



## **Two phenomenological constants explain similarity laws in stably stratified turbulence**

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In stably stratified turbulent flows, the mixing efficiency associated with eddy diffusivity for heat, or equivalently the turbulent Prandtl number ( $Pr_t$ ), is fraught with complex dynamics originating from the scale-wise interplay between shear generation of turbulence and its dissipation by density gradients. A large corpus of data and numerical simulations agree on a near-universal relation between  $Pr_t$  and the Richardson number ( $R_i$ ), which encodes the relative importance of buoyancy dissipation to mechanical production of turbulent kinetic energy. The  $Pr_t - R_i$  relation is shown to be derivable solely from the co-spectral budgets for momentum and heat fluxes if a scale-wise Rotta-like return to isotropy closure for the pressure-strain effects and Kolmogorov's theory for turbulent cascade are invoked. The ratio of the Kolmogorov to the Kolmogorov-Obukhov-Corrsin phenomenological constants, and a constant associated with isotropization of the production whose value has been predicted from Rapid Distortion Theory ( $= 3/5$ ), explain all the macroscopic non-linearities. Comparisons with a conventional Mellor-Yamada (MY) model for stably stratified atmospheric flows as well as the Energy- and Flux-Budget (EFB) approach is featured with a lens on the cut-off Richardson number dilemma.