## 1. Introduction

The European Centre for Medium-Range Weather Forecasts (ECMWF) issues global forecasts consisting of a 50 member ensemble, a high-resolution, and a control run. Such ensemble forecast systems tend to be biased and underdispersive for surface weather variables (Bougeault et al., 2010; Park et al. 2010). Bias and underdispersion can be reduced by different statistical post-processing methods, of which ensemble model output statistics (EMOS, Gneiting et al. 2005) is applied here. EMOS converts an ensemble of $K$ discrete forecasts $\boldsymbol{f}=\left(f_{1}, f_{2}, \ldots, f_{K}\right)^{T}$ into a predictive density:

$$
\begin{equation*}
y \mid \boldsymbol{f} \sim g(m, \sigma), \tag{1}
\end{equation*}
$$

where $g(\cdot)$ is a parametric density function with location and scale parameters $m$ and $\sigma$, respectively, which depend on the raw ensemble. Typically, post-processing increases forecast skill. Skill of probabilistic forecasts is often measured by the negatively oriented continuous ranked probability score (CRPS, Hersbach 2000):

$$
\begin{equation*}
\operatorname{CRPS}(F, y)=\int_{-\infty}^{\infty}\left[F(x)-\mathbb{1}_{[x \geq y]}\right]^{2} d x, \tag{2}
\end{equation*}
$$

where $F$ is the predictive CDF and $y$ is the verifying observation. Figure 1 shows CRPS values of the raw ensemble and the EMOS forecasts for the variables 2 m temperature (T2M), 24 h precipitation (PPT24), and near surface wind speed (V10)


## 2. Research question and methods

The ECMWF forecast ensemble is under continuous development (Buizza et al., 1998, 2007; Richardson et al., 2013; Haiden et al., 2014). Hence, its forecast skill improves over time due to the following causes

1. bias reductions and increased reliability $\rightarrow$ competes with statistical post-processing 2. an increase in potential skill $\rightarrow$ complementary to statistical post-processing

In order to determine which of the above causes is more important, the evolution of the CRPS difference $\triangle \mathrm{CRPS}_{t}=\mathrm{CRPS}_{\text {raw }, t}-\mathrm{CRPS}_{\text {EMOS }, t}$ is evaluated over time (Hemri et al, 2014). The following two approaches are used:

- Fit a parametric regression model to $\Delta \mathrm{CRPS}_{t}$ and evaluate the estimates $\hat{\beta}_{1}$ :

$$
\begin{equation*}
\Delta \mathrm{CRPS}_{t}=\beta_{0}+\beta_{1} t+\beta_{2} \sin \left(\frac{2 \pi t}{12}\right)+\beta_{3} \cos \left(\frac{2 \pi t}{12}\right)+\epsilon, \quad \epsilon \sim \mathcal{N}\left(0, \sigma^{2}\right) \tag{3}
\end{equation*}
$$

- Correct for seasonal effects by fitting the following model to $\Delta$ CRPS $_{t}$

$$
\begin{equation*}
\Delta \mathrm{CRPS}_{t}=\gamma_{0}+\gamma_{1} \sin \left(\frac{2 \pi t}{12}\right)+\gamma_{2} \cos \left(\frac{2 \pi t}{12}\right)+\epsilon, \quad \epsilon \sim \mathcal{N}\left(0, \sigma^{2}\right), \tag{4}
\end{equation*}
$$

and then use the non-parametric Kendall's $\tau$ rank correlation test to check for a significant trend in the residuals of model (4)

These models are fitted for each variable, station, and lead time seperately. Two examples for ECMWF forecasts with a lead time of 6 days are shown in figure 2 .


## 3. Results

There is no clear trend in $\triangle$ CRPS. Table 1 shows the percentages of SYNOP stations (totals are 4160 (T2M), 2917 (PPT24), and 4387 (V10)) showing no, negative, or positive trend in monthly $\triangle$ CRPS values against time at a significance level of 0.05 . Stations with no significant trend outnumber the stations with either negative or positive trend.

Tab.1: Percentages of stations with significant trend in $\triangle$ CRPS.

|  | parametric model |  |  | Kendall's $\tau$ statistic |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | T2M | PPT24 | V10 | T2M | PPT | V10 |
| no significant trend | 42 \% | $76 \%$ |  |  | 77 | 42 |
| $\pm \mathrm{m}$ negative trend | 34 \% | 19 \% | 31 \% | 32 | $18 \%$ | 29 \% |
| positive trend | 24 \% | 5 \% | 28 \% | 24 \% | 5 \% |  |
| no significant tren | 46 \% | 82\% | 43 \% |  | 82 \% | 兂 |
| negative trend | 31 \% | 14 \% | 31 \% | 29 \% | $13 \%$ | 29 |
| positive trend | 23 \% | $4 \%$ | 26 \% | 23 \% | $5 \%$ | 27 \% |
| no significant trend | 54 \% | 83\% | 45 \% |  | 82\% | 46 |
| $\bigcirc$ negative trend | 27 \% | 11 \% |  |  | $11 \%$ |  |
| positive trend | 19 | 6 \% |  |  |  |  |

A station-wise assessment of significant trend in $\triangle \mathrm{CRPS}$ is shown in figure 3:


Fig.3: Significants trend in $\triangle$ CRPS according to the Kendall's $\tau$ correlation coefficient test.

## 4. Conclusions

- Skill of both the raw ensemble and the EMOS forecasts improves over time
- The gap in $\triangle$ CRPS remains almost constant over time
- Improvements to the atmospheric model are increasing potential skill
- Statistical post-processing will keep adding skill in the foreseeable future.


## 5. References

[1] P. Bougeault et al., Bull. Am. Meteorol. Soc., 91 : 1059-1072, 2010. [2] R. Buizza et al., Q. J. R. Meteorol. Soc., 124: 1935-1960, 1998 [3] R. Buizza et al., Q. J. R. Meteorol. Soc., 133: 681-695, 2007. [4] T. Gneiting et al., Mon. Weather Rev., 133: 1098-1118, 2005 [5] T. Haiden et al., ECMWF Tech. Memo. 723, 34 pp., 2014 [6] S. Hemri et al., Geophys. Res. Lett., 41: 9197-9205, 2014 [7] H. Hersbach., Weather Forecasting, 15: 559-570, 2000. [8] Y. Park et al., Q. J. R. Meteorol. Soc., 134: 2029-2050, 2008.

