

# A model for water discharge based on energy consumption data (WATEN)

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## 1 Introduction

- In this study, we have developed a lumped model WATEN, aiming to calculate the flow rate discharged from the B-XII Irrigation District in Spain to the Guadalquivir River over the period 2002-2012.
- Intended as a first step to quantify the discharge of nitrates and salts from an irrigation district with scarce data availability to a receiving water body, and will serve as a baseline for similar worldwide studies and future alike applications.

## 2 Study area

- The 15000ha-B-XII Irrigation District is one of the largest irrigated areas in Spain.
- It is part of the Guadalquivir Marshland, located near the Atlantic coast of South-West Spain, close to the estuary of the Guadalquivir River (Fig. 1).
- A soil reclamation project was conducted in the second half of the XX century, installing subsurface drainage.



Figure 1

## 3 Methodology

### 3.1 Water balance and model equations

- Series of crop evapotranspiration ( $ET$ ), drainage ( $D$ ) and soil moisture deficit (SMD) or ( $S-S_{i-1}$ ), were determined based on precipitation ( $P$ ), irrigation ( $I$ ) and reference evapotranspiration ( $ET_o$ ).
- All the variables in Eq. (1) are positive, greater than or equal to 0.

#### Model equations

$$SMD = (SMD_{i-1} + ET - P \cdot R_p - I \cdot R_l) \cdot (0 < SMD_{i-1} + ET - P \cdot R_p - I \cdot R_l < TAM) + TAM \cdot (SMD_{i-1} + ET - P \cdot R_p - I \cdot R_l > TAM) \quad \text{Eq. (2)}$$

$$D = P \cdot (1 - R_p) + I \cdot (1 - R_l) + (P \cdot R_p + I \cdot R_l - SMD_{i-1} - ET) \cdot (P \cdot R_p + I \cdot R_l - SMD_{i-1} - ET > 0) \quad \text{Eq. (3)}$$

$$ET = (ET_c \cdot C_{ET}) \cdot \left( (SMD \leq RAM) + \frac{TAM - SMD}{TAM - RAM} \cdot (SMD > RAM) \right) \quad \text{Eq. (4)}$$

#### Model parameters

- TAM**: Total Available Moisture in the soil
- p**: mean fraction of  $TAM$  used up from the root zone before water stress occurs
- R<sub>p</sub>**: fixed percentage for effective precipitation
- R<sub>l1</sub>, R<sub>l2</sub>**: irrigation efficiency
- C<sub>ET</sub>**: coefficient of crop evapotranspiration  $ET'_c = ET_c \cdot C_{ET}$ ;  $ET_c = ET_o \cdot K_c$

## 3 Methodology

### 3.2 Model calibration

Energy consumption data ( $E_i$ ) was compared to energy consumption data derived from

$$\text{model results } (E_{Di}) \quad E_{Di} = D_i \cdot E_{ui} + \varepsilon_i \quad \text{where} \quad E_{ui} = \sum_{i=1}^n E_i / \sum_{i=1}^n D_i$$

### One-way and two-way sensitivity analysis

**Calibration process:** Monte Carlo Simulation (MCS) process and objective function optimization through algorithm GRG2.

### 3.3 Water balance discrimination per crops

- Irrigation ( $I$ ) proportionally distributed considering crop water needs and land use.
- Series of  $ET$ ,  $SMD$  and  $D$  resulted per individual crop. Model calibration was performed by MCS (6000 simulations), driven in a similar manner to genetic algorithms ( $PEDT$ ).

## 4 Results

### 4.1 Analysis of available data series and preliminary water balance

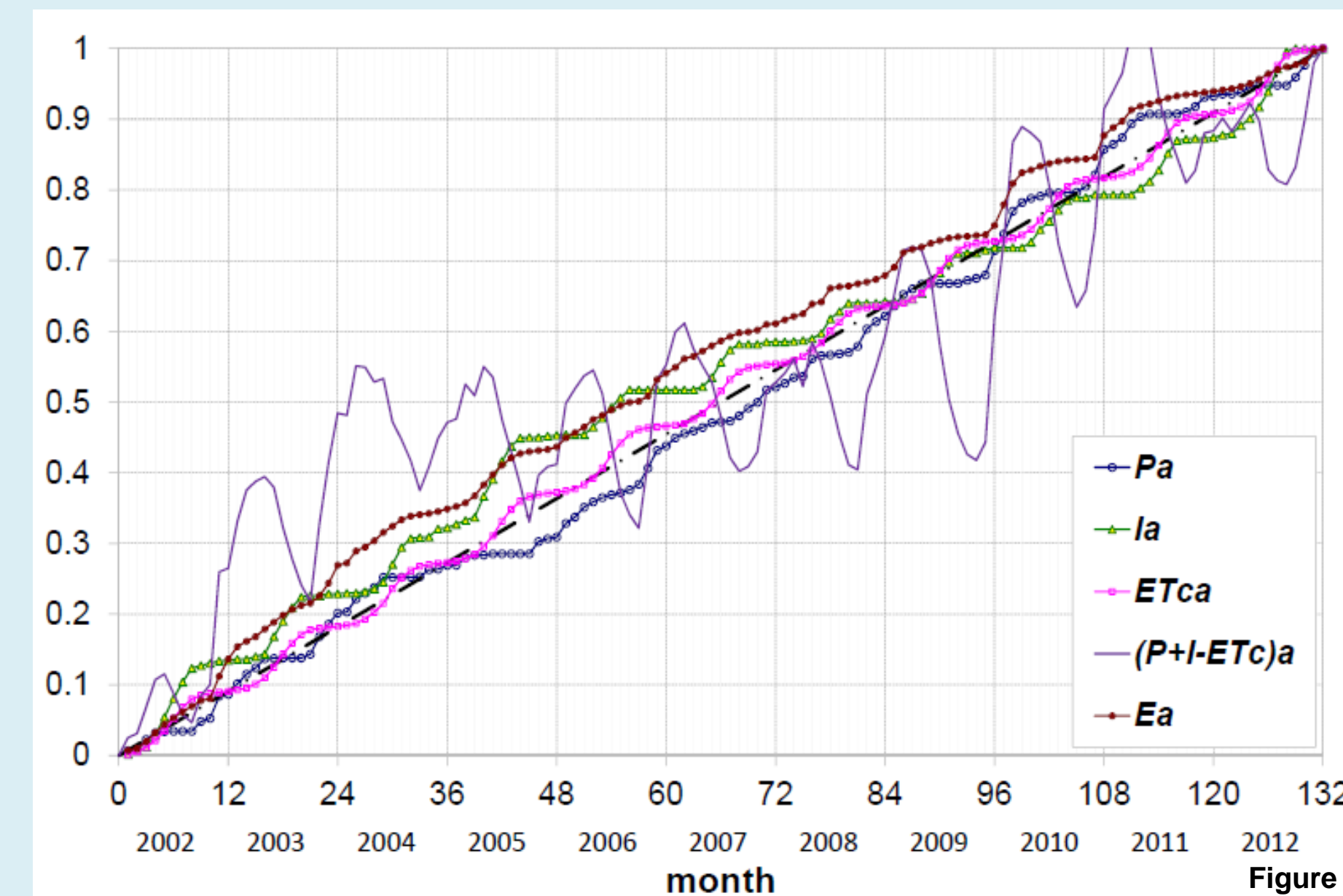


Figure 2

- A double-mass curve permitted to analyse data trends over the studied period (Fig. 2).
- Figure 2 shows accumulated series of the available components of the water balance: precipitation ( $P_a$ ), irrigation ( $I_a$ ), potential evapotranspiration ( $ET_{ca}$ ), and energy ( $E_a$ ).

### 4.2 Model results

- Potential crop evapotranspiration ( $ET_c$ ) and actual crop evapotranspiration ( $ET$ ) considering Reference 0<sup>1</sup> (Fig. 3)

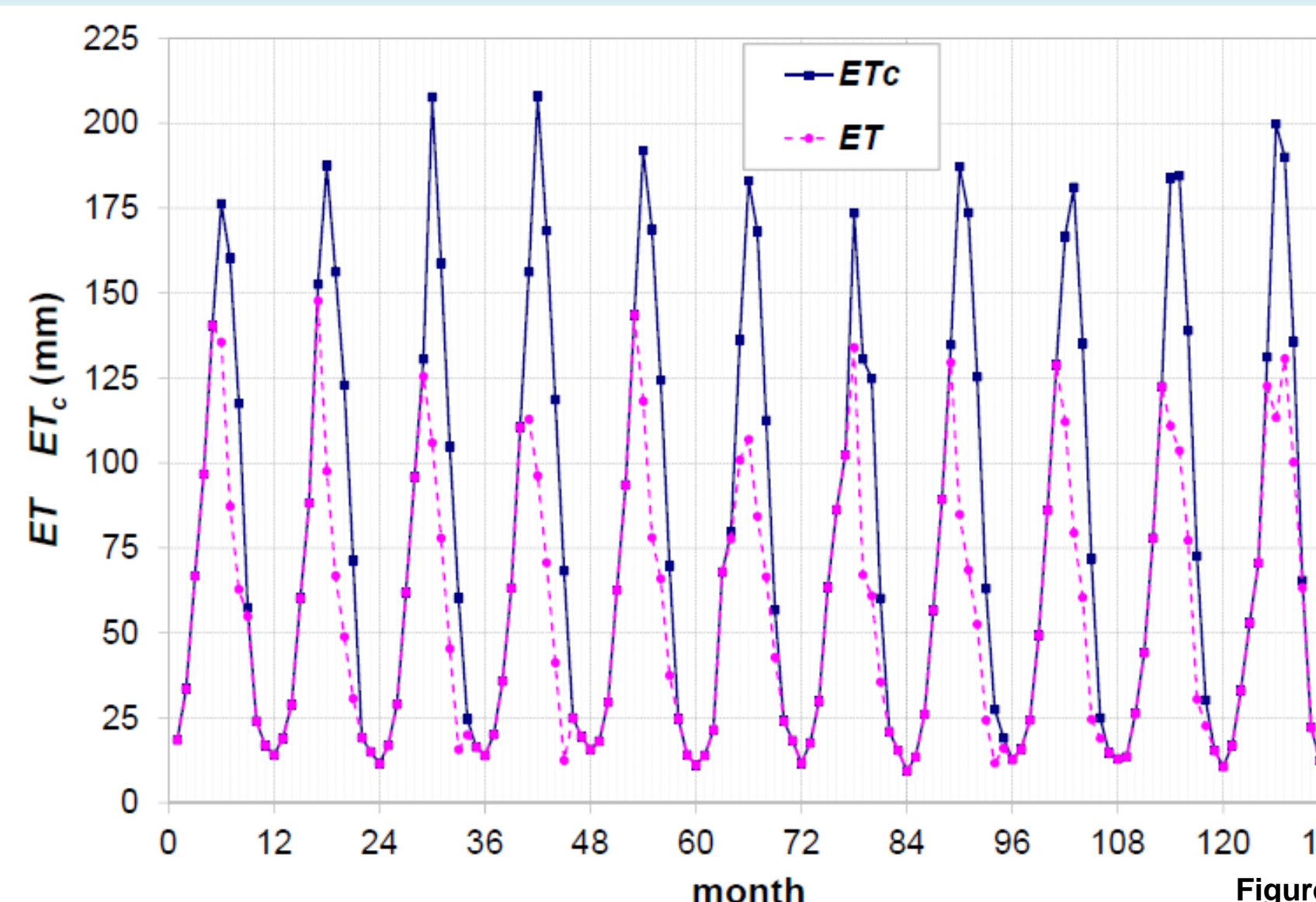


Figure 3

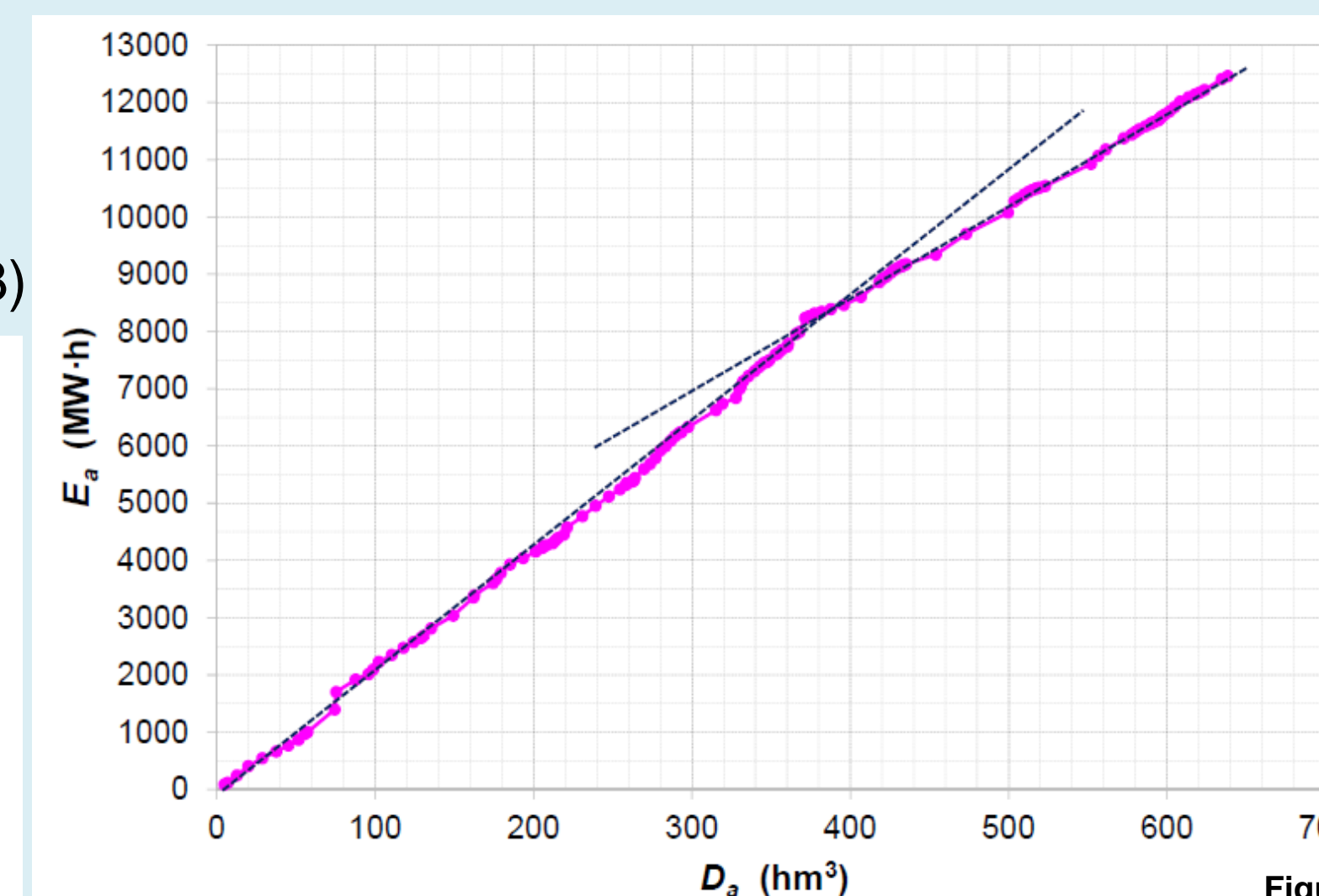


Figure 4

- Accumulated energy data ( $E_a$ ) versus accumulated drainage ( $D_a$ ) considering Reference 0<sup>1</sup>. Two differentiated trends (Fig. 4).

<sup>1</sup> Reference 0 (initially considered model parametric vector).

### 4.3 Model calibration

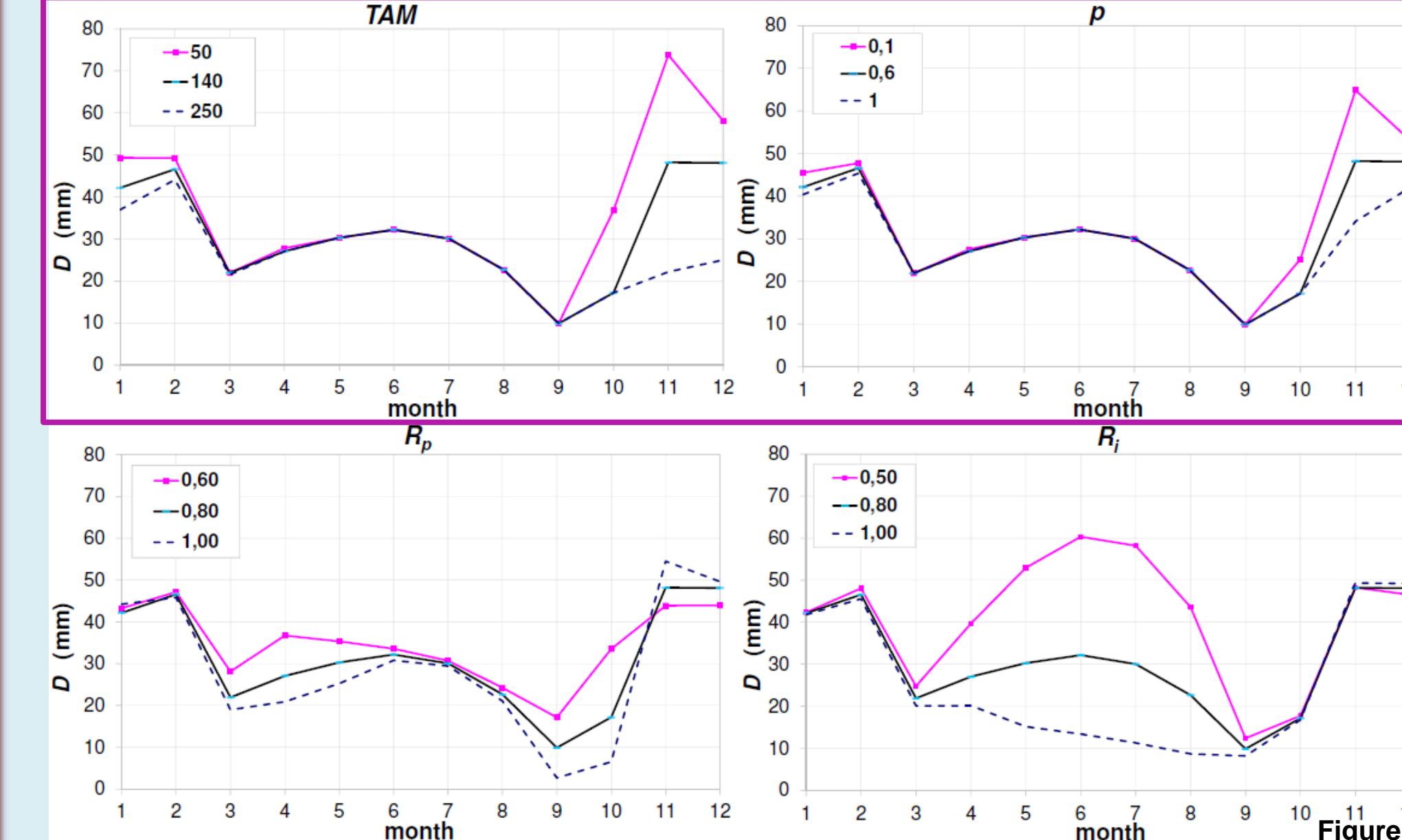


Figure 5

- One-way sensitivity analysis** (Fig. 5):  $TAM$  and  $p$  have an effect over winter model results,  $R_l$  has an effect on summer months;  $R_p$  showed interrelation with all the studied parameters.

## 4 Results

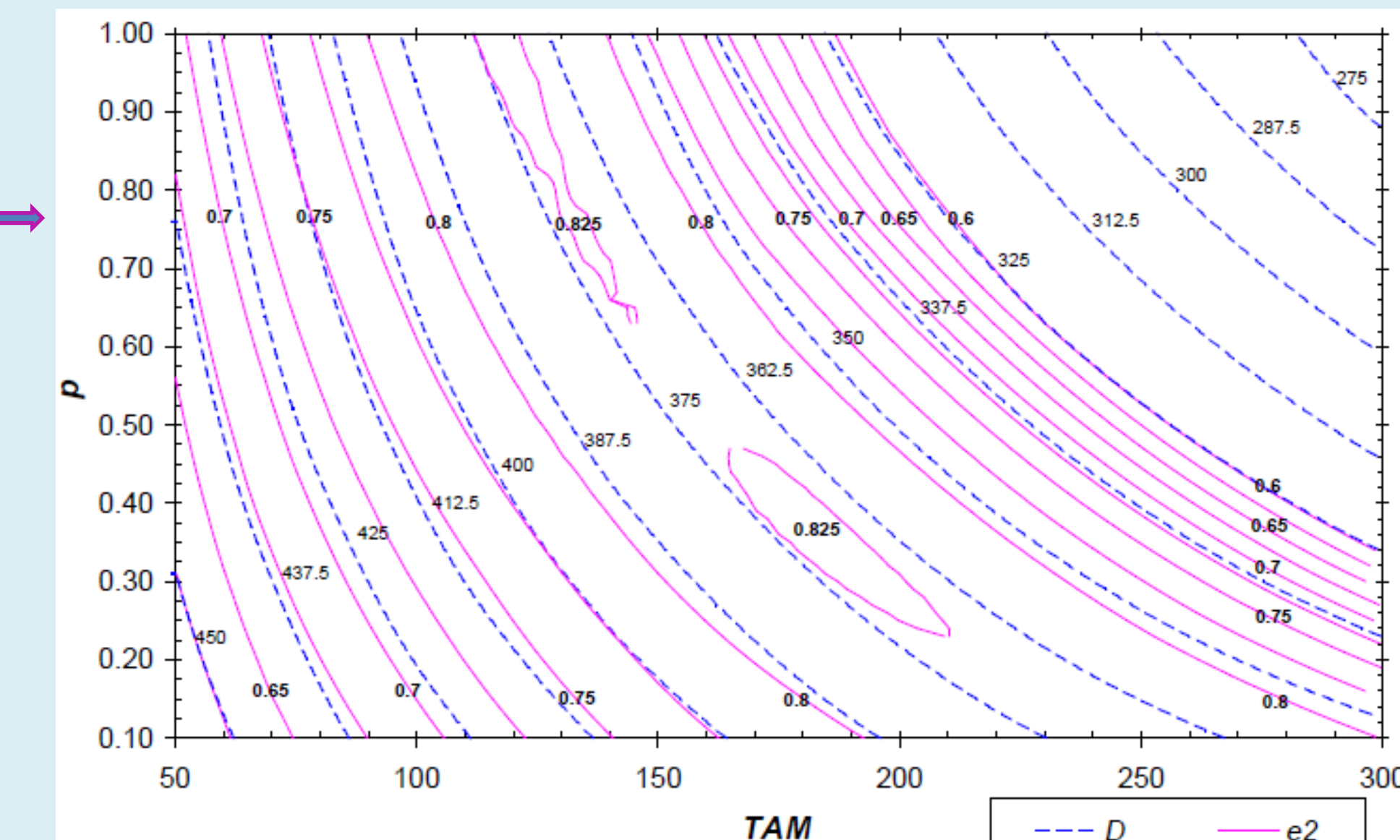


Figure 6

- Two-way sensitivity analysis:**  $TAM$ - $p$  correlation. Fig. 6 shows model results for the objective function coefficient of efficiency ( $e_2$ ) for different  $TAM$ - $p$  combinations.

### 4.4 Model results discriminating per crops



Figure 7

- Finally, a water balance for each individual crop based on Eq. (2), (3) and (4) was performed (Fig. 7).
- The new solution resulted on better model performance. The average coefficient of efficiency  $e_2$  improved from 0.87 to 0.90.
- Calibration through MCS process was driven in the direction of better model performance.

## 5 Conclusions

- The proposed lumped model WATEN attained an average Nash-Sutcliffe coefficient  $e_2 \cong 0.90$  between observed and estimated drainage discharge. Energy consumption for drainage discharge was used for model calibration.
- A significant crop evapotranspiration reduction was detected over the studied period. Average water discharge was close to 3740 m<sup>3</sup>/ha/year, probably sufficient for leaching irrigation water salts.
- Defined as a nitrate vulnerable zone, flow rate discharge and drainage chemical monitoring would allow improving water balance and energy savings, and to assess the long-term effect on the Guadalquivir River.
- This study is intended as a basis for analogous scarce-data coastal irrigation districts with drainage discharge to receiving water bodies, as is the case of many irrigated areas of Egypt, Pakistan or India amongst others.

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