



## **Bayesian inference of grain growth prediction via multi-phase-field models**

Hiromichi Nagao (1,2), Shin-ichi Ito (1,2), Takashi Kurokawa (2), Tadashi Kasuya (3), Junya Inoue (3,4)

(1) Earthquake Research Institute, The University of Tokyo, Tokyo, Japan, (2) Graduate School of Information Science and Technology, The University of Tokyo, Tokyo, Japan, (3) Graduate School of Engineering, The University of Tokyo, Tokyo, Japan, (4) Research Center for Advanced Science and Technology, The University of Tokyo, Tokyo, Japan

We propose a Bayesian inference methodology to evaluate unobservable parameters involved in multi-phase-field models with the aim of accurately predicting the observed grain growth, such as in rocks, metals and alloys. This approach integrates models and a set of observational image data of grain structures. Since the set of image data is not a time series, directly applying conventional inference techniques that require time series as the input data is difficult. The key idea in our methodology to overcome this difficulty is to construct a time series with an appropriate statistic that characterizes static image data of grain structures. Our methodology implements the empirical Bayes method. It can estimate not only a probability density function of the parameters but also an initial phase-field, which is generally unobservable in real experiments. After validating the proposed method through numerical tests using synthetic data, we apply it to real experimental images of grain structures in a steel alloy. The proposed method properly estimates unobservable parameters together with their uncertainties, and successfully selects the initial phase-field that best explains the experimental data from among candidate initial phase-fields.