

# An idealised setup for future experiments in satellite data assimilation research

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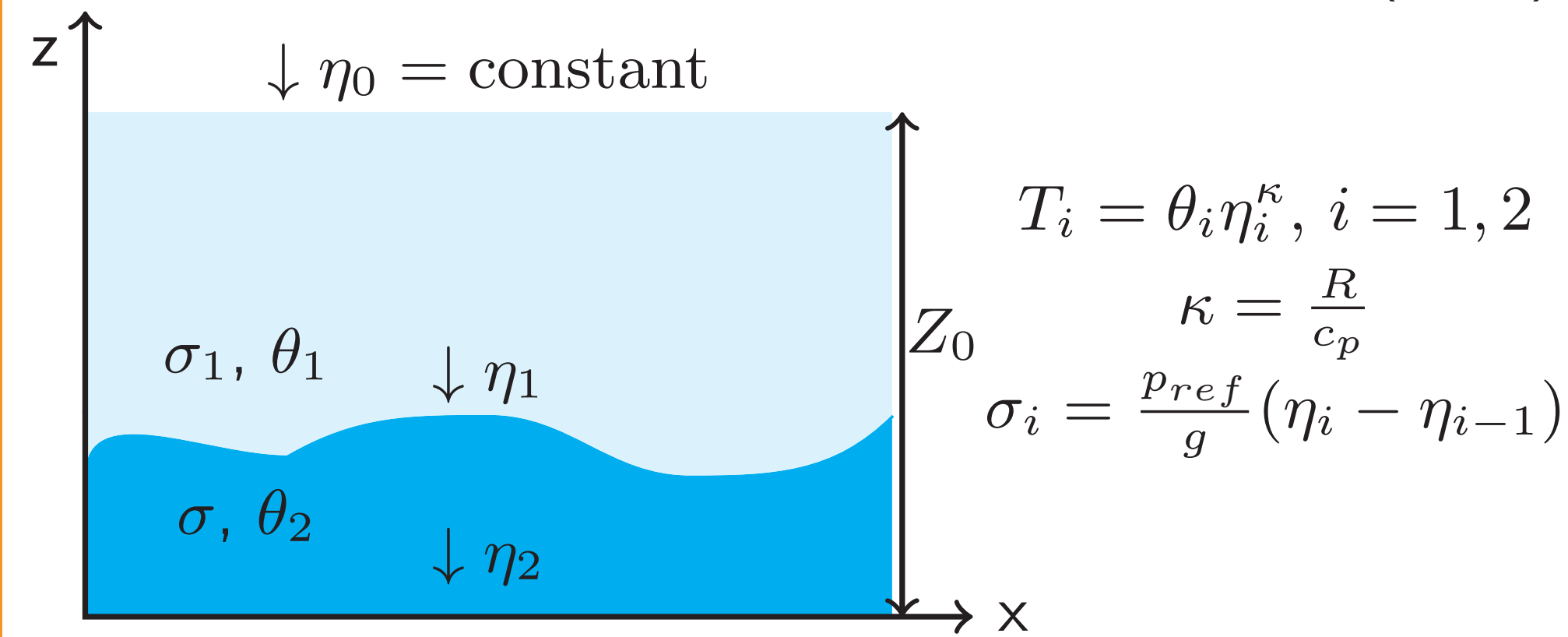
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## 1. OBJECTIVE

Operational data assimilation (DA) schemes rely significantly on satellite data. Our aim is to investigate **the impact of satellite observations of different spatial-temporal scales**: is there a case for concentrating effort into the assimilation of small-scale features over the large-scale dynamics, or vice versa?

## 2. THE ‘ISENRSW’ MODEL

We conduct our study with an **idealised model**: an isentropic 1.5D 1.5-layer model based on **modified** shallow water equations, able to mimic convection and precipitation (**no topography**). This is an updated version of the model developed by Kent et al. (2017).



In the sketch above:  $\theta_i$  is the potential temperature,  $\eta_i$  the (non-dimensional) pressure,  $T_i$  the temperature,  $R$  the specific gas constant for dry air,  $c_p$  the heat coefficient at constant pressure,  $g$  is the gravity acceleration and  $p_{ref}$  is a reference pressure. The non-dim system of eqs. reads:

$$(\sigma)_t + (\sigma u)_x = 0, \quad (1a)$$

$$(\sigma u)_t + (\sigma u^2 + \mathcal{M}(\sigma))_x + \sigma c_0^2 r_x = \frac{1}{Ro} \sigma v, \quad (1b)$$

$$(\sigma v)_t + (\sigma uv)_x = -\frac{1}{Ro} \sigma u, \quad (1c)$$

$$(\sigma r)_t + (\sigma ur)_x + \beta \sigma u_x + \alpha \sigma r = 0, \quad (1d)$$

in which:  $Ro$  is the Rossby number,  $\mathcal{M}$  the effective pressure,  $\sigma$  is the layer pseudo-density,  $u$  and  $v$  are the zonal and the meridional velocities and  $r$  is the ‘mass rain fraction’: a proxy for precipitation. **Convection and rain are triggered by a threshold mechanism** for  $\sigma$ :

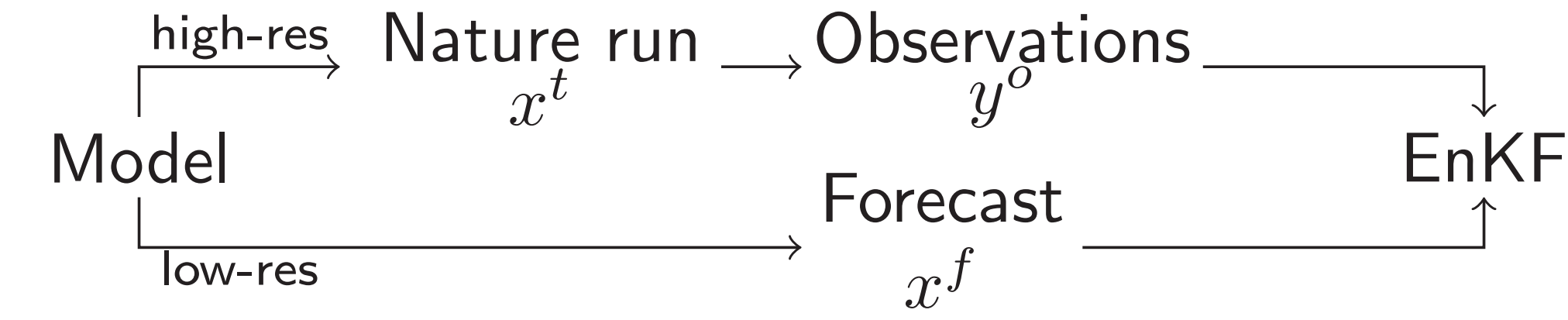
$$\mathcal{M}(\sigma) = \begin{cases} \mathcal{M}(\sigma) & \text{if } \sigma < \sigma_c, \\ \mathcal{M}(\sigma_c) & \text{if } \sigma \geq \sigma_c, \end{cases} \quad (2)$$

$$\beta = \begin{cases} \tilde{\beta} & \text{if } \sigma \geq \sigma_r, u_x < 0, \\ 0 & \text{otherwise.} \end{cases} \quad (3)$$

with  $\sigma_c < \sigma_r$ .  $\alpha$ ,  $\tilde{\beta}$  and  $c_0^2$  are additional model parameters controlling: the removal of rain ( $\alpha$ ), its production ( $\tilde{\beta}$ ) and the suppression of convection ( $c_0^2$ ), respectively.

## 3. DATA ASSIMILATION WITH THE ‘ISENRSW’ MODEL

We exploit a **twin-setting** configuration and use a **Deterministic Ensemble Kalman Filter** (DEnKF, as per Sakov & Oke, 2008) for data assimilation.



## 4. THE OBSERVING SYSTEM

A set of pseudo-observations is derived from the nature run at each analysis step. The observation vector  $y^o$  is made of **ground** and **satellite** observations.

### Satellite observations

Derived from the pseudo-density  $\sigma$ , we recreate vertically integrated **passive microwave radiation**  $B_{sat}$  (see section 5) and use the Rayleigh-Jeans law as radiative scheme. The non-dimensional radiation in each layer  $B_i$  is:

$$B_i = \eta_i^\kappa. \quad (4)$$

To mimic polar-orbiting satellites, 1D approximation: our satellite moves at constant  $v_{sat}$  and reenters the domain periodically (of length  $L$ ). Observations  $B_{sat}$  at time  $t$  will be located at:

$$x_{sat} = v_{sat} \cdot t \bmod L. \quad (5)$$

Each  $B_{sat}$  observation is a **weighted contribution from each layer** (see also section 5) and is also a **weighted horizontal average** that tries to reproduce a satellite's Field of View (FOV) of width  $\Delta x$ :

$$B_{sat}(x_{sat}) = \frac{\int_{x_{sat}-\Delta x/2}^{x_{sat}+\Delta x/2} B(x) w(x) dx}{\int_{x_{sat}-\Delta x/2}^{x_{sat}+\Delta x/2} w(x) dx}, \quad (6)$$

in which  $w(x)$  is Gaussian function centered on  $x_{sat}$  with a width comparable to  $\Delta x$ .

### Ground observations

Variables such as  $u$ ,  $v$  and  $r$  are assimilated at fixed evenly spaced locations along the domain (e.g. one each  $\sim 50 - 80$  km, N.B. tunable) at each analysis step.

## 6. OBSERVATION OPERATOR

A Deterministic Ensemble Kalman filter is used and the linearisation of the observation operator (i.e.,  $\mathbf{H} = \nabla \mathcal{H}$ ) is performed to compute the Kalman Gain  $\mathbf{K}$ , so that ensemble covariance localisation can be maintained in physical space. The right panel of Figure 2 shows the only non-trivial element of this (sparse) matrix, namely  $\frac{\partial B_{sat}}{\partial \sigma}$ , as a function of  $\sigma$ . The fully non-linear observation operator is used in the innovation vector.

## 5. MODELING CLOUDS

We exploit the 1.5-layer configuration to generate pseudo-vertically integrated values of radiance:

$$B_{sat} = \alpha_1 \cdot B_1 + \alpha_2 \cdot B_2. \quad (7)$$

$\alpha_1$  and  $\alpha_2$  (see Figure 2, left panel) are chosen such that our system can mimic the response of passive microwave radiation to the presence of both non-precipitating and precipitating clouds, exploiting the convection and the rain threshold  $\sigma_c$  and  $\sigma_r$ :

$$\begin{aligned} \sigma < \sigma_c < \sigma_r & \quad \text{clear – sky conditions;} \\ \sigma_c < \sigma < \sigma_r & \quad \text{non – precipitating clouds;} \\ \sigma_c < \sigma_r < \sigma & \quad \text{precipitating clouds.} \end{aligned}$$

Generally speaking, emitted microwave radiation is absorbed by non-precipitating clouds and scattered by precipitating ones. Above low-emissivity surfaces (i.e. the ocean), this turns into an increase in the radiance reaching the sensor in the presence of non-precipitating clouds and a decrease when precipitating clouds are present. This is the physical mechanism we are trying to imitate (see Figure 2, center panel).

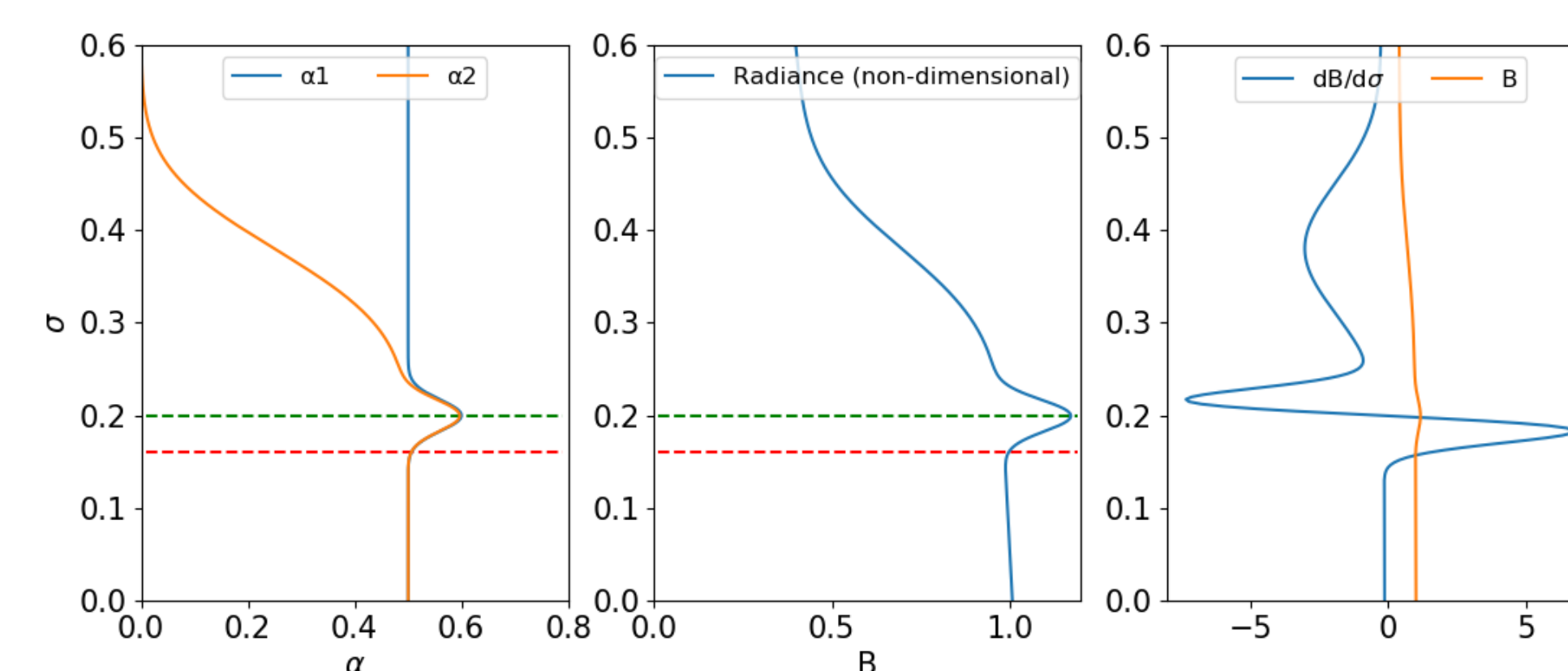


Figure 1: Plots of  $\alpha_1$ ,  $\alpha_2$  (left panel),  $B_{sat}$  (central panel) and  $\partial_\sigma B_{sat}$  (right panel) as a function of the pseudo-density in the bottom layer  $\sigma$ . The red and green dotted lines indicate the convection ( $\sigma_c$ ) and the rain thresholds ( $\sigma_r$ ), respectively.

## 7. THE NATURE RUN

The nature run is the high-resolution deterministic model integration from which we derive the pseudo-observations to be used in the data assimilation scheme. The one shown below represents a dynamically interesting case (with continuous production of convection and rain) and will be used in our future forecast-assimilation experiments.

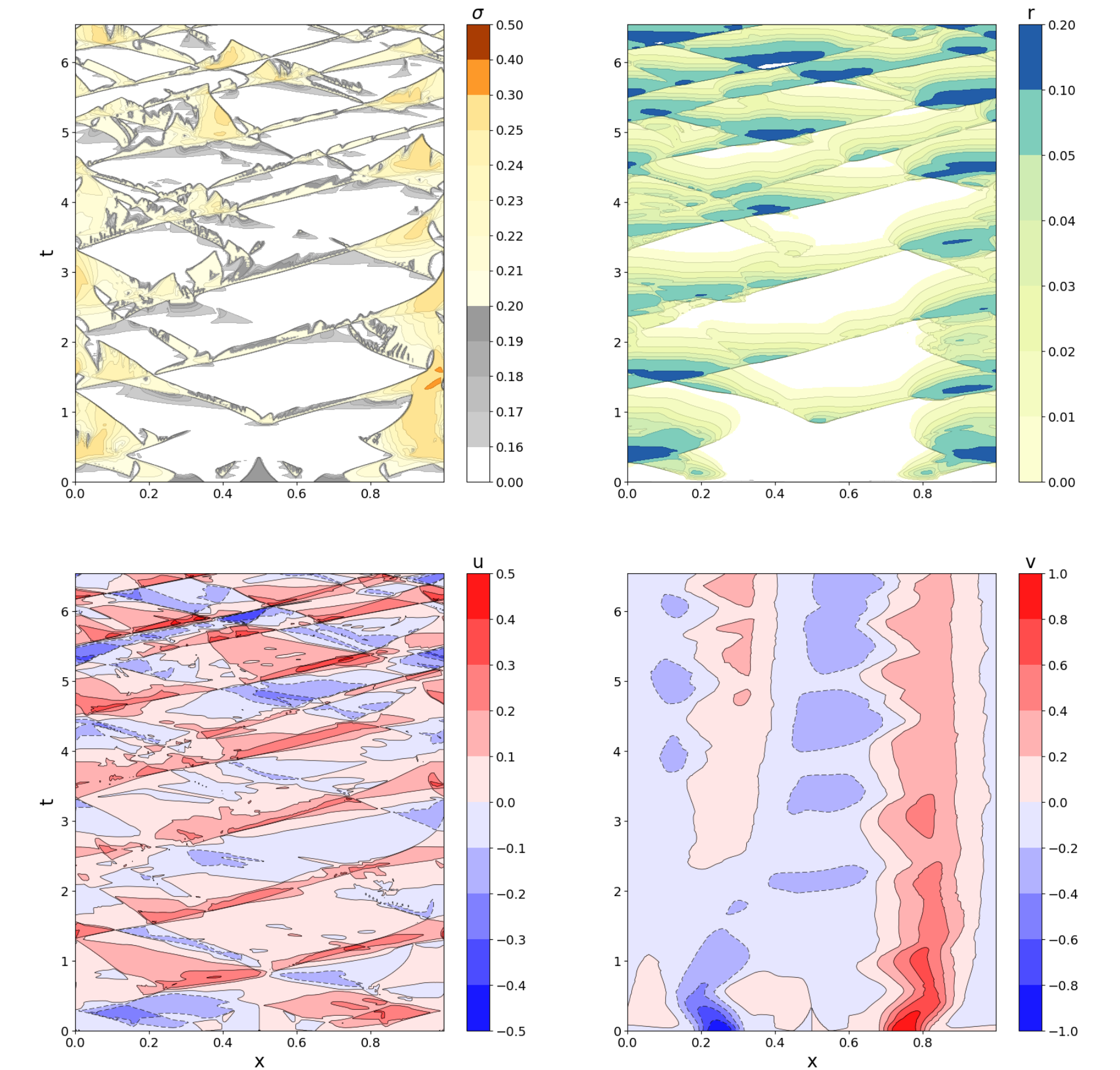


Figure 2: Hövmoller plots of the model evolution for each variable. Model parameters:  $\theta_1 = 300$  K,  $\theta_2 = 290$  K,  $Z_0 = 11000$  m,  $\eta_0 = 0.22$ ,  $\sigma_c = 0.16$ ,  $\sigma_r = 0.2$ ,  $\alpha = 5.0$ ,  $\tilde{\beta} = 0.8$ ,  $c_0^2 = 2.0$ ,  $Ro = 0.4$ .

## 8. CONCLUSIONS

- We have developed an isentropic 1.5-layer model to conduct future forecast-assimilation experiments relevant for satellite DA research;
- We have shown a dynamically interesting nature run simulation, our test-bed for future experiments;
- We have recreated a complex observing system that mimics satellite observations of passive microwave radiation taking also into account the effect of clouds and precipitation.

## 9. FUTURE WORK

Starting from the setup described here, idealised forecast-assimilation experiments will follow, to investigate the impact of satellite observations of different scales: for example, this can be achieved by varying  $\Delta x$ . The addition of more satellite observations to the observing system will be explored if required.



#### References:

- [1] Kent, T., Bokhove, O., & Tobias, S. (2017). Dynamics of an idealized fluid model for investigating convective-scale data assimilation. *Tellus A: Dynamic Meteorology and Oceanography*, 69(1), 1369332.
- [2] Sakov, P., & Oke, P. R. (2008). A deterministic formulation of the ensemble Kalman filter: an alternative to ensemble square root filters. *Tellus A: Dynamic Meteorology and Oceanography*, 60(2), 361-371.