



Nonnormality increases variance of gravity waves trapped in a tilted box

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We study the prototype problem of internal gravity waves in a square domain tilted with respect to the gravity vector by an angle θ . Only when θ is zero regular normal modes exist, for all other angles wave attractors and singularities dominate the flow. We show that the linear operator of the governing PDE becomes non-normal for nonzero θ giving rise to non-modal transient growth. This growth depends on the underlying norm: for the variance norm significant growth rates can be found whereas for the energy norm, no growth is possible since there is no source for energy (in contrast to shear flows, for which the mean flow feeds the perturbations). We continue by showing that the nonnormality of the system matrix is increasing with θ and reaches a maximum when θ is 45 degree. Moreover, the growth rate is increasing as can be expected from the increasing nonnormality of the matrix. Our results imply that at least the most simple wave attractors can be seen as those initial flow fields that gain most of the variance during a given time period.