



## Variational approach to direct and inverse problems of atmospheric pollution studies

Vladimir Penenko (1,2), Elena Tsvetova (1), Alexey Penenko (1,2)

(1) Institute of Computational Mathematics and Mathematical Geophysics SB RAS, Novosibirsk, Russian Federation, (2) Novosibirsk State University, Novosibirsk, Russian Federation

We present the development of a variational approach for solving interrelated problems of atmospheric hydrodynamics and chemistry concerning air pollution transport and transformations. The proposed approach allows us to carry out complex studies of different-scale physical and chemical processes using the methods of direct and inverse modeling [1-3]. We formulate the problems of risk/vulnerability and uncertainty assessment, sensitivity studies, variational data assimilation procedures [4], etc.

A computational technology of constructing consistent mathematical models and methods of their numerical implementation is based on the variational principle in the weak constraint formulation specifically designed to account for uncertainties in models and observations. Algorithms for direct and inverse modeling are designed with the use of global and local adjoint problems. Implementing the idea of adjoint integrating factors provides unconditionally monotone and stable discrete-analytic approximations for convection-diffusion-reaction problems [5,6].

The general framework is applied to the direct and inverse problems for the models of transport and transformation of pollutants in Siberian and Arctic regions.

The work has been partially supported by the RFBR grant 14-01-00125 and RAS Presidium Program I.33P.

### References:

1. V. Penenko, A. Baklanov, E. Tsvetova and A. Mahura . Direct and inverse problems in a variational concept of environmental modeling //Pure and Applied Geoph.(2012) v.169: 447-465.
2. V. V. Penenko, E. A. Tsvetova, and A. V. Penenko Development of variational approach for direct and inverse problems of atmospheric hydrodynamics and chemistry, *Izvestiya, Atmospheric and Oceanic Physics*, 2015, Vol. 51, No. 3, p. 311–319, DOI: 10.1134/S0001433815030093.
3. V.V. Penenko, E.A. Tsvetova, A.V. Penenko. Methods based on the joint use of models and observational data in the framework of variational approach to forecasting weather and atmospheric composition quality// *Russian meteorology and hydrology*, V. 40, Issue: 6, Pages: 365-373, DOI: 10.3103/S1068373915060023.
4. A.V. Penenko and V.V. Penenko. Direct data assimilation method for convection-diffusion models based on splitting scheme. *Computational technologies*, 19(4):69–83, 2014.
5. V.V. Penenko, E.A. Tsvetova, A.V. Penenko Variational approach and Euler's integrating factors for environmental studies// *Computers and Mathematics with Applications*, 2014, V.67, Issue 12, Pages 2240–2256, DOI:10.1016/j.camwa.2014.04.004
6. V.V. Penenko, E.A. Tsvetova. Variational methods of constructing monotone approximations for atmospheric chemistry models // *Numerical analysis and applications*, 2013, V. 6, Issue 3, pp 210-220, DOI 10.1134/S199542391303004X