



## Mechanics of Pendulum-type waves

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Pendulum-type waves are the waves propagating in blocky/fragmented rock or rock mass. They are characterised by low velocities and by the presence of multiple peaks in the spectrum. The pendulum-type waves were suggested by Kurlenya, et al. (1996a). Assuming hierarchical structure of rock mass the peak frequencies they suggested to be multiples of square root of 2 (so-called canonical frequencies). Pendulum-type waves were detected in laboratory experiments (e.g., Kurlenya, et al., 1996b; Alexandrova, 2003.) and in the walls of mining excavations (Kurlenya, et al., 1996c). Models of the Pendulum-type waves are usually based on dynamics of discrete systems with independent displacements of rigid blocks (e.g., Alexandrova & Sher, 2003).

In this presentation we analyse the effect of independent block rotation. To this end we consider a finite (1D) chain of identical rigid blocks each having two degrees of freedom capable of independent oscillations in the longitudinal axis and rotational oscillations in a common plane passing through that axis. Each pair of blocks is connected by two springs that model interblock connection providing resistance to both relative displacement and rotation.

The model shows that such a system supports two types of waves, longitudinal and rotational and these waves are independent. The wave velocities are controlled by spring stiffnesses, block dimensions and density and can be quite low. Furthermore the chain consisting of  $n$  blocks with the first block fixed possesses  $2(n-1)$  degrees of freedom and hence  $2(n-1)$  modes (resonant frequencies) leading to the appearance of multiple peaks in the spectrum. It is the large number of peaks that makes the frequencies being close to some multiples of square root of 2.

The proposed model can provide the means of identification of the properties of blocky/fragmented rock based on the observed velocity of the waves and their spectrum.

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