



## Evaluation of reduced power spectra from three-dimensional $k$ -space

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We present a new tool to evaluate one dimensional reduced power spectral densities (PSD) from arbitrary energy distributions in  $k$ -space. This enables us to calculate the power spectra as they are measured in spacecraft frame for any given measurement geometry assuming Taylor's frozen-in approximation. It is possible to separately calculate the diagonal elements of the spectral tensor and also to insert additional, non-turbulent energy in  $k$ -space (e.g. mirror mode waves). Given a critically balanced turbulent cascade with  $k_{\parallel} \sim k_{\perp}^{\alpha}$ , we explore the implications on the spectral form of the PSD and the functional dependence of the spectral index  $\kappa$  on the field-to-flow angle  $\theta$  between plasma flow and background magnetic field. We show that critically balanced turbulence develops a  $\theta$ -independent cascade with the spectral slope of the perpendicular cascade  $\kappa(\theta=90^{\circ})$ . This happens at frequencies  $f > f_{max}$ , where  $f_{max}(L, \alpha, \theta)$  is a function of outer scale  $L$ , critical balance exponent  $\alpha$  and field-to-flow angle  $\theta$ . The resulting spectra resemble the  $\theta$ -independent spectral form reported by Grappin & Müller (2010). We also discuss potential damping terms acting on the  $k$ -space distribution of energy and their effect on the PSD. Further, we show that the functional dependence  $\kappa(\theta)$  as found by Horbury *et al.* (2008) can be explained with a critically balanced turbulence model.