

J. Molson<sup>1</sup>, E.O. Frind<sup>2</sup> <sup>1</sup>Department of Geology and Geological Engineering, Université Laval, Québec, Québec, Canada [john.molson@ggl.ulaval.ca](mailto:john.molson@ggl.ulaval.ca)  
<sup>2</sup>Department of Earth and Environmental Sciences, University of Waterloo, Waterloo, ON

## Context

Age simulations can be applied in a variety of contexts including defining capture zones for pumping wells, characterizing fractured rock aquifers, and for improved understanding of flow systems and geochemical evolution.

## Methodology

We apply the finite element models FLONET/TR2 (in the 2D vertical plane; Molson & Frind, 2020) and HEATFLOW (in 3D systems), using the standard advection-dispersion equation with an age source term. The governing equations for mean age ( $A$ ) or residence time, including advective-dispersive age mixing within a porous medium can be written as:

$$\frac{\partial}{\partial x_i} \left[ D_{ij} \frac{\partial A}{\partial x_j} \right] - v_i \frac{\partial A}{\partial x_i} + 1 = 0$$

where  $x_i$  are the spatial coordinates ( $x, y$ ) ( $L$ ),  $v_i$  is the average linear flow velocity ( $L/T$ ),  $D_{ij}$  is the hydrodynamic dispersion tensor ( $L^2/T$ ),  $A$  is the mean age ( $T$ ), and the +1 source term expresses the growth of the age mass at the rate of 1 day/day as it moves along its flowpath in the forward (downgradient) direction. A Type-1 boundary condition where  $A=0$  is applied along recharge zones. Life expectancy uses a similar equation in a reversed flow field. The codes are available without charge for research use; please contact authors..

## Numerical Simulations

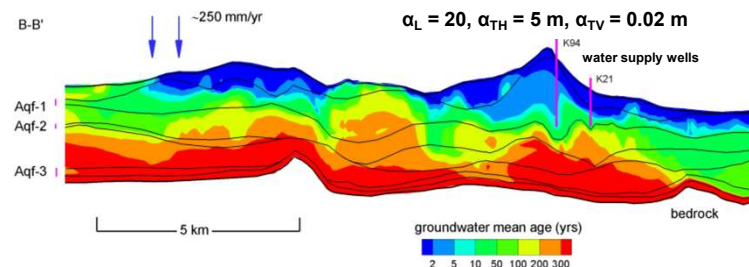


Fig. 1 3D model of groundwater age in a multi-aquifer system

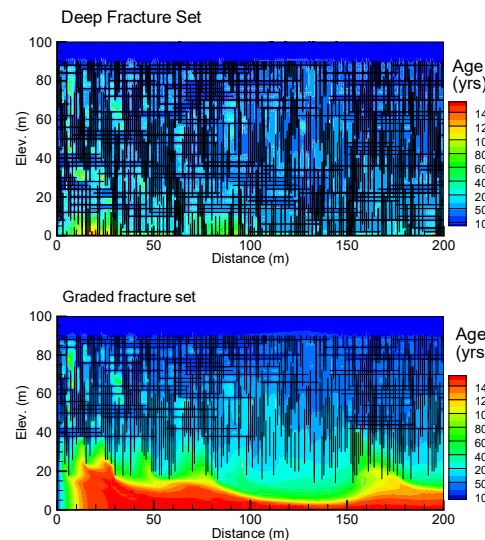


Fig. 2 Groundwater age in a discrete fracture network

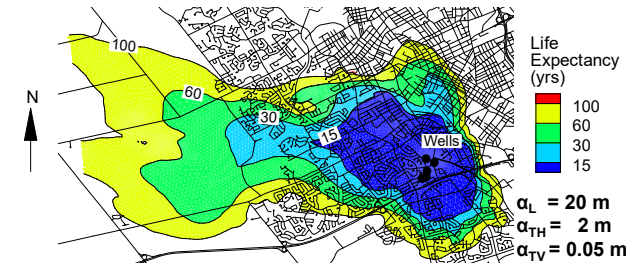


Fig. 3 Application to well-head protection zones

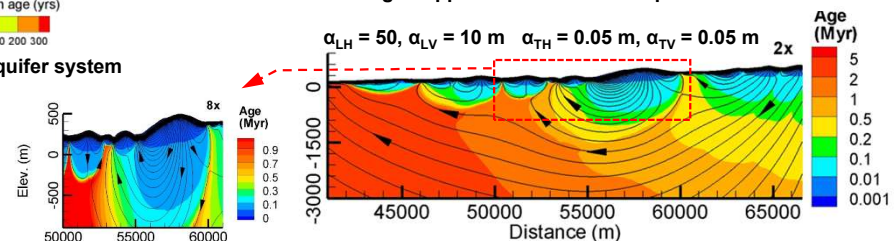


Fig. 4 Simulated age distribution in a regional groundwater flow system (Flonet/TR2 model).

## Discussion:

- Age simulations provide insight into complex flow systems
- Dispersivities control age mixing, the Lichtner (2002) formulation is preferred

## References:

- Janos, D., Molson, J., Lefebvre, R., Regional groundwater flow dynamics and residence times in Chaudière-Appalaches, Québec, Canada: Insights from numerical simulations, *Canadian Water Resources Journal*, Special Issue : Quebec PACES Projects, <https://doi.org/10.1080/07011784.2018.1437370>, 2018.
- Lichtner, P.C., Kelkar, S., & Robinson, B., New form of dispersion tensor for axisymmetric porous media with implementation in particle tracking. *Water Resources Research*, Vol. 38/8, 2002.
- Molson, J.W., E.O. Frind, On the use of mean groundwater age, life expectancy and capture probability for defining aquifer vulnerability and time-of-travel zones for source water protection, *J. Contaminant Hydrology*, Vol. 127, p76–87, [doi:10.1016/j.jconhyd.2011.06.001](https://doi.org/10.1016/j.jconhyd.2011.06.001), 2012.
- Molson, J.W. and E.O. Frind, *FLONET/TR2 User Guide*, A Two-Dimensional Simulator for Groundwater Flownets, Contaminant Transport and Residence Time, Université Laval, 2020.