



Bi-spectral Analysis of the El-Niño index and its stochastic modeling

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ENSO is highly nonlinear and non-Gaussian. Some of its features, however, may be approximated by a linear or quasi-linear process. We assess the different features of ENSO by analyzing the bispectra of El-Niño index observed over a period of 102 years. 2D-Fourier bispectra $B(f_1, f_2)$, are computed using the bicorrelation (or lagged skewness) $sk(t_1, t_2) = E[x'(t)x'(t+t_1)x'(t+t_2)]$. The largest and statistically significant contributions to $B(f_1, f_2)$ occur for frequency pairs (f_1, f_2) , corresponding to: (5.3yr, 34yr), (5.3yr, 3.6yr) and (4.9yr, 4.9yr), all of them peaking in the power spectrum. The integrated bispectrum, i.e. the 2D-integral of $B(f_1, f_2)$ yields the El-Niño positive skewness $sk(0,0) = 0.23$. A test of nonlinearity is assessed through the Hinich test: $Hi(f_1, f_2) = |B(f_1, f_2)|^2 / [S(f_1)S(f_2)S(f_1+f_2)]$. Under the null hypothesis of linearity, $Hi(f_1, f_2)$ is constant and proportional to the square of $sk(0,0)$ and the bi-spectrum depends only on $S(f)$. The test is performed to check the nature of the 2D spectral 'islands' for linearity. Low-order autoregressive processes, forced by non-Gaussian additive and/or multiplicative noise are fitted to the data, and we look for triadic frequency resonances (f_1, f_2, f_1+f_2) . This would improve stochastic modelling of El-Niño. Application to other SST indices are also performed with particular focus on possible nonlinear correlations and teleconnections are also discussed. Publication supported by FCT- project UID/GEO/50019/2019 - Instituto Dom Luiz.