

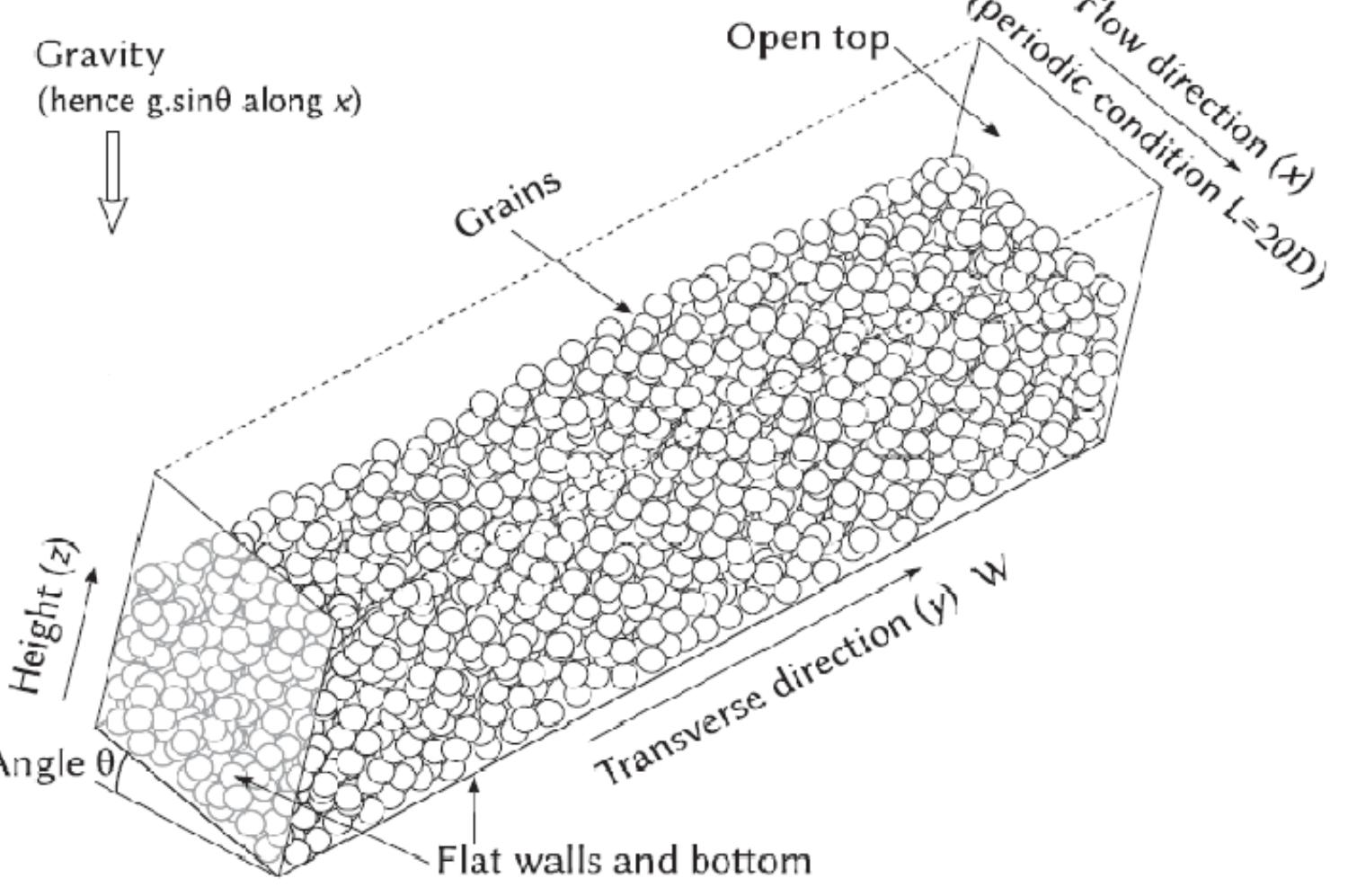
# Numerical simulations

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## Numerical Method

Discrete Element Method[1].

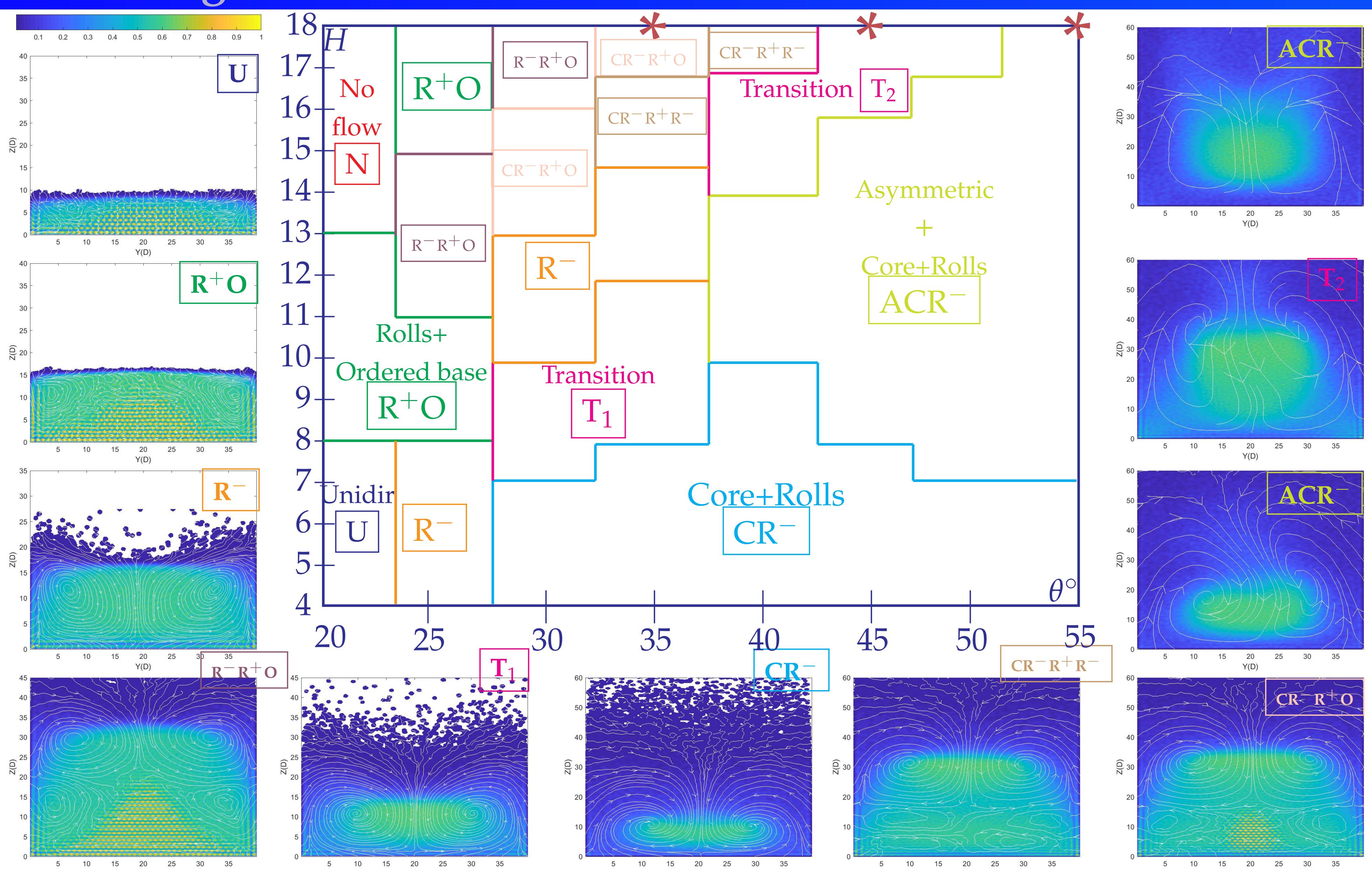


The control parameters.

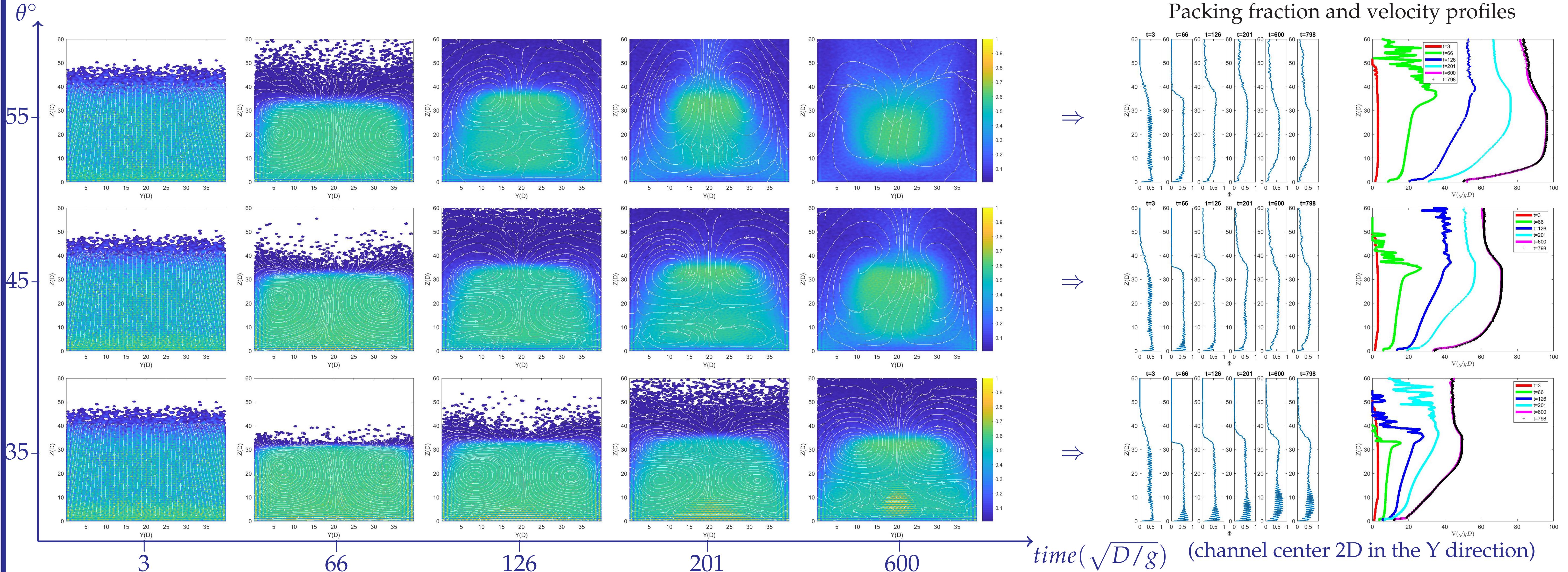
$W(D)$	$H(D)$	$\theta(^{\circ})$
40	4 – 18	20 – 55

D: diameter of the grain. H: mass hold up.

## Phase diagram

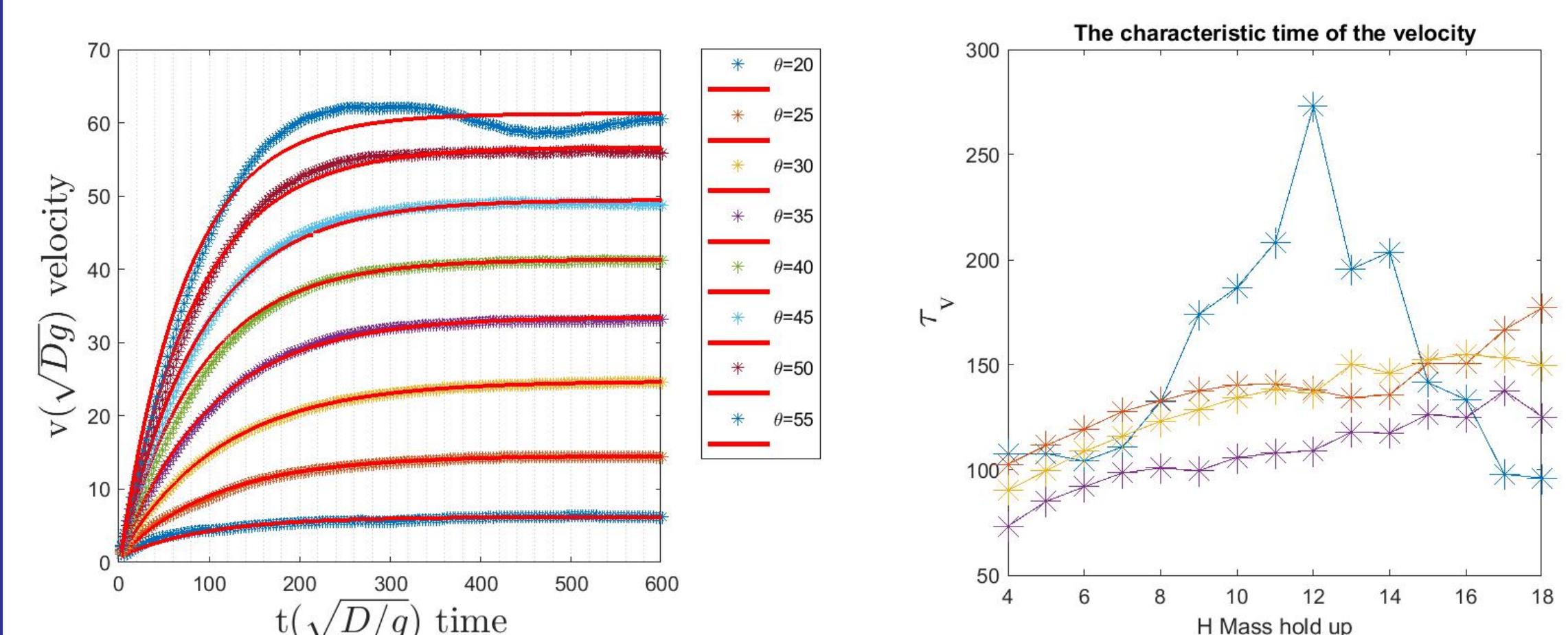


## The temporal evolution of the flow $H=18^*$

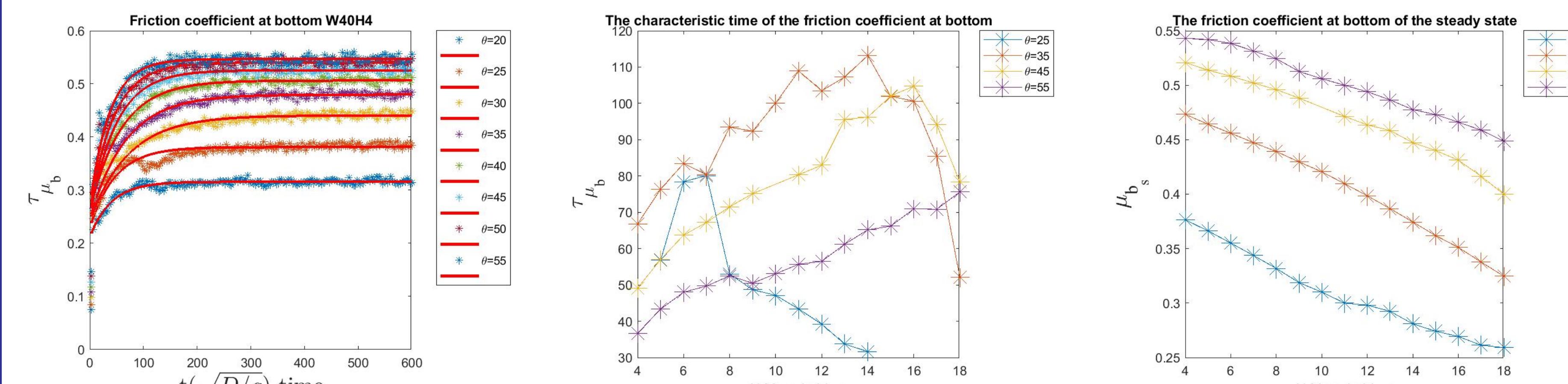


## Towards the steady state

$$1. \text{ Velocity: } v(t) = (v - v_{t_0})(1 - e^{-\frac{t-t_0}{\tau}}) + v_{t_0} \quad (H=4)$$



$$2. \text{ Friction coefficient: } \mu(t) = (\mu - \mu_{t_0})(1 - e^{-\frac{t-t_0}{\tau}}) + \mu_{t_0} \quad (H=4)$$



## Conclusion

- Enriched phase diagram for  $W = 40D$  in comparison with that obtained for  $W = 68D$ [2].
- Most of steady states exhibit pair of rolls which can rotate with different rotation directions.
- These rolls coexist with a dense supported core or a dynamic ordered dense base.
- The flow reaches its stationary state through a rich transient dynamics where rolls can appear and disappear in favor of other rolls with a reverse rotation direction.

## References

- Nicolas Brodu, Patrick Richard, and Renaud Delannay. Shallow granular flows down flat frictional channels: Steady flows and longitudinal vortices. *Phys. Rev. E*, 87:022202, Feb 2013.
- Nicolas Brodu, Renaud Delannay, Alexandre Valance, and Patrick Richard. New patterns in high-speed granular flows. *Journal of Fluid Mechanics*, pages 1–11, April 2015.