



# Preliminary application of machine learning in ensemble forecasting

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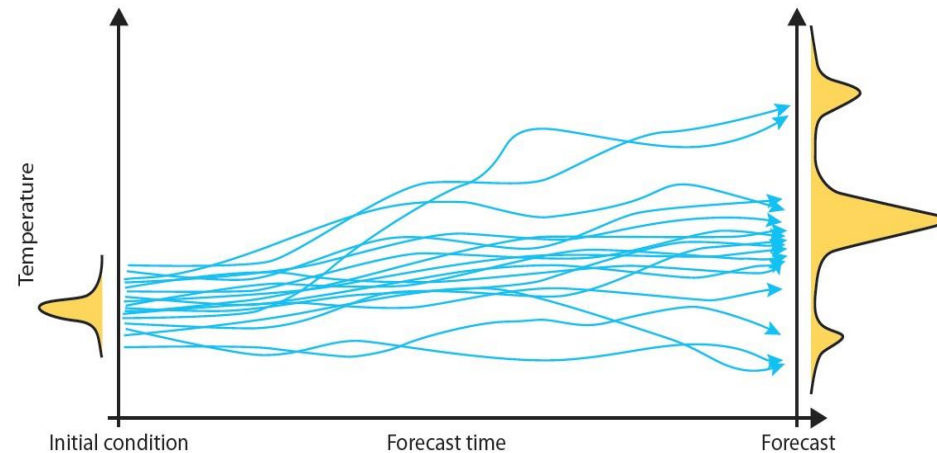
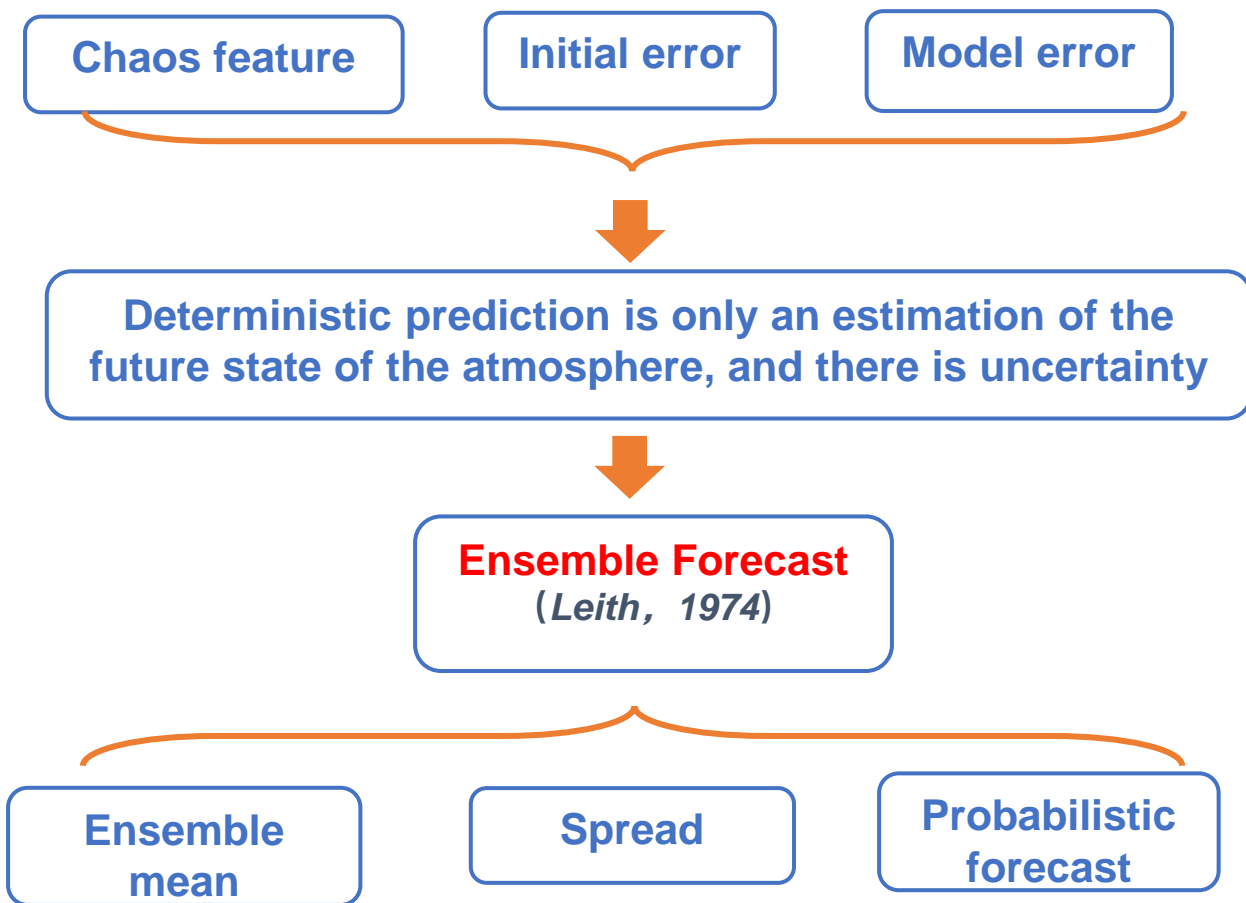


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# 1. Introduction



**Ensemble Forecast (ECMWF,2012)**

| TABLE 1. TIGGE project partners.                   |                |         |
|--|----------------|---------|
| Center   | Country        | Acronym |
| Bureau of Meteorology                              | Australia      | BoM     |
| China Meteorological Administration                | China          | CMA     |
| Canadian Meteorological Centre                     | Canada         | CMC     |
| Centro de Previsão de Tempo e Estudos Climáticos   | Brazil         | CTPEC   |
| European Centre for Medium-Range Weather Forecasts | Europe         | ECMWF   |
| Japan Meteorological Agency                        | Japan          | JMA     |
| Korea Meteorological Administration                | Korea          | KMA     |
| Météo-France                                       | France         | MF      |
| Met Office   | United Kingdom | UKMO    |
| National Center for Atmospheric Research           | United States  | NCAR    |
| National Centers for Environmental Prediction      | United States  | NCEP    |
| National Climatic Data Center                      | United States  | NCDC    |

*Richard Swinbank et al., 2016, BAMS*

**What and why?**



# 1. Introduction

## Methods

Compared with Linear singular Vectors (SVs) and forcing singular vectors (FSVs), orthogonal conditional nonlinear optimal perturbations (O-CNOPs) and orthogonal nonlinear forcing singular vectors (O-NFSVs) consider the influence of nonlinear physical process, and give more accurate ensemble average and more reasonable prediction uncertainty estimation.

*(Duan and Huo, 2016; Huo and Duan, 2018)*

## But

O-CNOPs and O-NFSVs have the drawback of high computational cost.  
In practical weather prediction, the ensemble members usually need to be generated quickly.

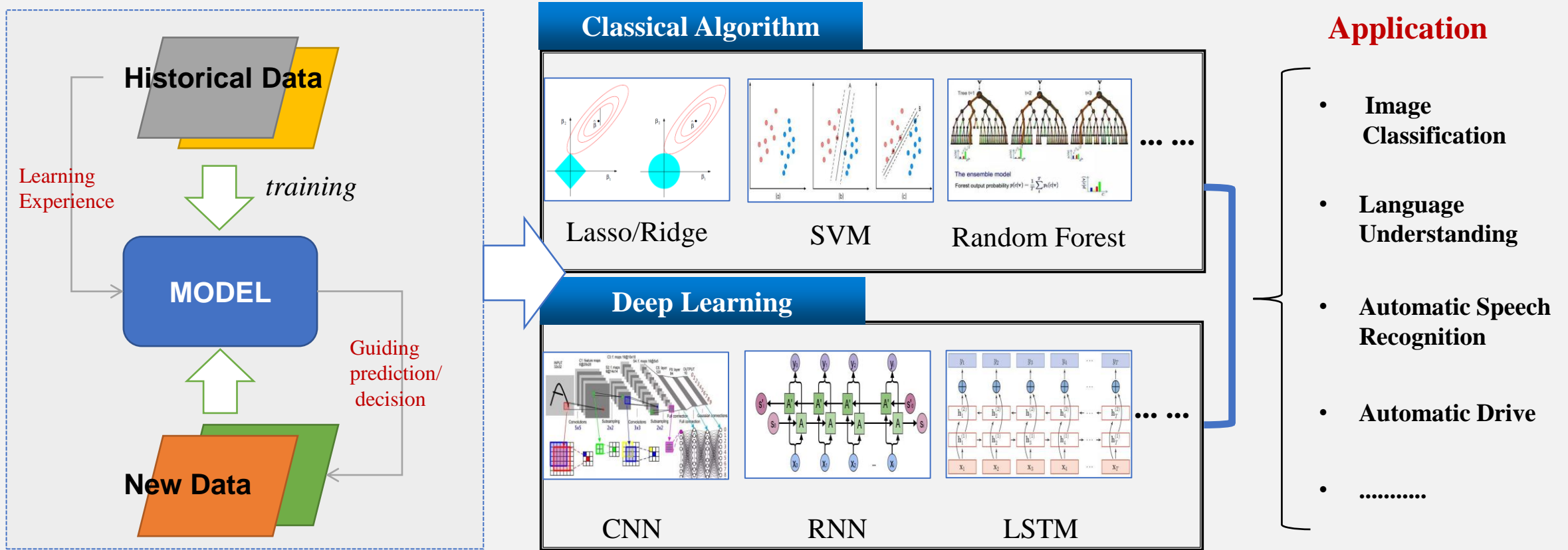
## So

**◆How to model and benefit from O-CNOPs and O-NFSVs ?**



# 1. Introduction

## Machine Learning



◆ Machine Learning provides some thoughts to solve the above problem.



## 2.1 O-CNOPs and O-NFSVs

### ➤ O-CNOPs

Forecast model with  
initial perturbation

$$\begin{cases} \frac{\partial(U+u)}{\partial t} = F(U+u), \\ U+u|_{t=0} = U_0 + u_0. \end{cases}$$

prediction

$$U(x, \tau) = M_\tau(U_0 + u_0)$$

Prediction error

$$J(u_{0j}) = \|M_\tau(U_0 + u_{0j}) - M_\tau(0)(U_0)\|_2$$

$$J(u_{0j}^*) = \max_{u_{0j} \in \Omega_j^{(1)}} J(u_{0j})$$

$$\Omega_j^{(1)} = \begin{cases} \{u_{0j} \in R^n \mid \|u_{0j}\| \leq \delta_u\}, j = 1 \\ \{u_{0j} \in R^n \mid \|u_{0j}\| \leq \delta, u_{0j} \perp \Omega_k, k = 1, \dots, j-1\}, j > 1 \end{cases}$$

### ➤ O-NFSVs

Forecast model with  
model perturbation

$$\begin{cases} \frac{\partial(U+u)}{\partial t} = F(U+u) + f(x), \\ U+u|_{t=0} = U_0 + u_0. \end{cases}$$

prediction

$$U(x, \tau) = M_\tau(f)(U_0 + u_0)$$

Prediction error

$$J(u_{0j}, f_j) = \|M_\tau(f_j)(U_0) - M_\tau(0)(U_0)\|_2$$

$$J(f_j^*) = \max_{f_j \in \Omega_j^{(2)}} J(f_j)$$

$$\Omega_j^{(2)} = \begin{cases} \{f_j \in R^n \mid \|f_j\| \leq \delta_f\}, j = 1 \\ \{f_j \in R^n \mid \|f_j\| \leq \delta, f_j \perp \Omega_k, k = 1, \dots, j-1\}, j > 1 \end{cases}$$



## 2.2 Lorenz-96 model

The model is governed by the following differential equation:

$$\frac{dX_j}{dt} = (X_{j+1} - X_{j-2})X_{j-1} - X_j + F$$

where  $j = 1, 2, \dots, m$ , with cyclic boundary conditions ( $X_{-1} = X_{m-1}$ ,  $X_0 = X_m$ ,  $X_1 = X_{m+1}$ ).

**Configuration:**  $m=40$ , fourth-order Runge–Kutta scheme, 0.05 time units (6h)

*The variables in the differential equation are nondimensional and can describe the main basic characteristics of atmospheric motion and be commonly used to simulate atmospheric dynamics over a single latitudinal circle, such as the dynamical behavior of vorticity, temperature, and gravitational potential.*

**(Lorenz and Emanuel, 1998; Basnarkov and Kocarev, 2012; Duan and Huo, 2016)**



## 2.3 Machine learning in ensemble forecasting

### Clustering Analysis :

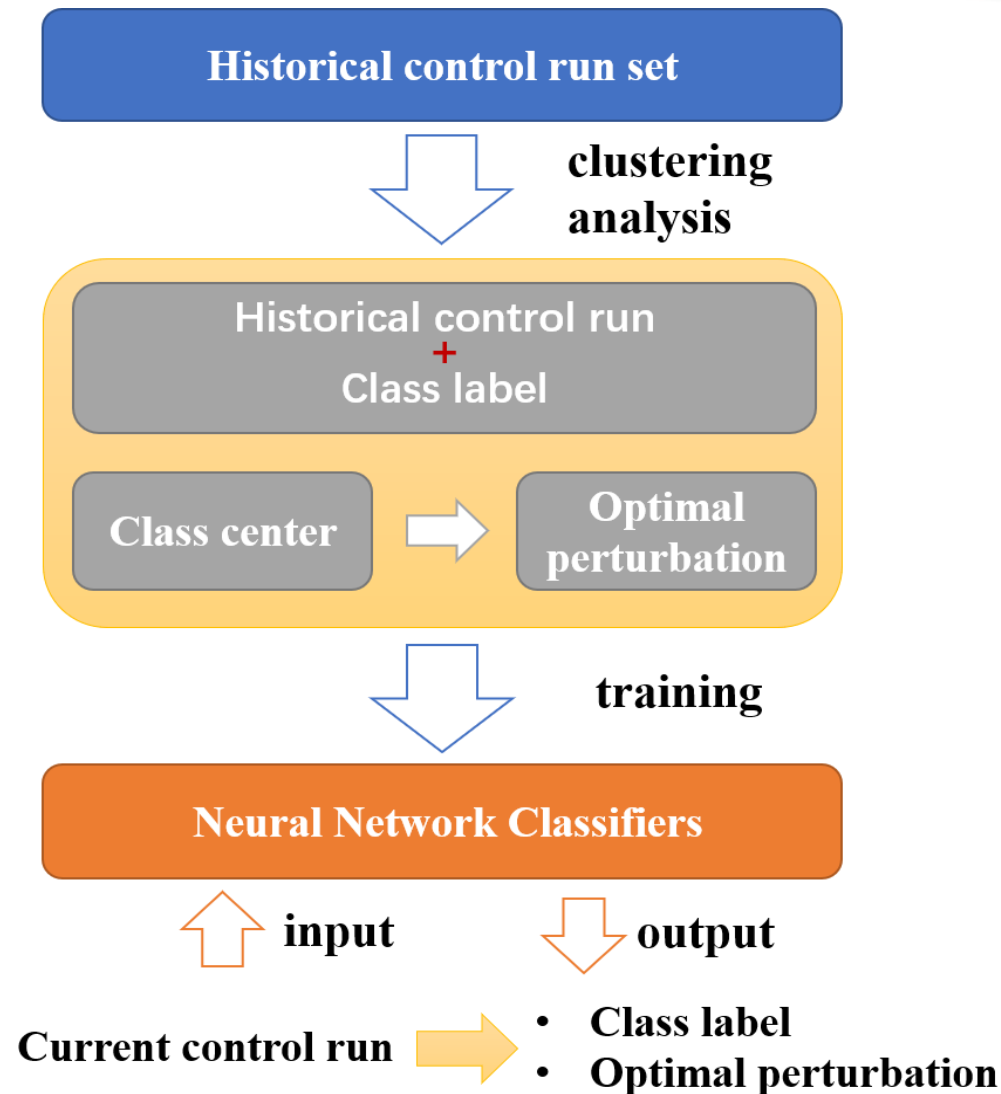
- Hierarchical clustering

### Control Run:

- Spatial data (~Image classification)
- Time series (~Language understanding)

### Neural Network Classifiers:

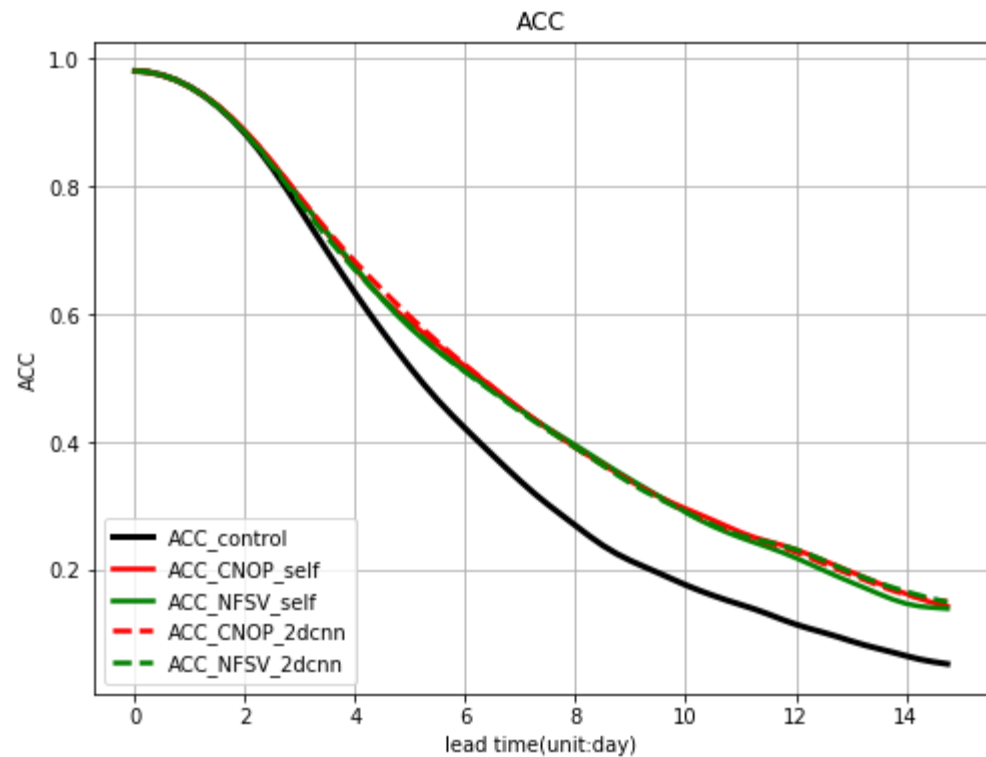
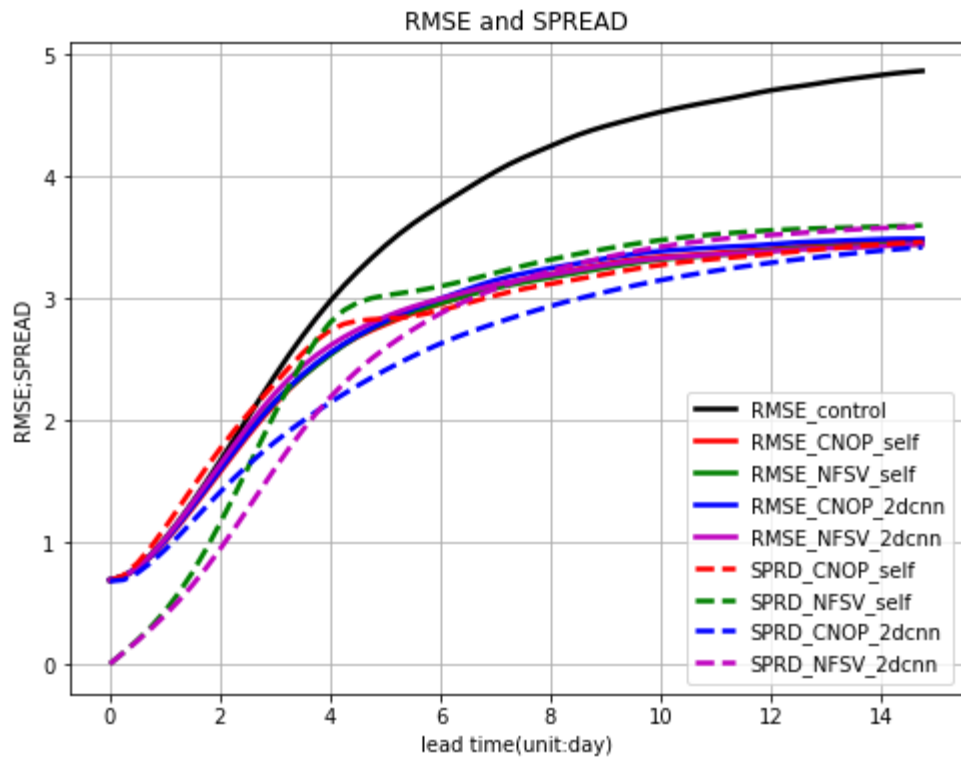
- Convolutional neural network (CNN)
- Recurrent neural network (RNN)







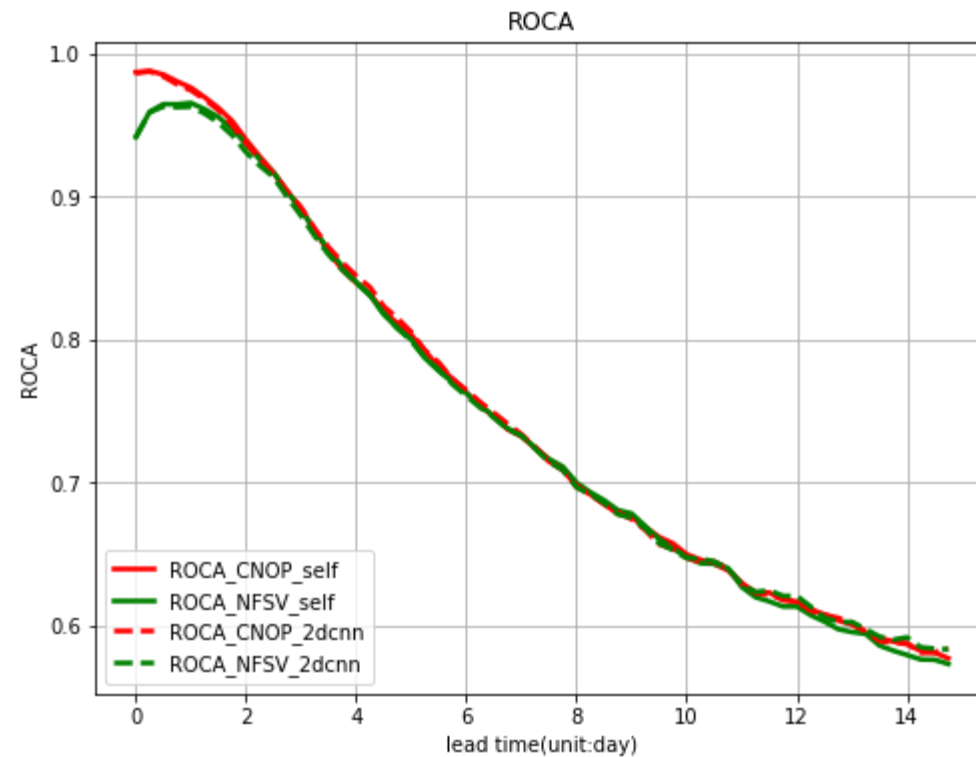
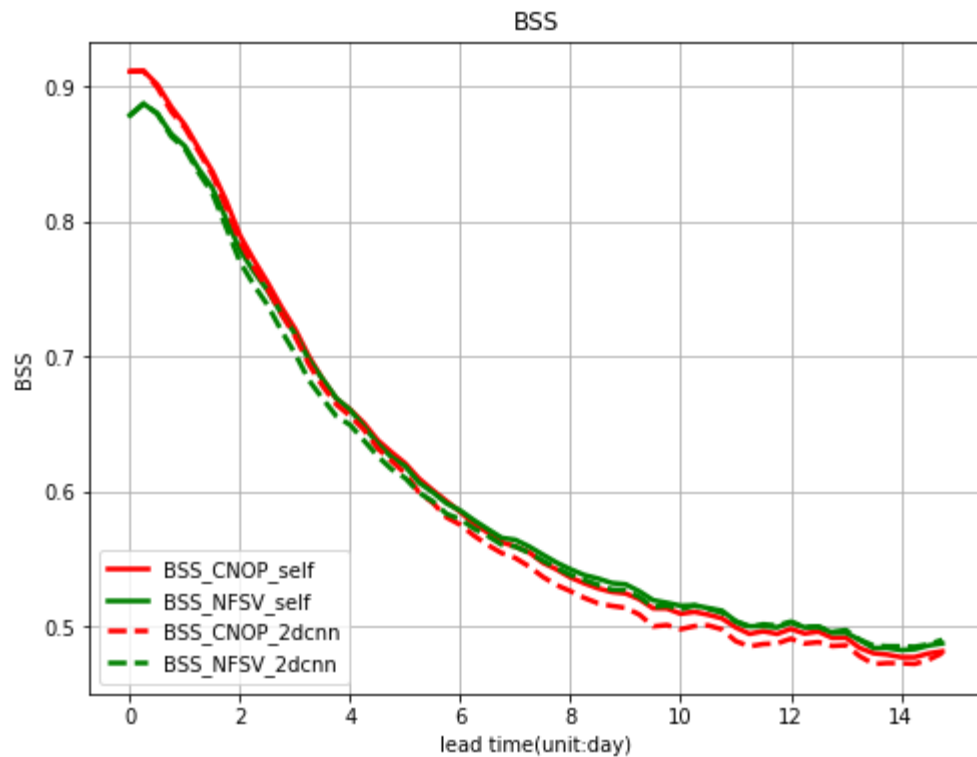
## 3.1 Results and comparison-CNN



From the comparison of RMSE/SPRD, the O-CNOPs ensemble forecast with optimization algorithm is more reliable than ensemble forecast with CNN, but from the comparison of RMSE and ACC, the ensemble forecast with CNN is acceptable.



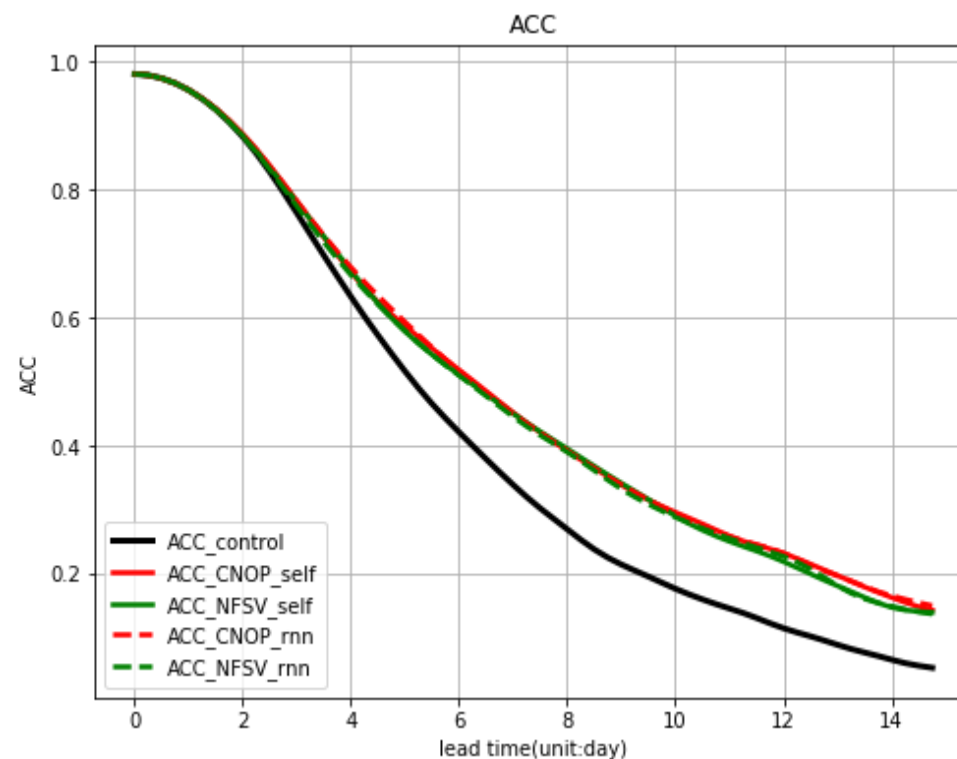
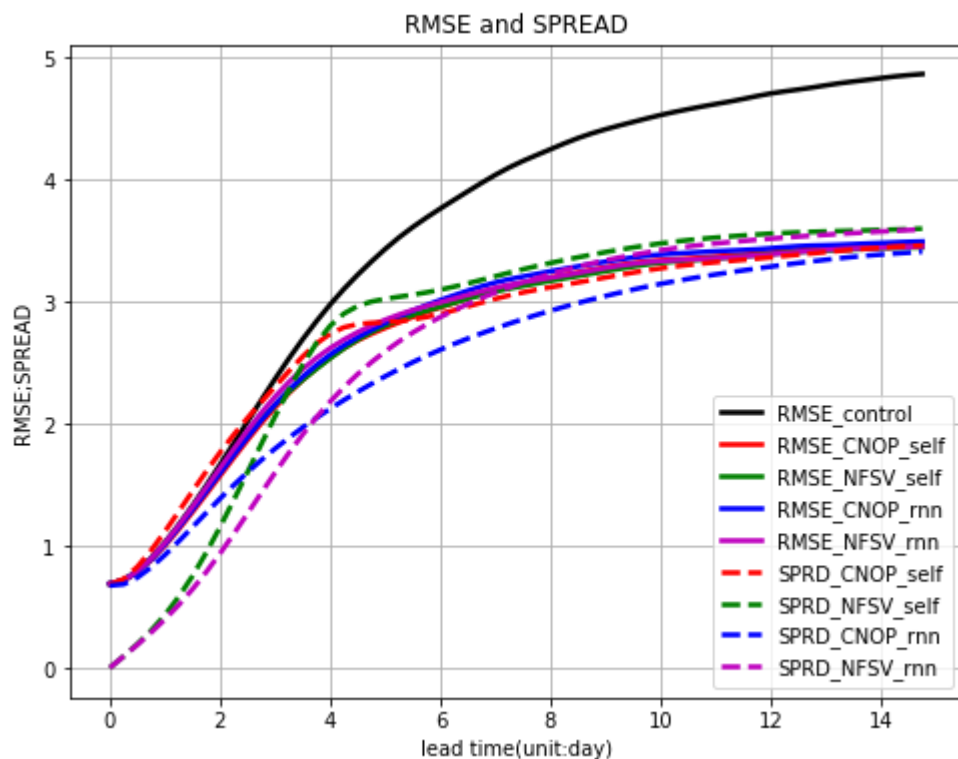
## 3.1 Results and comparison-CNN



From the comparison of BSS and ROCA, the ensemble forecast with CNN is acceptable.



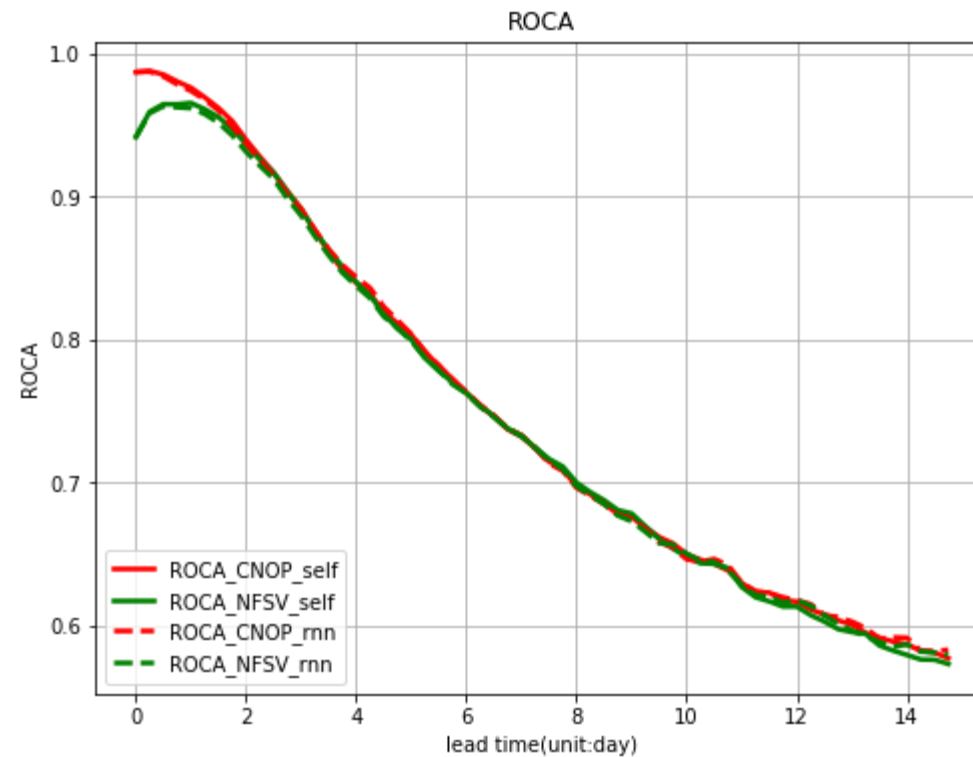
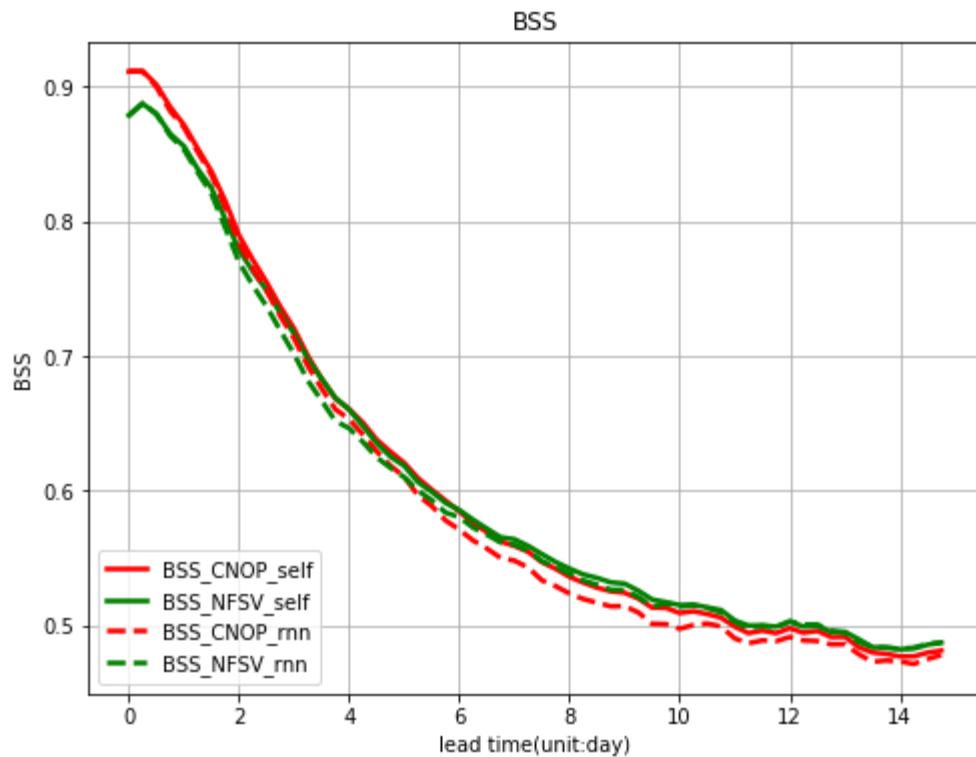
## 3.2 Results and comparison-RNN



From the comparison of RMSE/SPRD, the O-CNOPs ensemble forecast with optimization algorithm is more reliable than ensemble forecast with RNN, but from the comparison of RMSE and ACC, the ensemble forecast with RNN is acceptable.



## 3.2 Results and comparison-RNN



From the comparison of BSS and ROCA, the ensemble forecast with RNN is acceptable.



## 4. Summary

- From numerical simulation experiments, the application of machine learning in ensemble forecast is not good enough but it can make up for drawback of high computational cost of O-CNOPs and O-NFSVs, and the results is acceptable.
- To combine machine learning with ensemble forecasting is only a preliminary attempt in our study, and further research is needed.



# References

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