

## BITE The Bayesian Ice Thickness Estimation model

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#### ETH

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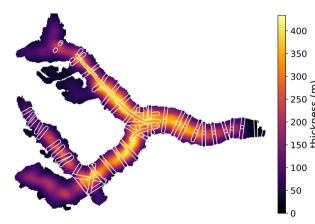
Versuchsanstalt für Wasserbau, Hydrologie und Glaziologie







### Modelling ice thickness maps



BITE-modelled thickness of Unteraar Glacier with superimposed radar-measured thickness (white-framed)

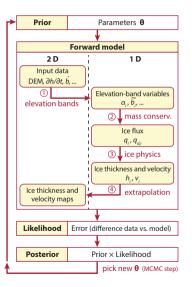
• ice thickness is needed for ice flow modelling, hydrological forecasts and sea-level rise projections

 various models have been proposed to do this (see overview in Farinotti & al. 2017)

# This work is published in Werder & al. (2020)

A Bayesian ice thickness estimation model for large-scale applications Journal of Glaciology 66(255), 137–152.

#### The BITE model



We combine an established forward model with a Bayesian inversion scheme.

- forward model of Huss & Farinotti, 2012 based on mass conservation, the shallow ice approximation, and empirical relations
- stochastic model posits that model errors have a normal distribution



Bayes for parameters  $\theta$  and data d:

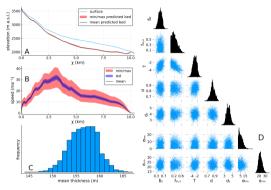
$$p(\theta|d) = \frac{p(d|\theta) p(\theta)}{p(d)},$$

Likelihood:

$$p(d|\theta) \propto \underbrace{\frac{1}{\sigma_{\rm h}} \mathrm{e}^{-\frac{\sum(h(\theta)-h')^2}{2\sigma_{\rm h}^2}}}_{\text{thickness error}} + \dots$$

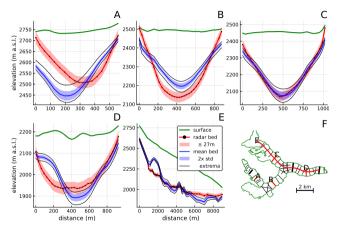
Priors ( $\theta$ ) for the model parameters  $\theta$  given by other models and measurements.

Using MCMC method to calcualte the distribution of  $\theta$ s and make predictions – including uncertainties – for thickness and surface speed.



(A) flow line geometry: given surface and modelled bed (with uncertainty). (B) modelled surface flow speeds (with uncertainty). (C) Distribution of mean glacier thickness. (D) scatter and histogram plots of fitted parameters.

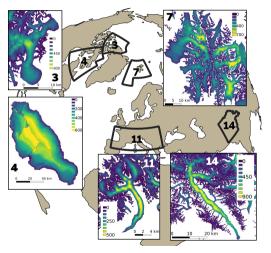
#### Results: Unteraar Glacier



Modelled (blue) vs measured (red) ice thickness at selected profiles (marked as red lines in panel (F)). The three thick black lines are the tracks used to fit the model.

The model is fitted to Unteraar Glacier to show-case.

- model fits data relatively well
- model as setup is limited to one profile shape, modified by surface features

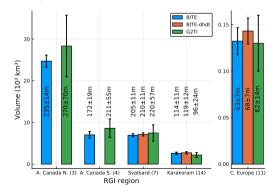


Globe with the five RGI regions marked. Insets show example thickness maps from each region.

#### Results: regional application

The model was applied to all glacier from five RGI regions, amounting to  ${\sim}30'000$  glaciers.

The comparison to the recent consensus estimate from the G2TI study (Farinotti & al., 2019) shows good agreement:



#### Conclusions



BITE-Model

BITE-Model: Bayesian Ice Thickness Estimation Model

TOC Data Loading Forward Model Inverse Model Post-processing and PI API Index • BITE-Model: Bayesian Ice Thickness Estimation Model

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BITE-Model: Bayesian Ice Thickness Estimation Model



Surging, biting Vernagtferner by R. Reschreiter (1911)

This model can be used to estimate ice thickness maps of mountain glaciers and ice caps. It needs surface elevation and a glacier outline and can make use of the following additional data: surface mass balance,

Documentation of BITE model. Code hosted on https://github.com/mauro3/BITEmodel.jl

- BITE model performs as well as the best other models
- However, ice surface flow speeds are not improving the assimilation :-(
- How to best transfer parameters from glaciers with ample measurements to others with no or few measurements is not clear yet
- applied to 30'000 glaciers requiring the calculation of  $10^8$  ice thickness maps
- Model is open source, written in Julia 🖡

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