

EGU 2020

Structure function analysis of plasma density fluctuations during total loss of lock of GPS signal events



UNIVERSITY OF
CALGARY

Hossein Ghadjari

David Knudsen

Susan Skone



Background Information

- Ionospheric Irregularities have scale sizes from a hundred meters to hundreds of km
- They are a major source of disturbance for propagation of radio waves
- Total loss of lock events (acquisition of fewer than 4 GPS satellites) are a proxy for severe ionospheric irregularities
- We use Swarm mission plasma density and GPS receivers data for this research.
-

Traditional methods and explanations

Plasma density irregularities are typically characterized by spectral slope index α , i.e. PSD proportional to $\frac{1}{f^\alpha}$

A single value of α indicates scale invariance

The scale-invariant structure of variability is explainable with a monofractal formalism where a single scaling (Hurst) exponent is enough for describing the fractal structures.

Multifractal Analysis

- Two similar multifractal analysis methods are: Structure function(SF) and detrended fluctuation analysis (DFA)

- The structure function of one-dimensional variable $X(t)$ is :

$$S_q(\tau) \equiv \langle [|X(t_{i+\tau}) - x(t_i)|]^q \rangle$$

$$S_q(\tau) \approx \tau^{h(q)}$$

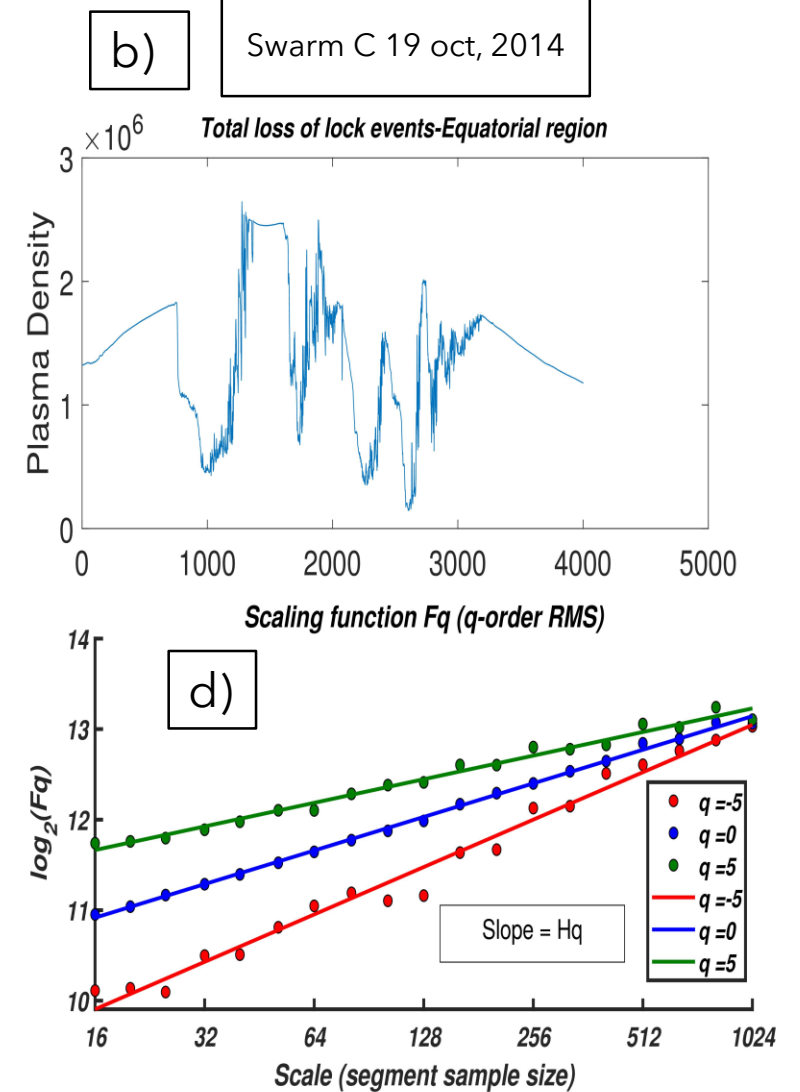
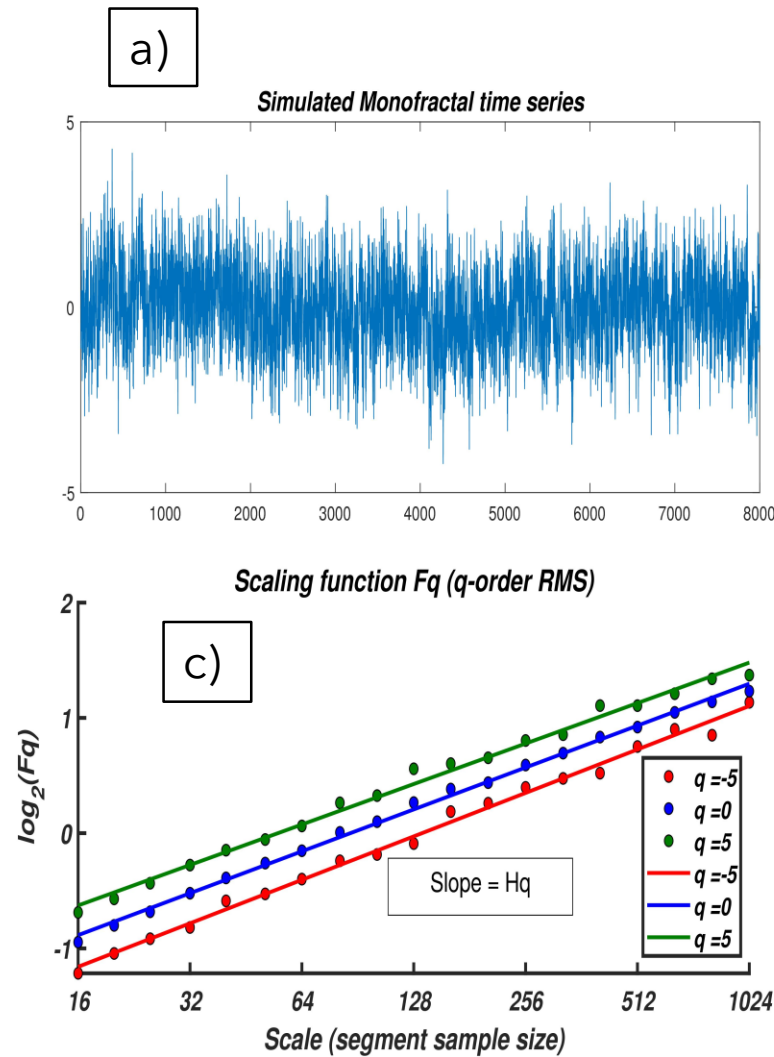
- The exponent factor of the first order structure function(H) is called Hurst exponent

$$S_1(\tau) \approx \tau^H$$

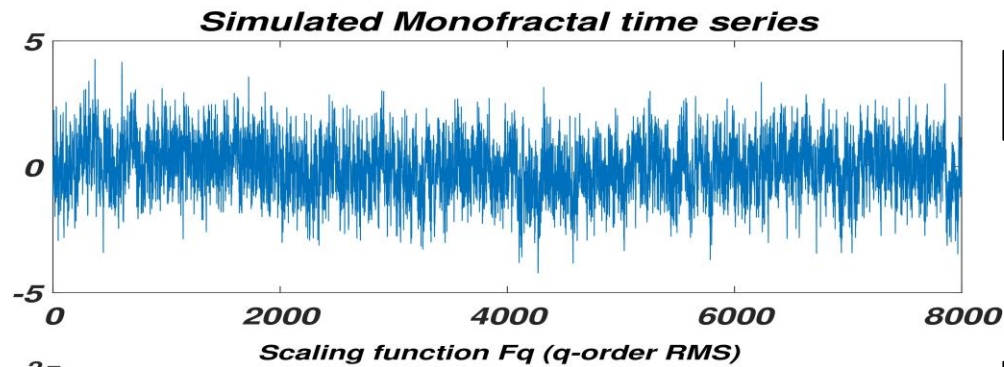
- For monofractals there is a relation between Hurst exponent and exponent factors of the different order structure function $h(q) = qH$
- For this research we use Detrended Fluctuation Analysis, which differs from the SF in that negative orders exist.

Scale exponent of different orders of detrended fluctuation analysis (DFA)

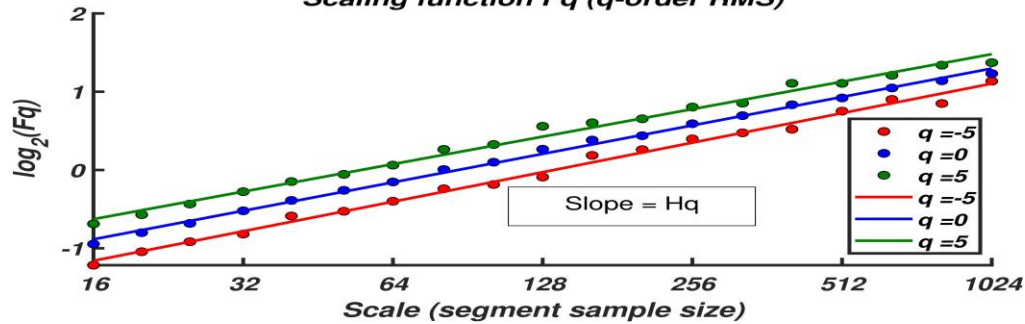
- a) Simulated monofractal time series
- b) Measured plasma density of a total loss of lock event at the equatorial region
- c) Slope of different order of DFA for monofractal data
- d) slope of different order of DFA for total loss of lock event
- Different slopes for different orders of DFA is a sign of multifractality



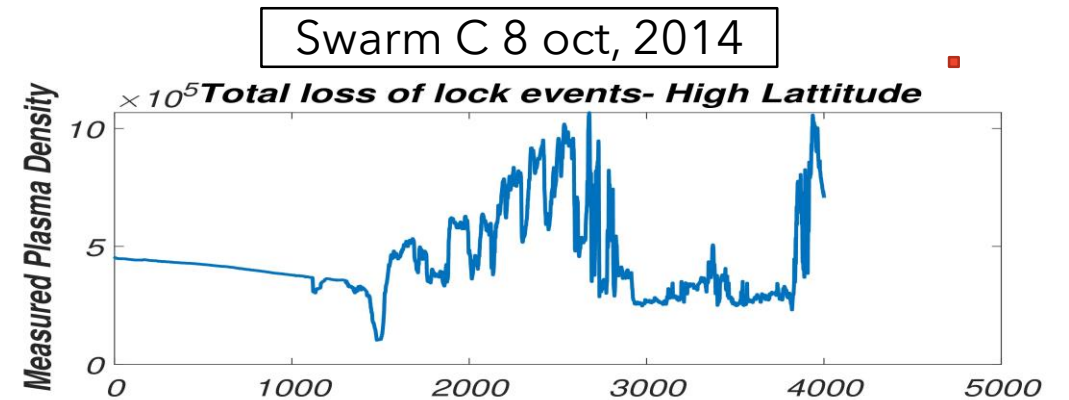
a)



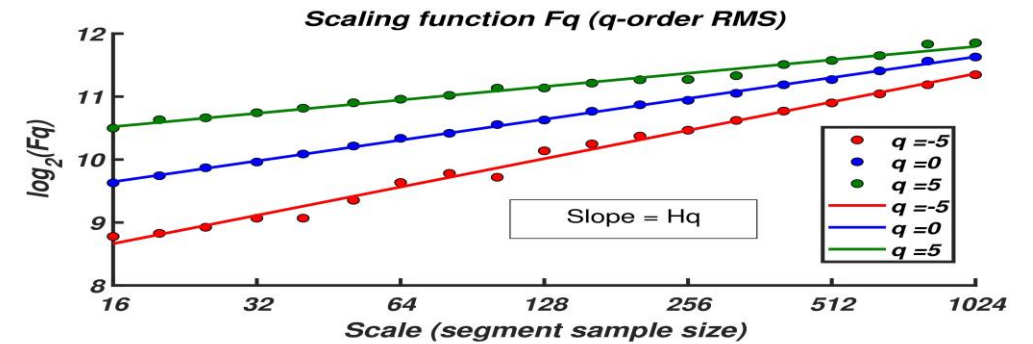
c)



b)



d)



Scale exponent of different order of detrended fluctuation analysis (DFA)

- In this slide we repeat the same procedure, but for a total loss of lock even at high latitude

Summary

- We present evidence for multifractality in the equatorial region and high latitude region of the ionosphere during total loss of lock of the Swarm GPS receivers
- For a better understanding of physics of ionospheric irregularities that cause total loss of lock and severe scintillation we need to consider multifractal structures instead of monofractal structures