



## Inter-relationship between scaling exponents for describing self-similar river networks

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Natural river networks show well-known self-similar characteristics. Such characteristics are represented by various power-law relationships, e.g., between upstream length and drainage area (exponent  $h$ ) (Hack, 1957), and in the exceedance probability distribution of upstream area (exponent  $\varepsilon$ ) (Rodríguez-Iturbe *et al.*, 1992). It is empirically revealed that these power-law exponents are within narrow ranges. Power-law is also found in the relationship between drainage density (the total stream length divided by the total basin area) and specified source area (the minimum drainage area to form a stream head) (exponent  $\eta$ ) (Moussa and Bocquillon, 1996).

Considering that above three scaling relationships all refer to fundamental measures of 'length' and 'area' of a given drainage basin, it is natural to hypothesize plausible inter-relationship between these three scaling exponents. Indeed, Rigon *et al.* (1996) demonstrated the relationship between  $\varepsilon$  and  $h$ . In this study, we expand this to a more general  $\varepsilon$ - $\eta$ - $h$  relationship. We approach  $\varepsilon$ - $\eta$  relationship in an analytical manner while  $\eta$ - $h$  relationship is demonstrated for six study basins in Korea. Detailed analysis and implications will be presented.

### References

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