

Granular flows in inclined channels

Deepak Tunuguntla, Irana Denissen, Thomas Weinhart, and Anthony Thornton

Department of Thermal and Fluid Engineering, University of Twente, The Netherlands (d.r.tunuguntla@utwente.nl)

Study of granular flows down inclined channels is essential in understanding the dynamics of natural grain flows like landslides and snow avalanches (e.g. Delannay et al., 2017). As a stepping stone, we consider a monodisperse dry granular material owing down a rough inclined channel with downslope contracting sidewalls: theoretically and numerically. Utilising the depth-averaged shallow granular theory (Savage & Hutter, 1989) together with an empirical (Pouliquen, 1999; Pouliquen & Forterre, 2002), but discrete particle simulations validated constitutive friction law (Weinhart et al., 2012; Thornton et al., 2012), an extended novel one-dimensional (depth- and width-averaged) granular hydraulic theory will be presented. Different flow states are predicted by this novel one-dimensional theory. Flow regimes with distinct flow states are determined as a function of upstream channel Froude number, F , and channel width ratio at the exit, B_c . The latter being the ratio of the channel's exit width and upstream channel width. For steady flows, besides describing the subcritical flow state ($F < 1$), the one-dimensional model also predicts two other steady states for a range of upstream prescribed supercritical flow conditions ($F > 1$) and channel openings (B_c). The two other states are flows with weak oblique shocks (smooth when width-averaged) and flows with a steady jump in the contraction region. Both, super- and subcritical flow states are verified by numerically solving the closed depth-averaged two-dimensional shallow granular model using an open-source continuum solver hpGEM (Pesch et al., 2007). Despite the strong inhomogeneities in the linear contraction region, we will show that the one- and two-dimensional solutions (averaged across the channel) incomparably match well.

References

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