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## Spherical and ellipsoidal surface mass change from GRACE time-variable gravity data

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## 1. Motivation:

- GRACE (Gravity Recovery and Climate Experiment),
- Mapping the Earth's time-variable gravitational field (2002-2017),
- Altitude: $\mathbf{\sim 4 6 0} \mathbf{~ k m}$ (above the Earth's surface),
- Spatial resolution: several 100 km,
- Temporal resolution: ~1 month.

- Revolutionary applications (geodesy, geophysics, hydrology, glaciology, oceanography, ...),
- GRACE-FO launched in 2018 to extend GRACE time series,
- Methodology, processing, and background geophysical models continuously improve,
- Standard approach for surface mass determination by Wahr et al. (1998) is based on the spherical approximation of the Earth,
- More realistic geometry, such as ellipsoidal, has to be considered for accurate modelling and geoscience applications.


## 2. Theory:

## A) Spherical surface mass (Wahr et al. 1998):

$$
\sigma_{\mathrm{S}}(R, \varphi, \lambda)=\frac{R \rho_{\mathrm{ave}}}{3} \sum_{n=0}^{\infty} \sum_{m=-n}^{+n} \frac{2 n+1}{1+k_{n}^{s}} \bar{C}_{n, m}^{\mathrm{s}} \bar{Y}_{n, m}(\varphi, \lambda)
$$

## Geometry:



## Notation:

$\sigma_{\mathrm{s}}$ - spherical surface mass,
$R, \varphi, \lambda$ - spherical geocentric coordinates,
$\rho_{\text {ave }}$ - average density,
$k_{n}^{\mathrm{S}}$ - spherical Love number,
$\bar{C}_{n, m}^{s}$ - spherical harmonic coefficient,
$\bar{Y}_{n, m}-$ surface (spherical) harmonic function.

## B) Ellipsoidal surface mass (Ghobadi-Far et al. 2019):

$$
\sigma_{\mathrm{E}}(a, b, \beta, \lambda)=\frac{a b \rho_{\mathrm{ave}}}{3 \sqrt{b^{2}+\left(a^{2}-b^{2}\right) \sin ^{2} \beta}} \sum_{n=0}^{\infty} \sum_{m=-n}^{+n} \frac{2 n+1}{1+k_{n, m}^{\mathrm{E}}} \frac{1}{T_{n, m}(a, b)} \bar{C}_{n, m}^{\mathrm{E}} \bar{Y}_{n, m}(\beta, \lambda)
$$

## Geometry:



## Notation:

$\sigma_{\mathrm{E}}$ - ellipsoidal surface mass,
$a$ - semi-major axis,
$b, \beta, \lambda-$ ellipsoidal geocentric coordinates,
$k_{n, m}^{\mathrm{E}}-$ ellipsoidal Love number,
$T_{n, m}$ - auxiliary function,
$\bar{C}_{n, m}^{\mathrm{E}}-$ ellipsoidal harmonic coefficient.

## 3. Numerical experiments:

- Spherical vs. ellipsoidal approach for computing surface mass change rate (linear trend),
- GRACE Level 2 monthly gravitational fields by the Center for Space Research (Bettadpur 2012), 2003-2015, RL06, up to d/o 60,
- Corrected for GIA (A et al. 2012), geocenter motion (Swenson et al. 2008), $\bar{C}_{2,0}$ from SLR (Cheng et al. 2013),
- Spherical surface mass changes calculated @ $R=6378136.3 \mathrm{~m}$,
- Ellipsoidal surface mass changes calculated @ EGM08 reference ellipsoid ( $a=6378136.3 \mathrm{~m}, b=6356751.6 \mathrm{~m}$ ).


## A) Spectrum of the surface mass change rate




## B) Surface mass change rate in Antarctica

Spherical approach


Ellipsoidal minus spherical


Relative difference


Absolute value of the signal
$>10 \mathrm{~cm} /$ year

## C) Surface mass change rate in Greenland

Spherical approach


Ellipsoidal minus spherical


Relative difference


Absolute value of the signal $>10 \mathrm{~cm} /$ year

## 4. Conclusions:

- We developed a rigorous ellipsoidal approach for the determination of the surface mass from the external gravitational field,
- The spherical approach by Wahr et al. (1998) underestimates the surface ice mass change by $\mathbf{1 0 - 1 5 \%}$ in Antarctica and Greenland,
- Source codes implementing the ellipsoidal approach are available to potential users.

More details can be found in:
Ghobadi-Far K, Šprlák M, Han S-C (2019) Determination of ellipsoidal surface mass change from GRACE time-variable gravity data. Geophysical Journal International 219(1):248-259.

## Thank you for your attention!!!

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