough
- the interfaces matter

„work in progress“

we are really interested  
in alternative definitions  
of soil water diffusion  
and your comments

Thanks to CAOS group.

Thank you.

