

Numerical modeling of seismically-induced slope displacements: a comparison between 2D and 3D finite difference models and Newmark-Displacements



Gisela Domej (presenting)

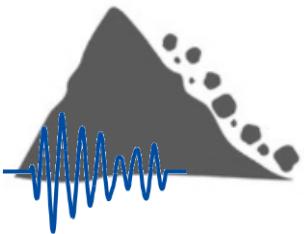
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Target question:



Which slope response is caused by different seismic scenarios?

Let's test in 2D and 3D with FDM and 11 earthquakes ...

... and compare to Newmark!

- Domej G., Bourdeau C., **2020**. Seismically-induced landslide displacements: a comparison between numerical models in 2D and 3D and the Newmark Method. *Article in preparation*.
- Domej G., Bourdeau C., Lenti L., Martino S., Semblat J. F., 2019. Assessing seismically induced slope deformation of the Diezma Landslide via limit equilibrium analysis and numerical modeling. In: Silvestri F., Moraci N. (Eds.). Earthquake Geotechnical Engineering for Protection and Development of Environment and Constructions - Proceedings of the 7th International Conference on Earthquake Geotechnical Engineering (ICEGE 2019), CRC Press, London, p. 2166-2173.
- Domej G., Bourdeau C., Lenti L., Martino S., Semblat J. F., 2019. Assessing seismically induced slope deformation of the Diezma Landslide via limit equilibrium analysis and numerical modeling. Talk. 7th International Conference on Earthquake Geotechnical Engineering (7ICEGE), Italian Geotechnical Society, Rome.
- Domej G., 2018. Seismically induced effects and slope stability in urbanized zones by numerical modeling. Doctoral Thesis, Université Gustave Eiffel (ex: Université Paris-Est & IFSSTAR), 266 p.

Which landslide to choose as case study and why?



Diezma Landslide

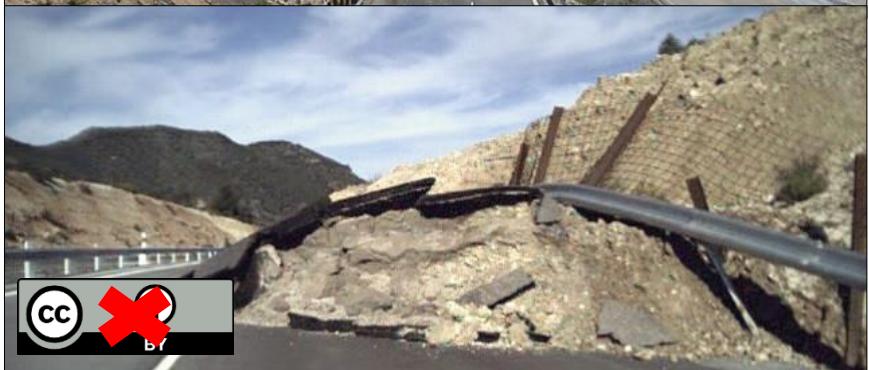
- 25 km NE of Granada, Spain
- translational (11°), 500 m, $1.2 \cdot 10^6 \text{ m}^3$
- so far no reported seismic trigger

1) location:

seismic region

at the A-92 motorway (vibrations)

Which landslide to choose as case study and why?



Diezma Landslide

- 25 km NE of Granada, Spain
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- so far no reported seismic trigger

1) location:

seismic region

at the A-92 motorway (vibrations)

2) activity:

since 1990

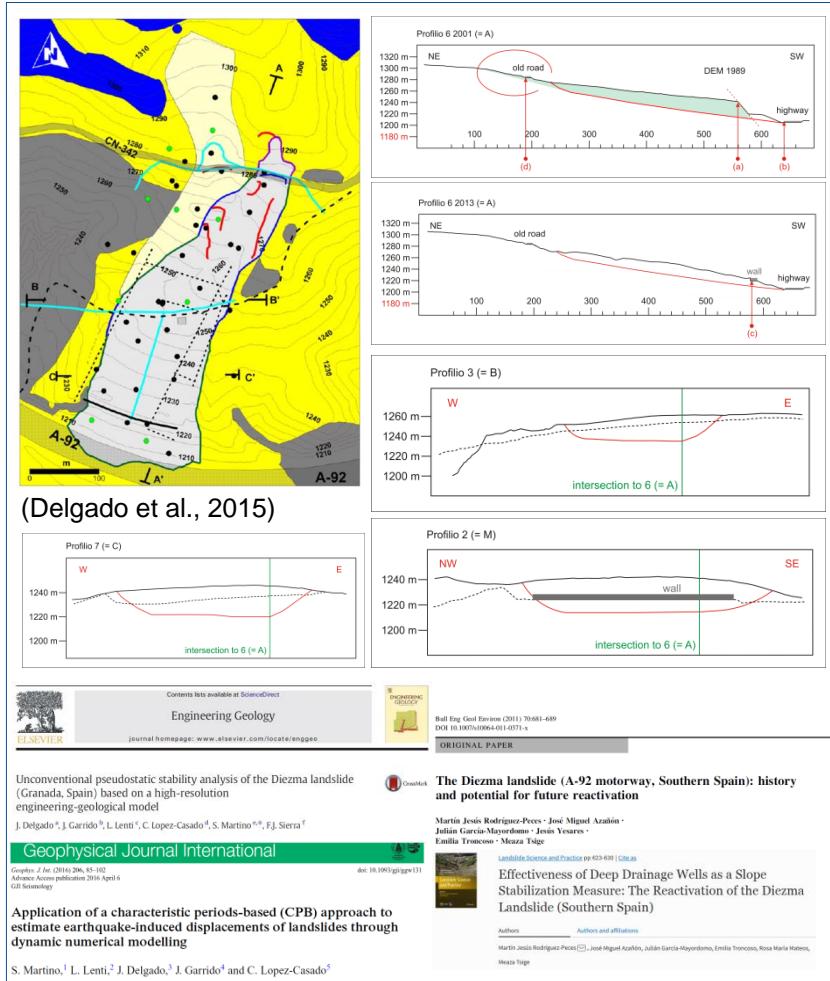
18th of March 2001, after rain event

(particular courtesy: Junta de Andalucía, 2001)

Which landslide to choose as case study and why?



Which landslide to choose as case study and why?



Diezma Landslide

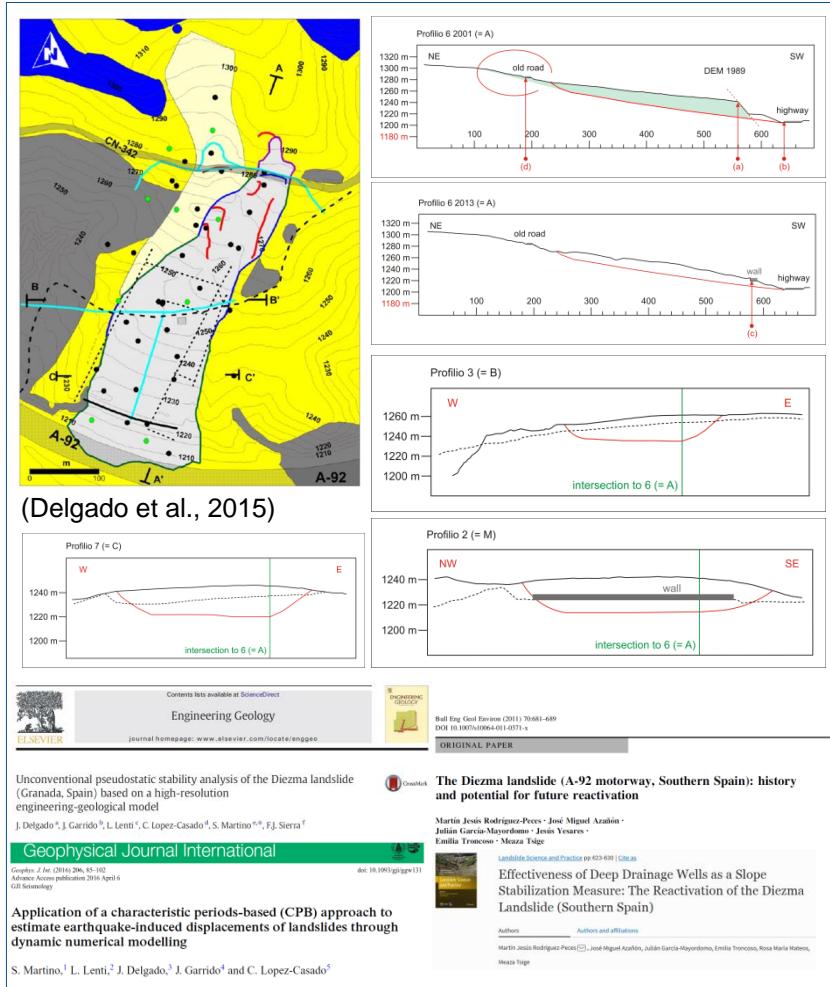
- 25 km NE of Granada, Spain
- translational (11°), 500 m, $1.2 \cdot 10^6 \text{ m}^3$
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3) documentation:

completeness of survey chart (71%)
geology / geotechnics / chronology

- | | |
|------------------------|--------|
| Azañon et al. | (2010) |
| Delgado et al. | (2015) |
| Martino et al. | (2016) |
| Rodríguez-Peces et al. | (2011) |

Which landslide to choose as case study and why?



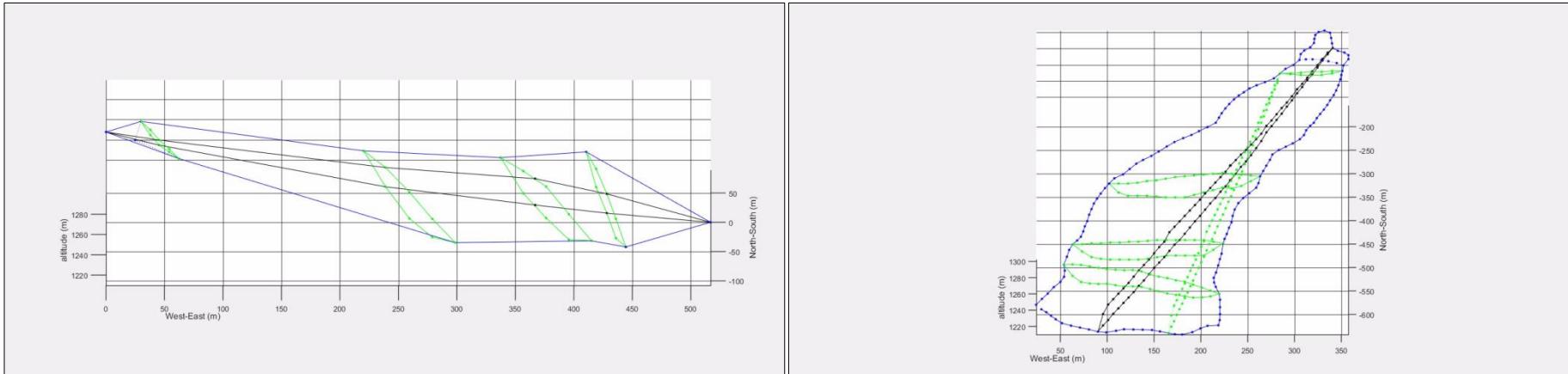
Diezma Landslide

- 25 km NE of Granada, Spain
- translational (11°), 500 m, $1.2 \cdot 10^6 \text{ m}^3$
- so far no reported seismic trigger

4) parameters:
 material (plastic clay, silt, marl, blocks)
 mechanism (drainage, permeability)

parameter	γ (kN/m ³)	γ_{sat} (kN/m ³)	c_{peak} (kPa)	c_{res} (kPa)	Φ_{peak} (°)	Φ_{res} (°)	v_s (m/s)	v (-)
landslide	19.0	21.4	46.0	4.0	26.0	12.0	300	0.25
bedrock	18.2	20.6	05.4	0.6	31.0	11.0	750	0.35

Creating 3D and 2D models in two versions: simple and fine geometries

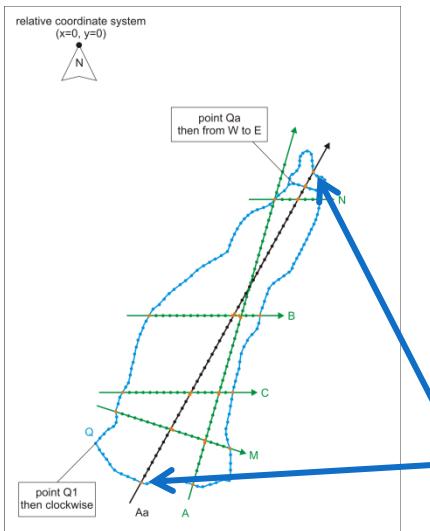


simple 3D geometry:

- 1 LCS (Aa)
- 4 TCS (N, B, C, M)
- 1 trace (Q - **10 points only**)

simple 2D geometry:

- 1 LCS (Aa - **10 points only**)



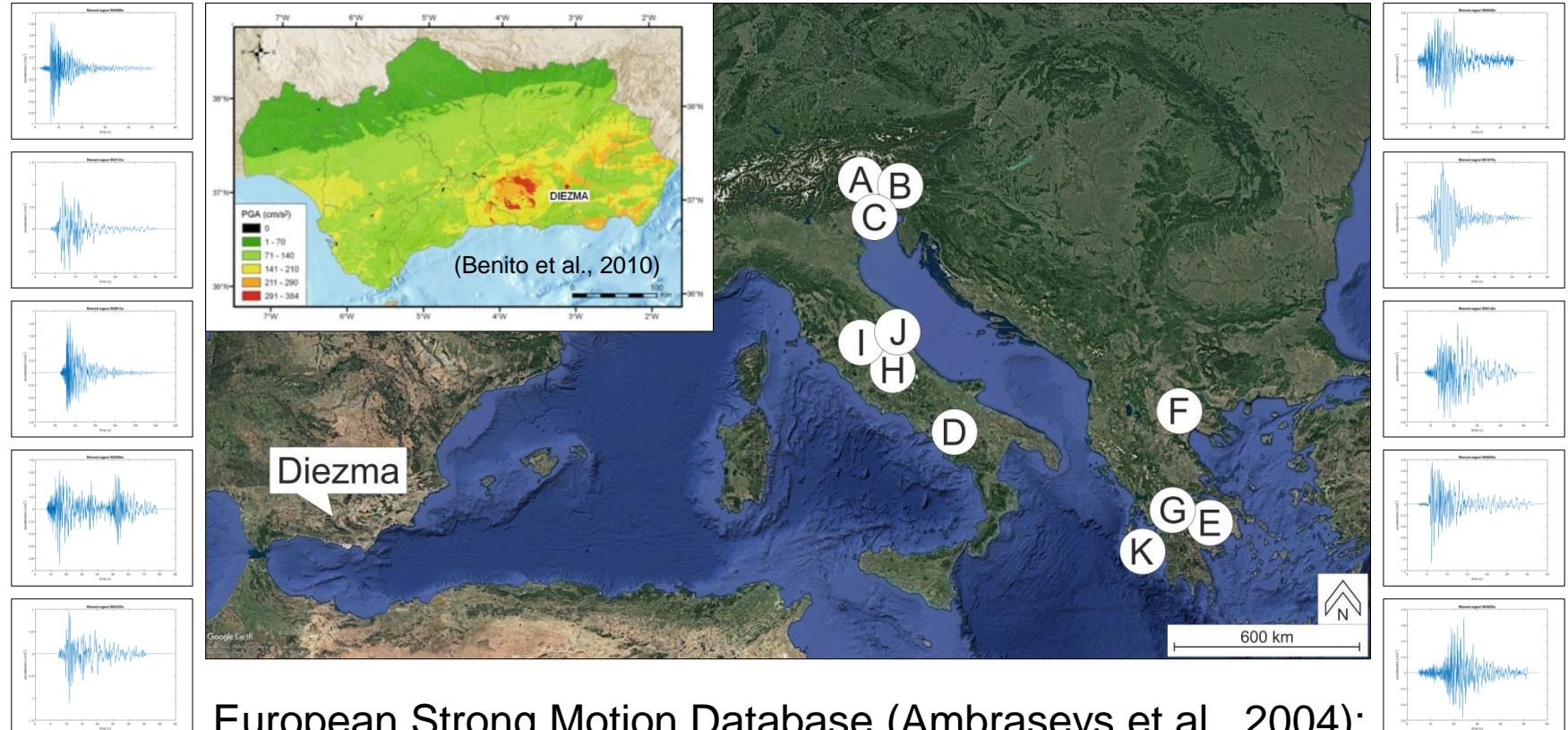
fine 3D geometry:

- 2 LCS (A, Aa)
- 4 TCS (N, B, C, M)
- 1 trace (Q - **1 point/10 m**)

fine 2D geometry:

- 1 LCS (Aa - **1 point/10 m**)

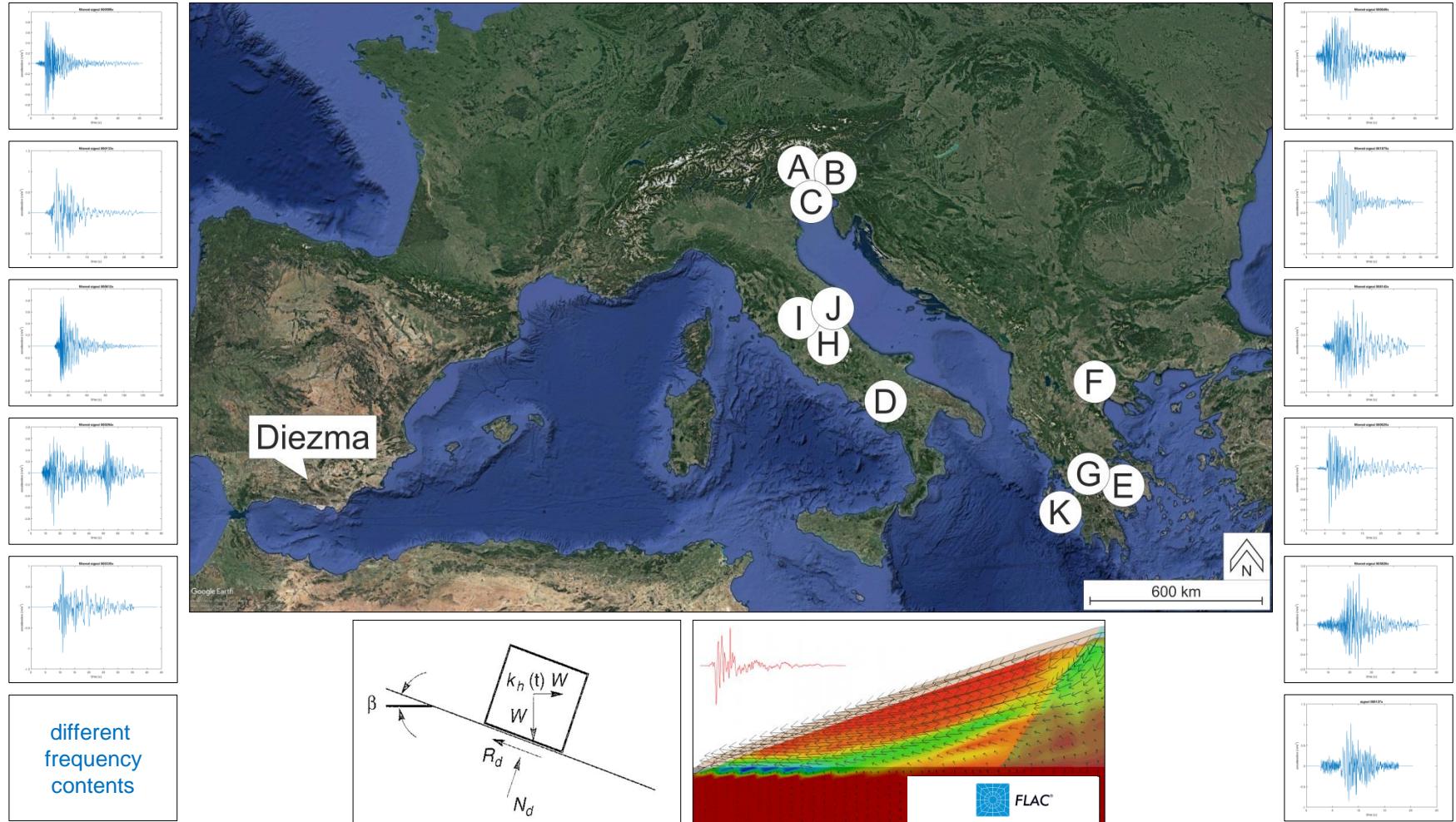
Choosing seismic scenarios that represent the seismicity of Southern Spain



European Strong Motion Database (Ambraseys et al., 2004):

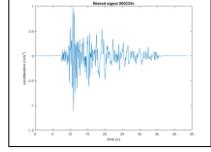
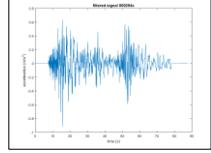
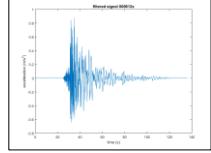
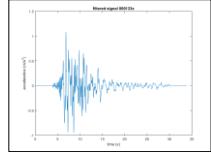
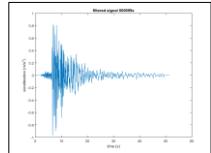
- horizontal components
- $M_W = 5.0\text{--}7.0$
- $AI = 0.1\text{--}1.0 \text{ m/s}$
- $\text{PGA} = 0.8\text{--}1.2 \text{ m/s}^2$

Use these signals for the Newmark-Method (1965) and FDM



Newmark-Method (1965) & finite difference method (after Kramer, 1996; ITASCA, 2015)

Use these signals for the Newmark-Method (1965) and FDM



different frequency contents

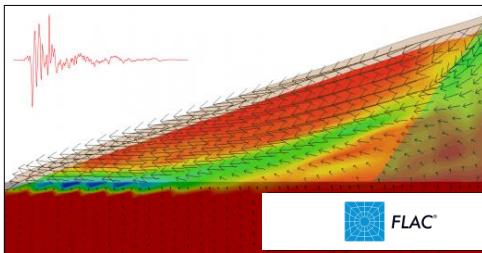
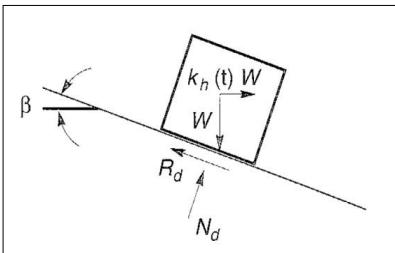
1) analysis of seismically induced displacements

2) comparison of method performance and their applicability

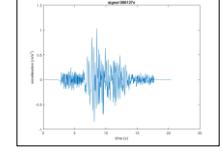
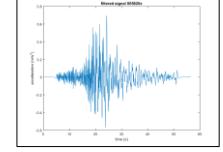
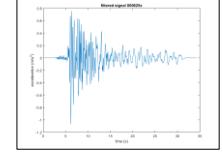
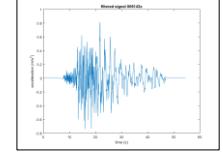
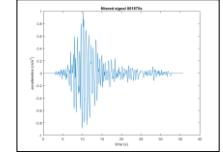
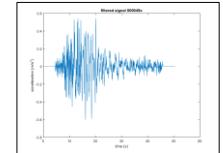
2D
simple
geometry



2D & 3D
simple & fine
geometries



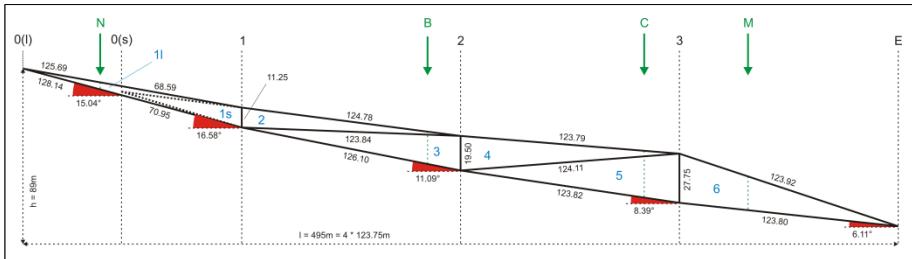
Newmark-Method (1965) & finite difference method (after Kramer, 1996; ITASCA, 2015)



Running Newmark-Models (1965)

Newmark-Method (1965):

- non-numerical method
- pseudostatic limit equilibrium analysis
- dynamic performance of slopes in 2D
- aspects of safety factor & 1 estimation

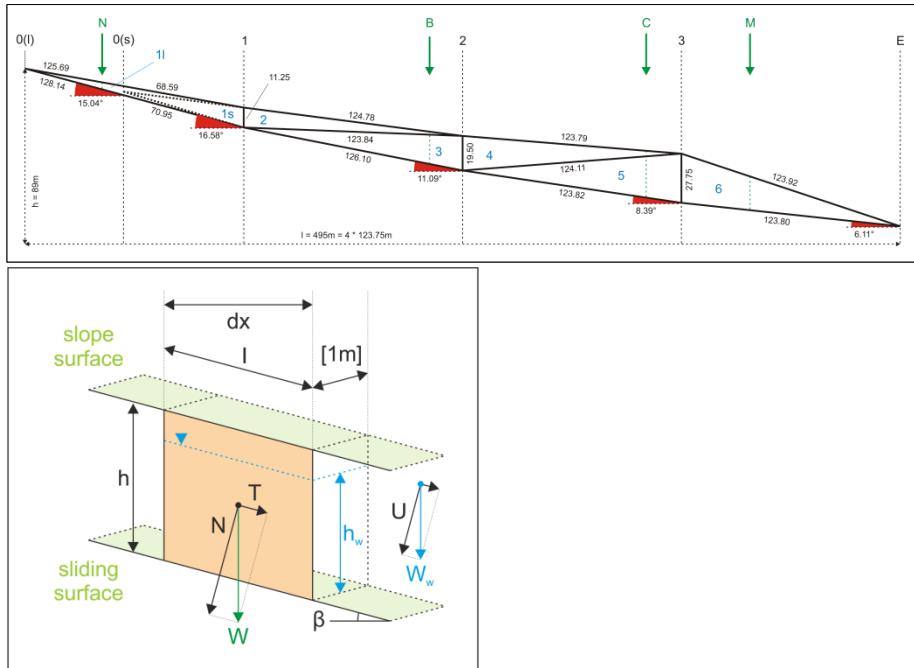


Running Newmark-Models (1965)

Newmark-Method (1965):

- non-numerical method
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- aspects of safety factor & 1 estimation
- rigid block on an inclined plane
(Mohr-Coulomb Criterion)

$$SF = \frac{c' \cdot \frac{dx}{\cos(\beta)} \cdot 1 + \left(N - u \cdot \frac{dx}{\cos(\beta)} \cdot 1 \right) \cdot \tan(\Phi')}{W \cdot \sin(\beta)} = \frac{\text{holding}}{\text{driving}}$$



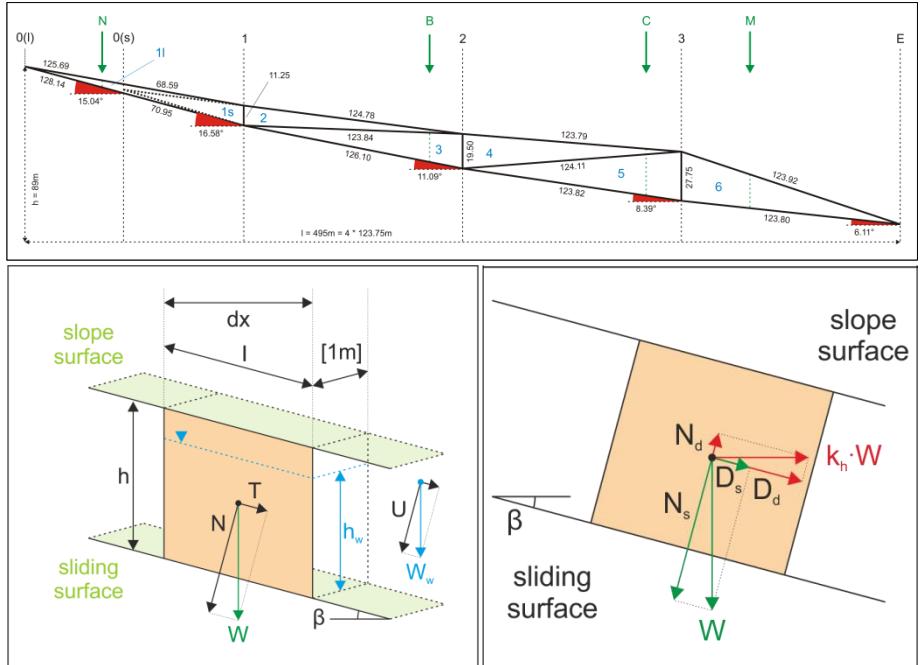
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(Mohr-Coulomb Criterion)

$$SF = \frac{c \cdot \frac{dx}{\cos(\beta)} \cdot 1 + (N - k_h \cdot W \cdot \sin(\beta)) \cdot \tan(\Phi)}{W \cdot \sin(\beta) + k_h \cdot W \cdot \cos(\beta)} = \frac{\text{holding}}{\text{driving}}$$

- representation of earthquake as additional horizontal force in equation
- assumes displacement when SF = 1
- deducts $a_{\text{crit}} (= k_h \cdot g)$ to overcome



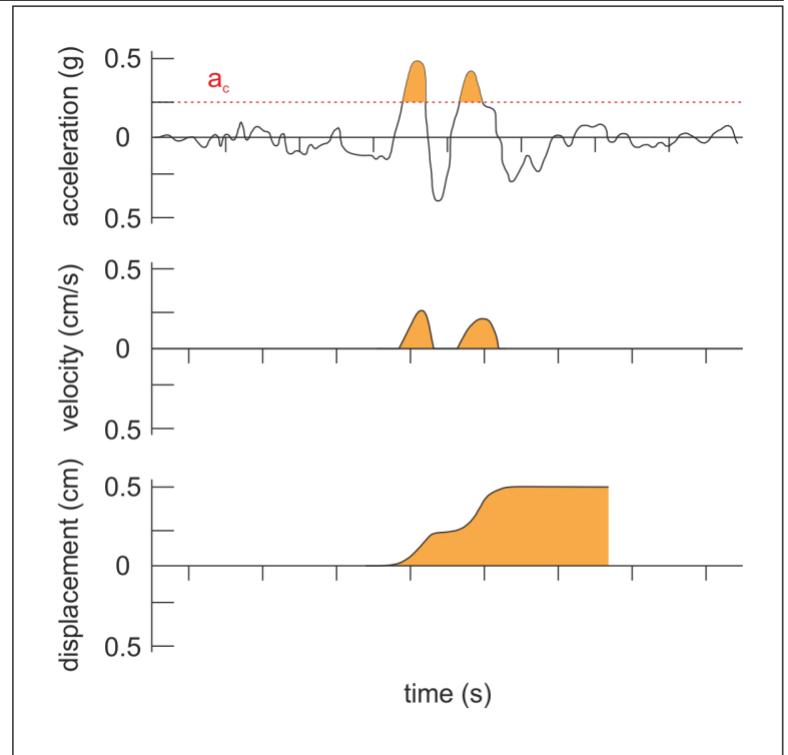
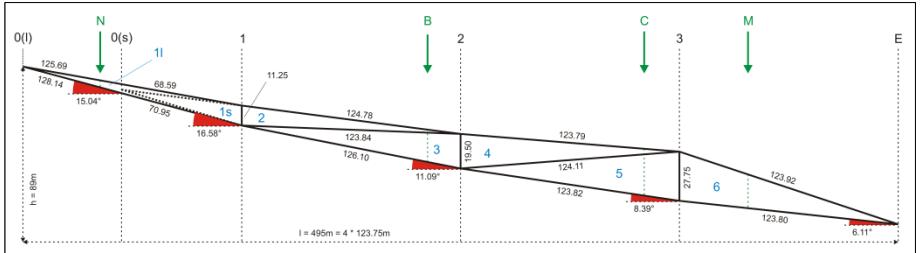
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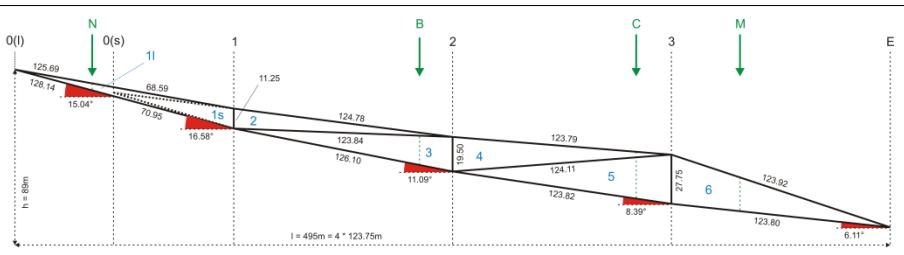
- representation of earthquake as additional horizontal force in equation
- assumes displacement when SF = 1
- deducts $a_{\text{crit}} (= k_h \cdot g)$ to overcome
- SLAMMER (Jibson et al., 2013)



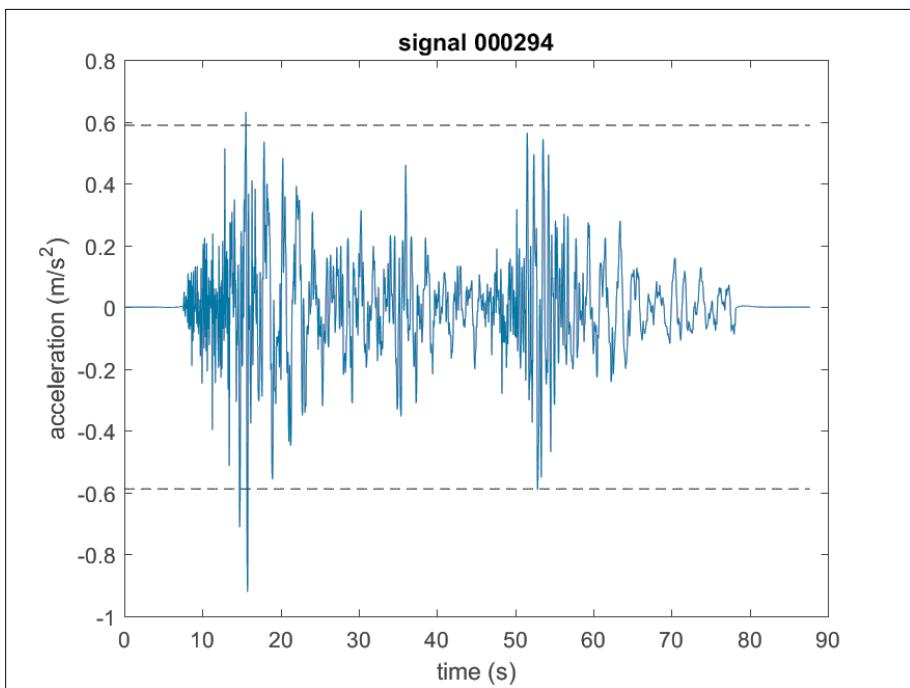
Running Newmark-Models (1965)

Application to the Diezma Landslide:

- threshold, frequency content, duration
- macro-seismic / landslide parameters
- site effects, confinement, deformation



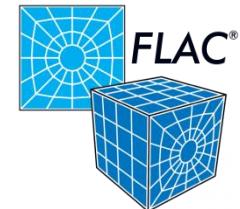
signal	normal d_{cum} (cm)	inverse d_{cum} (cm)
A – 000049	-	0.0002
B – 000133	0.3840	0.3510
C – 000127	0.1201	0.0323
D – 000294	0.0038	0.3254
E – 000335	0.5309	0.3699
F – 001875	1.4084	1.1590
G – 006142	0.2138	0.0490
H – 000599	0.1284	0.3034
I – 000612	0.1488	0.0020
J – 000625	0.0488	0.3534
K – 005820	0.0565	-



Running FDM-Models

Finite Difference Method:

- numerical method (time domain)
- dynamic performance of slopes in 2D & 3D
- visco-elasto-perfectly-plastic material behavior
- 1 estimation per point

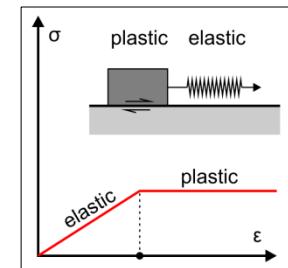
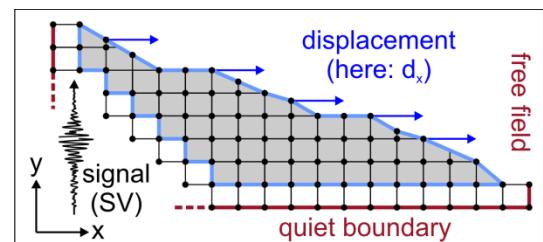


Running FDM-Models

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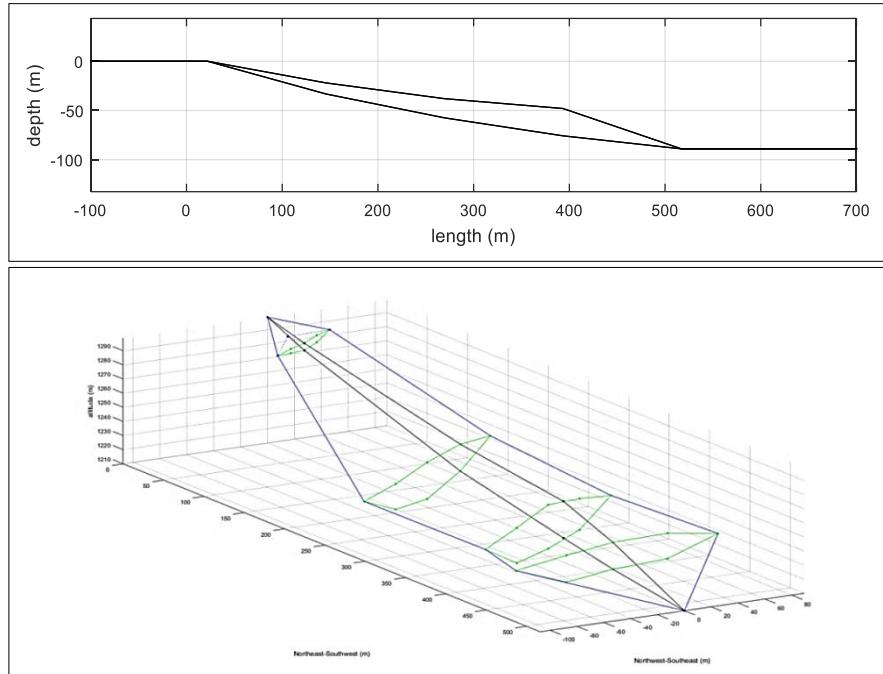
- geotechnical analysis
- finite number of grid points
- stress-strain-application (finite difference equations)
- solve for d (here: d_{res})
- static part: settlement due to gravity
- dynamic part: response to seismic load (Mohr-Coulomb)



Running FDM-Models

Application to the Diezma Landslide:

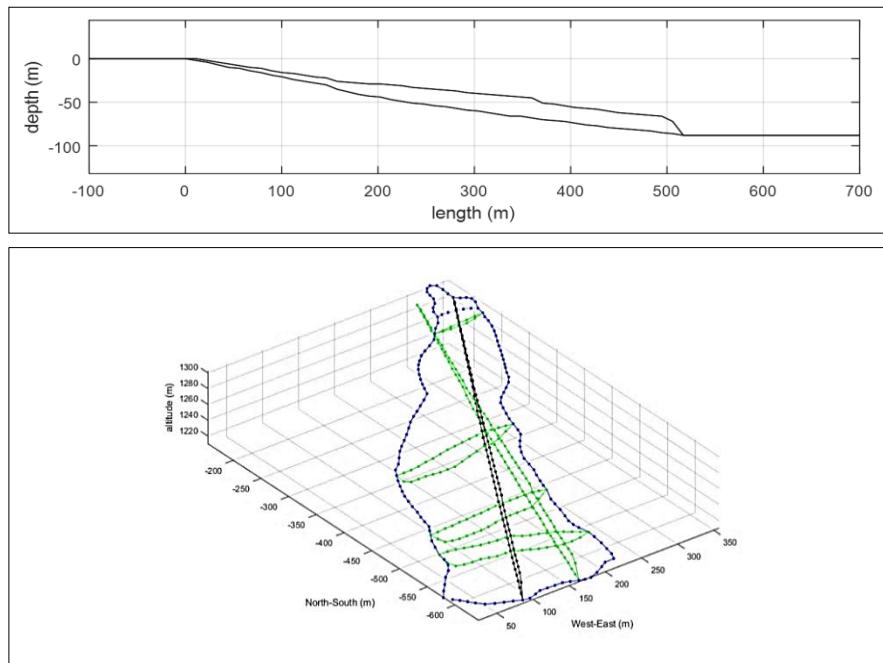
- geometry: **2D & 3D (simple & fine)**
- mesh: $2D \rightarrow 1\text{ m}$ (up to 30 Hz)
 $3D \rightarrow 3\text{ m}$ (up to 8 Hz)
- properties: $\rho = 2181.4\text{ kg/m}^3$
 $v = 0.25 (-)$
(landslide) $v_s = 300\text{ m/s}$
 $c' = 46 \cdot 10^3\text{ Pa}$
 $\Phi' = 26^\circ$
- boundaries: quiet at model base, free field at model sides
- loading: 11 signals (SV vertically to model base \rightarrow horizontal shear)



Running FDM-Models

Application to the Diezma Landslide:

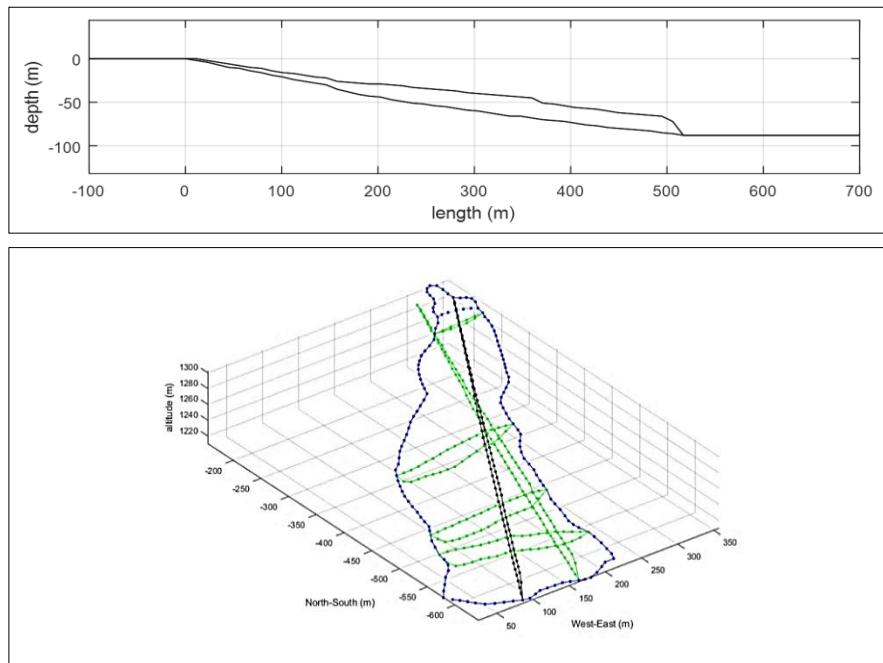
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Running FDM-Models

Application to the Diezma Landslide:

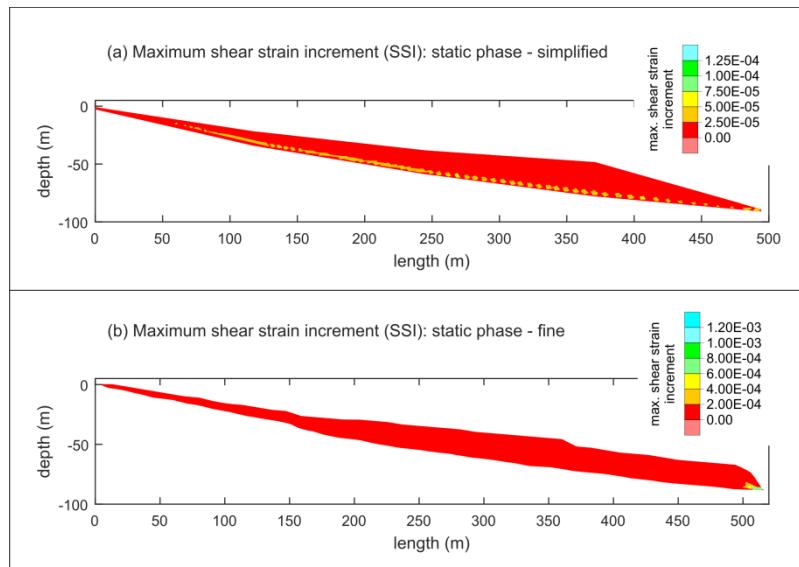
- geometry: **2D & 3D** (simple & **fine**)
- mesh: $2D \rightarrow 1\text{ m}$ (up to 30 Hz)
 $3D \rightarrow 3\text{ m}$ (up to 8 Hz)
- properties: $\rho = 2500\text{ kg/m}^3$
 $v = 0.35 (-)$
(bedrock) $v_s = 1000\text{ m/s}$
 $c' = 4 \cdot 10^9\text{ Pa}$
 $\Phi' = 30^\circ$
- boundaries: quiet at model base, free field at model sides
- loading: 11 signals (SV vertically to model base \rightarrow horizontal shear)



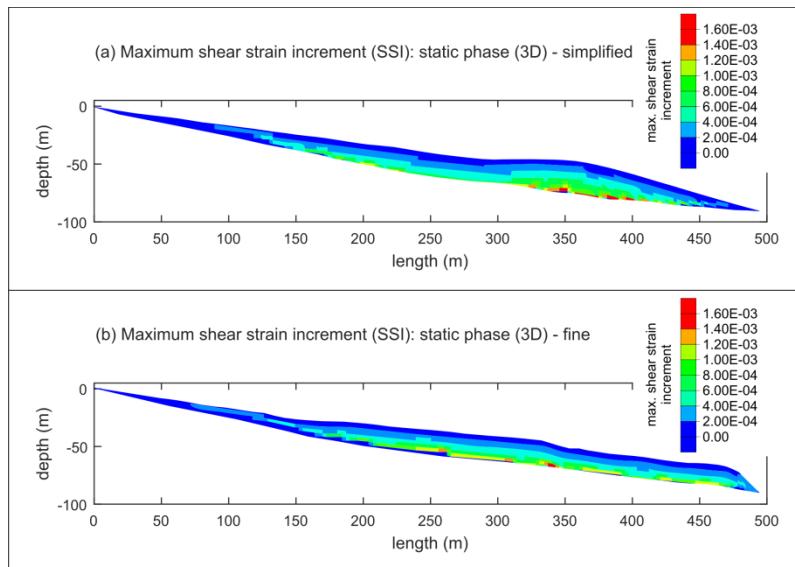
Running FDM-Models

static phases

2D



3D



simple
fine

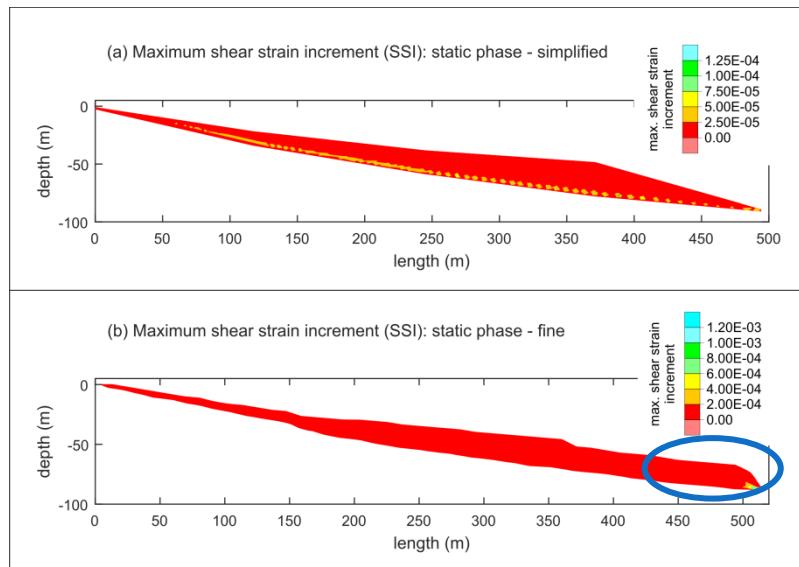
simple
fine

- settling due to gravity → stability without external loads
- maximum SSI → concentration of shear strain

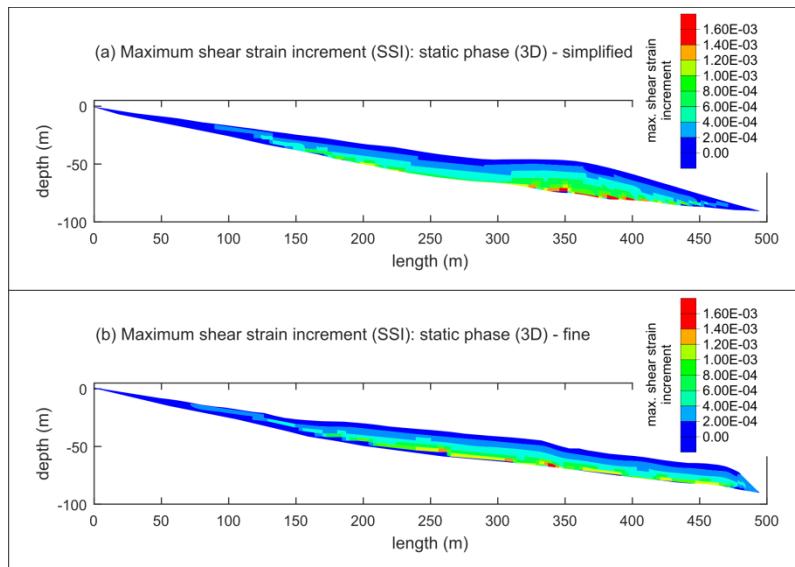
Running FDM-Models

static phases

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3D



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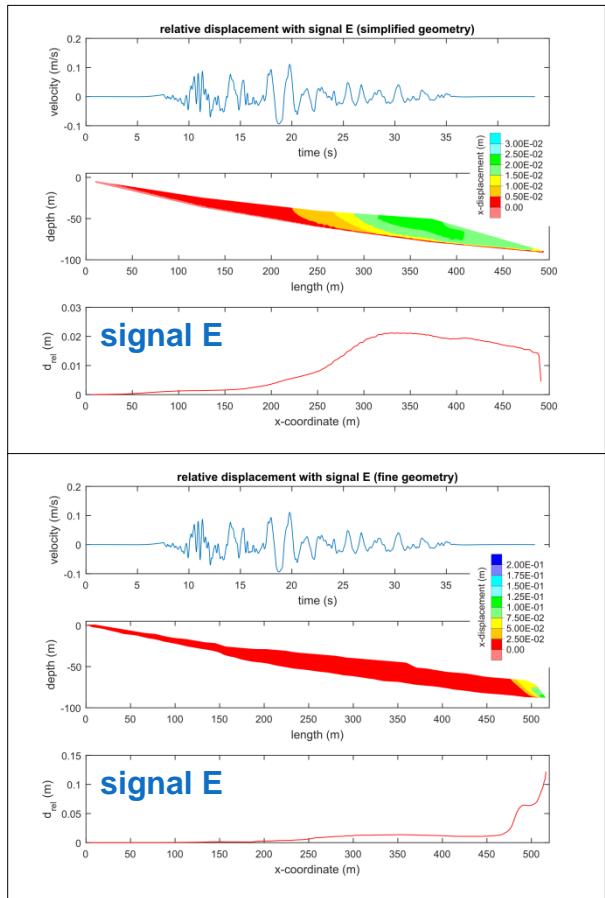
simple
fine

- settling due to gravity → stability without external loads
- maximum SSI → concentration of shear strain
- different static behavior → different dynamic behavior

Running FDM-Models

simple

2D



fine

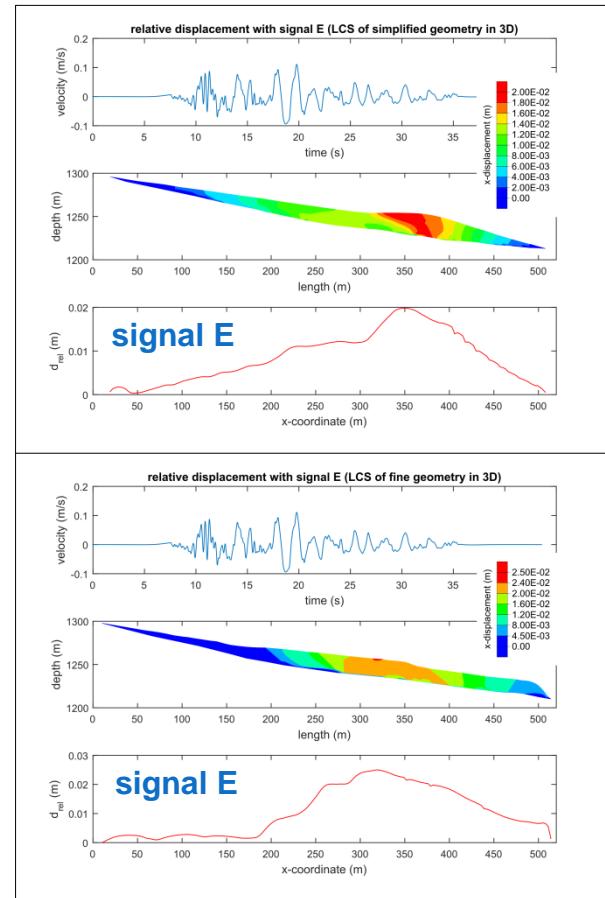
dynamic phases

slope response
relative to bedrock

qualitative:

quantitative:

3D



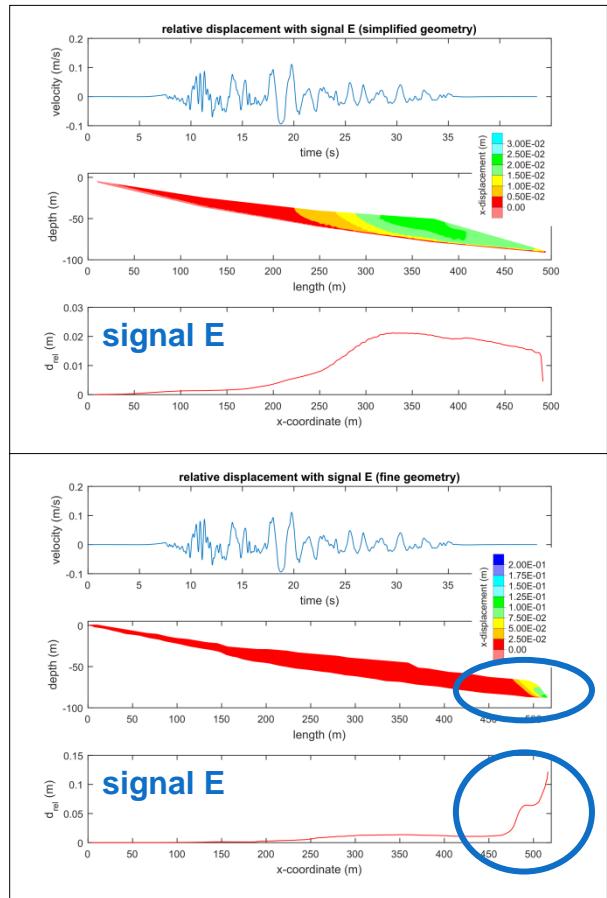
simple

fine

Running FDM-Models

simple

2D



fine

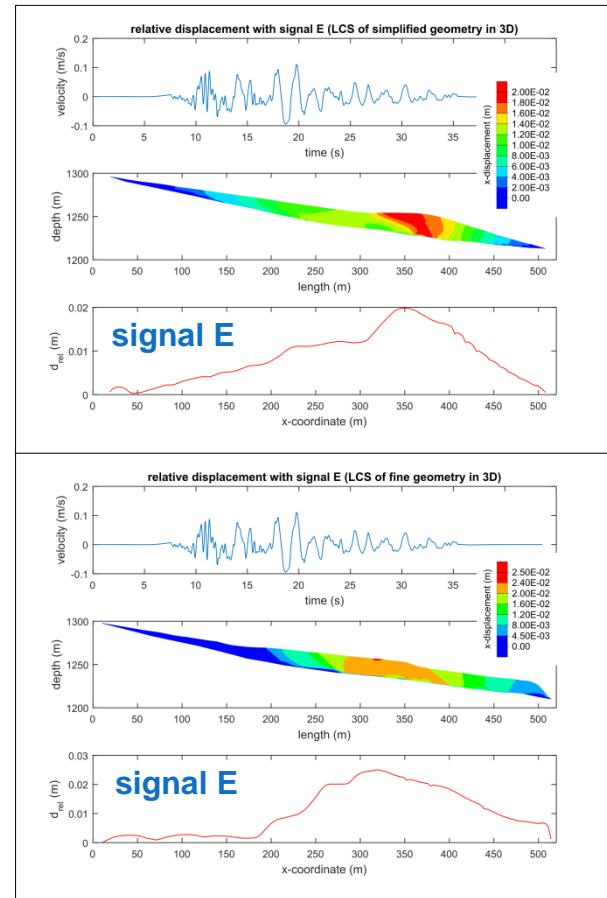
dynamic phases

slope response
relative to bedrock

qualitative:
geometry

quantitative:

3D



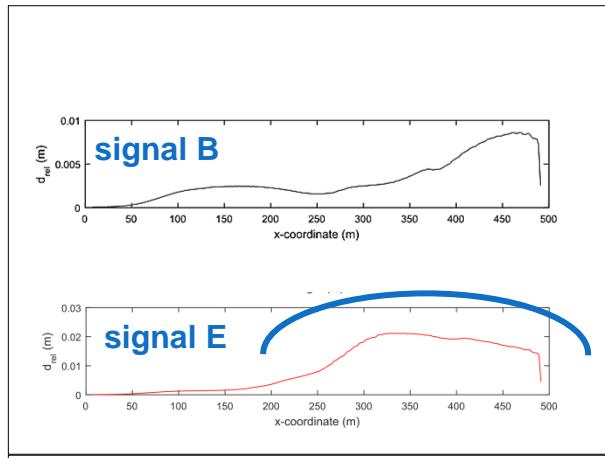
simple

fine

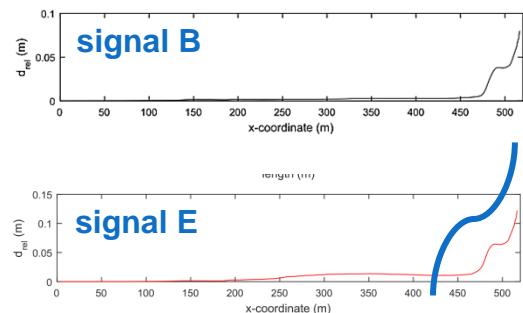
Running FDM-Models

simple

2D



fine



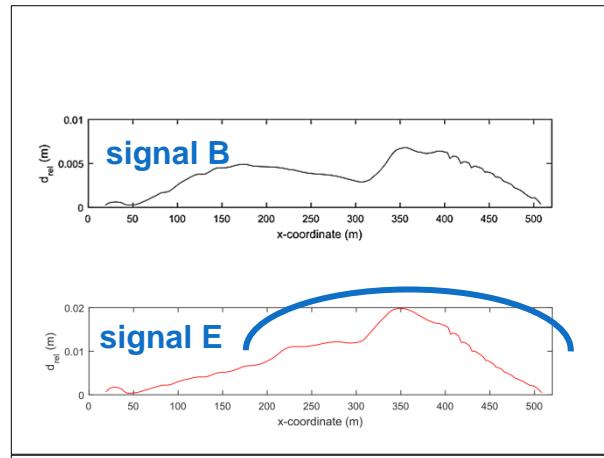
dynamic phases

slope response
relative to bedrock

qualitative:
geometry
signal

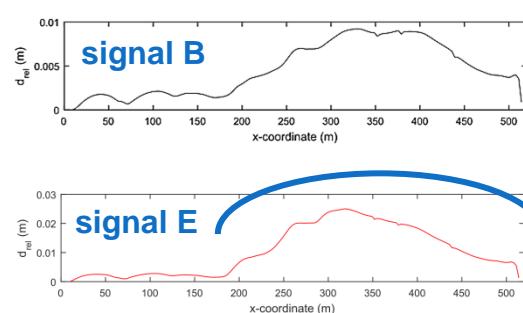
quantitative:

3D



simple

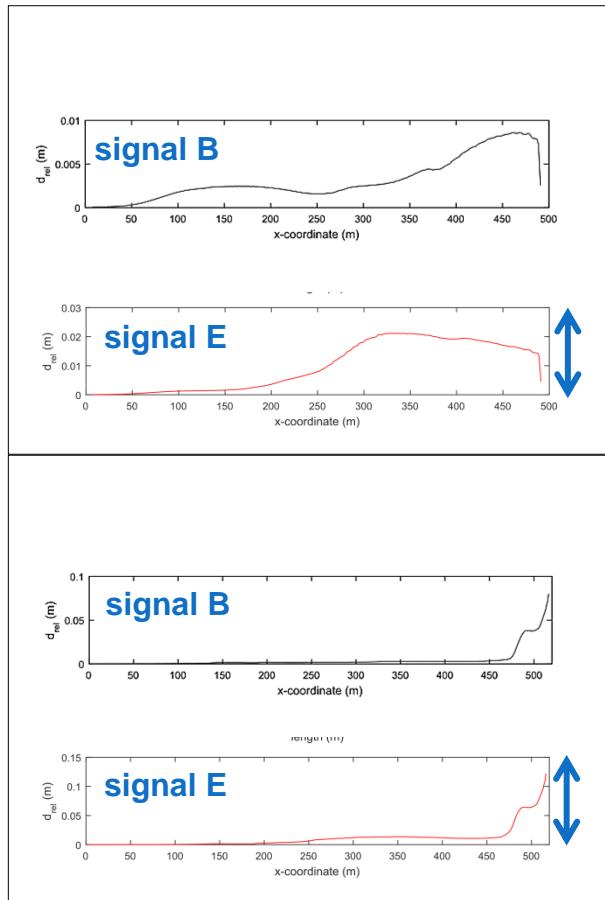
fine



Running FDM-Models

simple
fine

2D



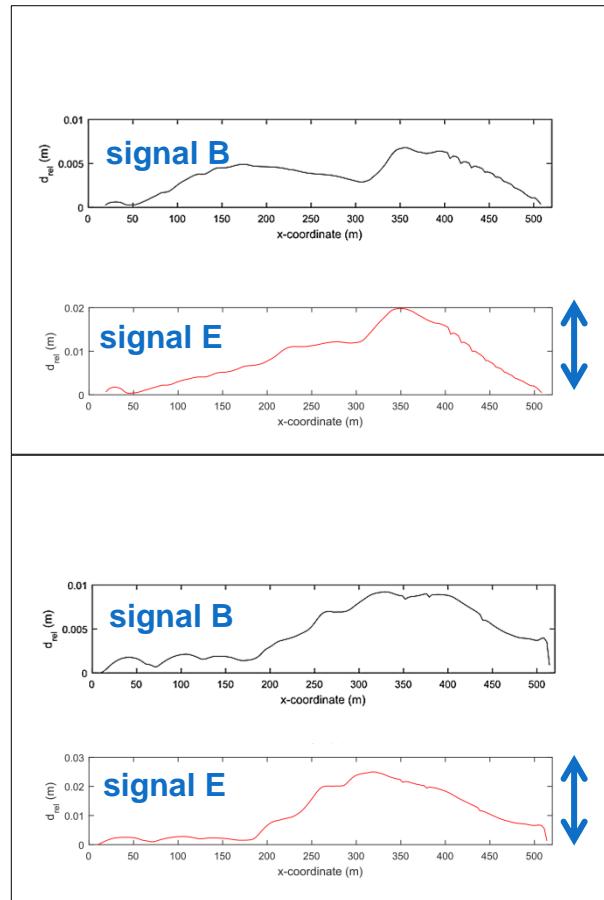
dynamic phases

slope response
relative to bedrock

qualitative:
geometry
signal

quantitative:
signal

3D

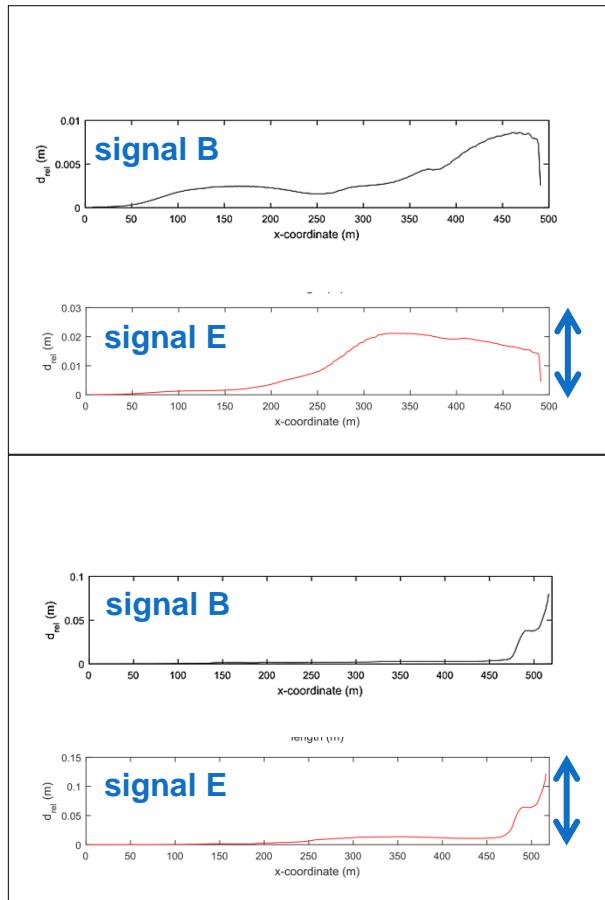


simple
fine

Running FDM-Models

simple

2D



dynamic phases

slope response
relative to bedrock

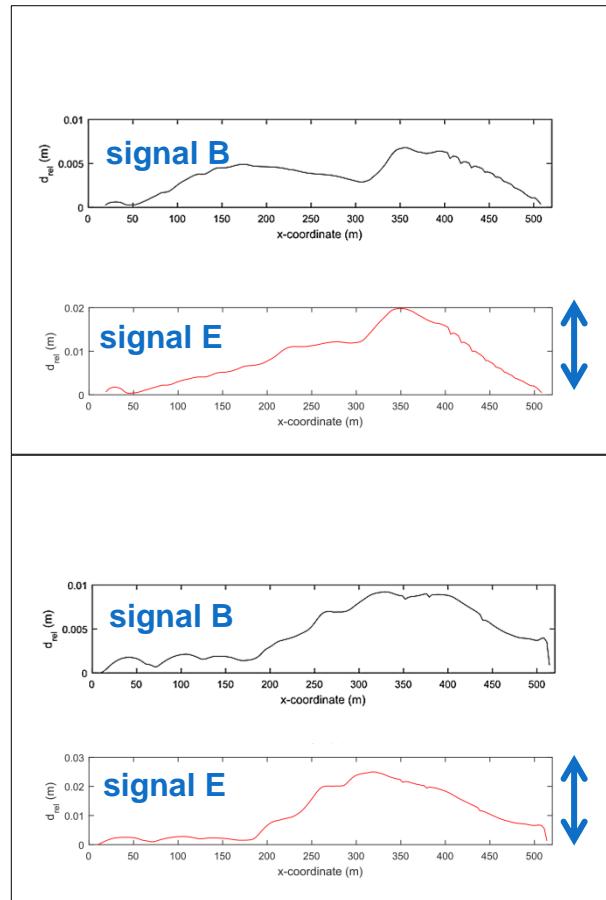
qualitative:
geometry
signal

quantitative:
signal

→ 2D fine geometry
not representative

fine

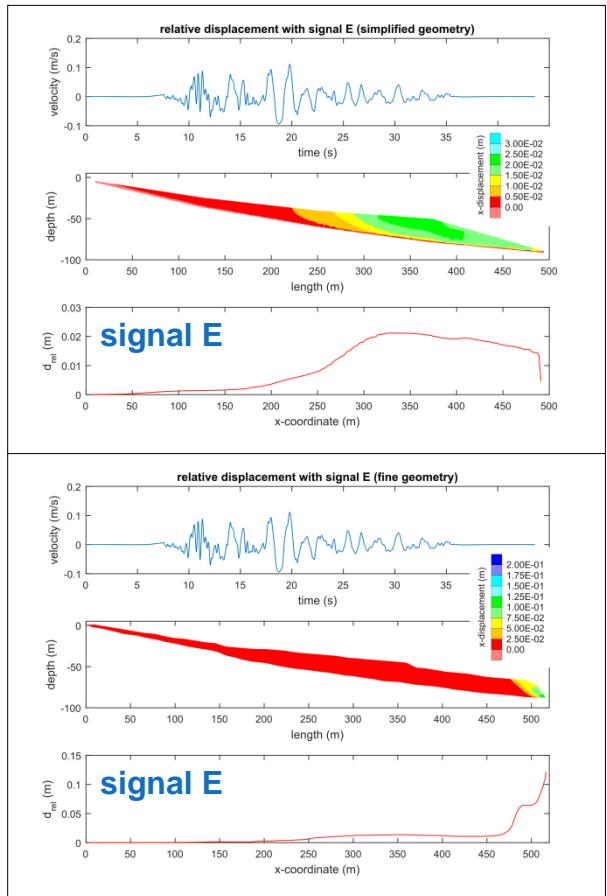
3D



Running FDM-Models

simple

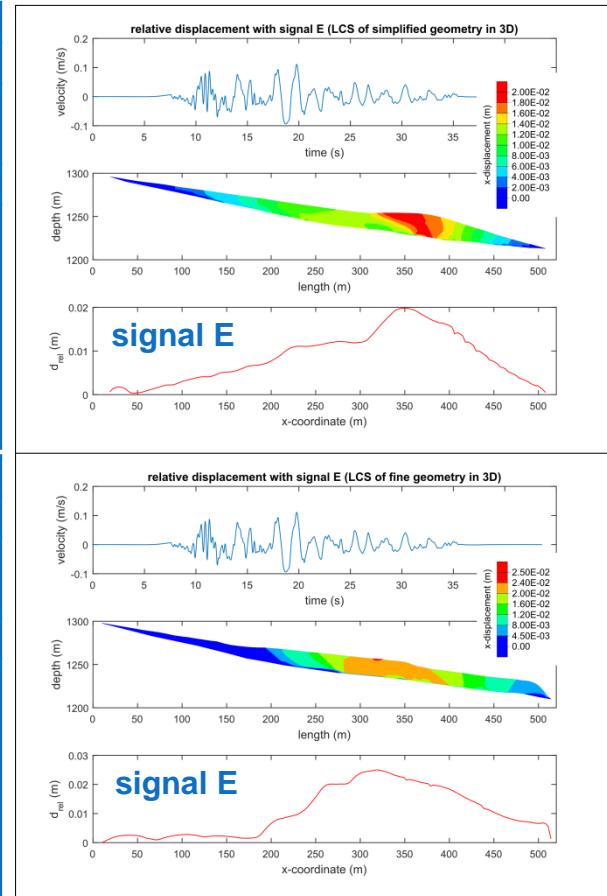
2D



maximum d_{res} (cm)

A	0.18
B	0.86
C	0.28
D	0.98
E	2.12
F	2.85
G	0.52
H	0.69
I	0.30
J	0.91
K	0.17

3D



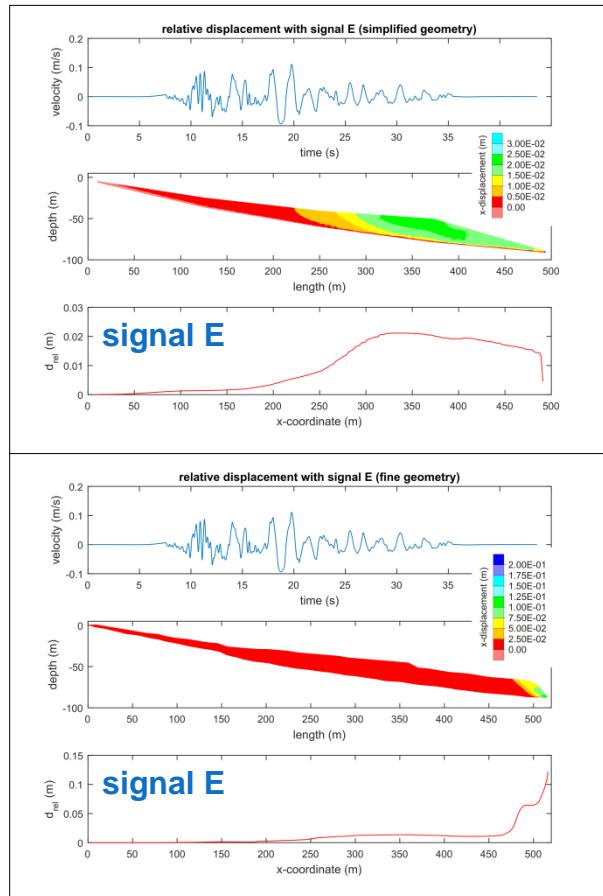
simple

fine

Running FDM-Models

simple

2D



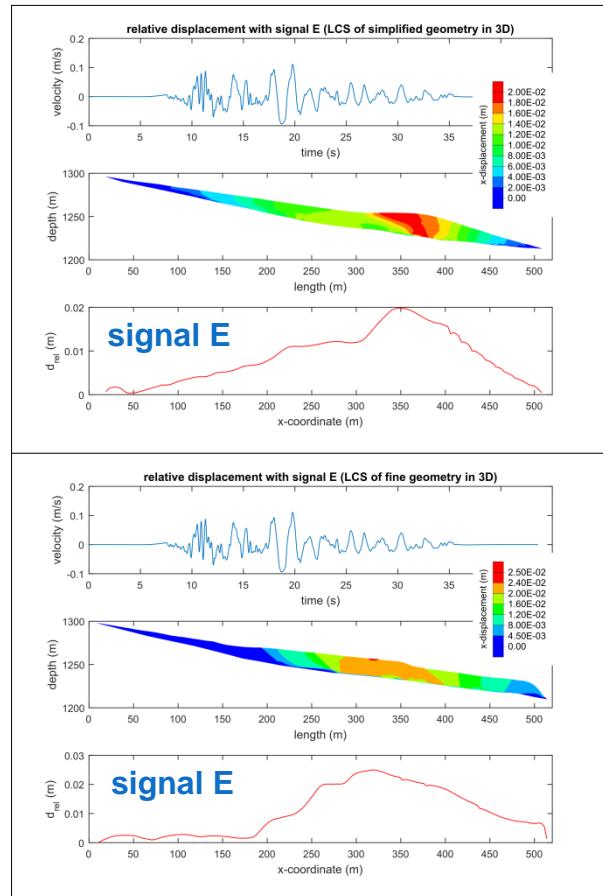
maximum d_{res} (cm)

A	0.18
B	0.86
C	0.28
D	0.98
E	2.12
F	2.85
G	0.52
H	0.69
I	0.30
J	0.91
K	0.17

factors 6 to 24

A	4.25
B	7.99
C	5.76
D	8.64
E	12.20
F	17.06
G	6.15
H	9.35
I	7.08
J	9.58
K	3.64

3D



simple

fine

Running FDM-Models

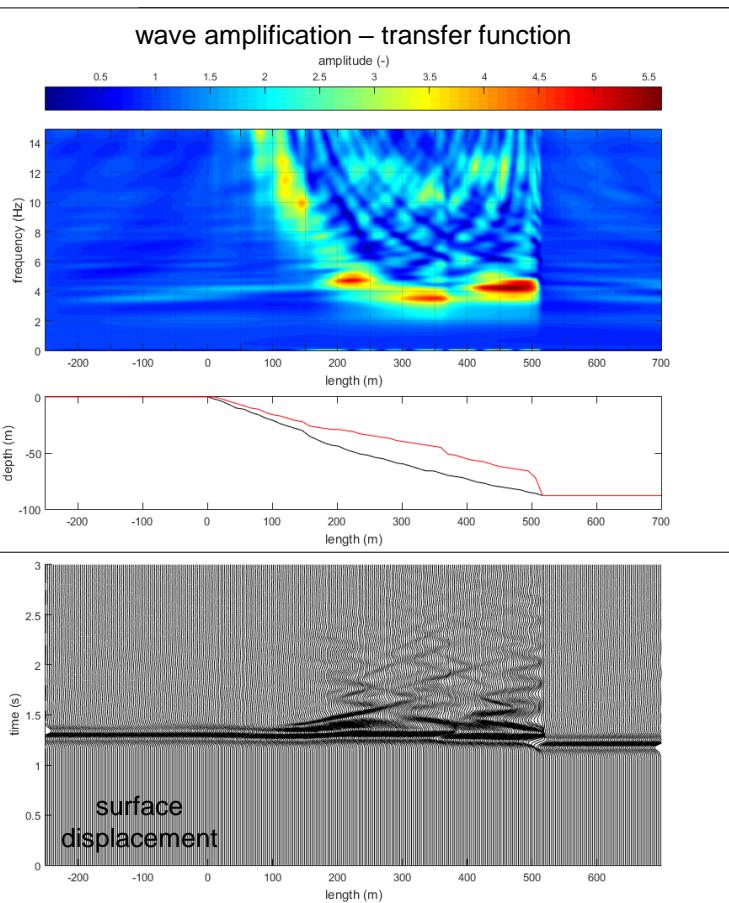
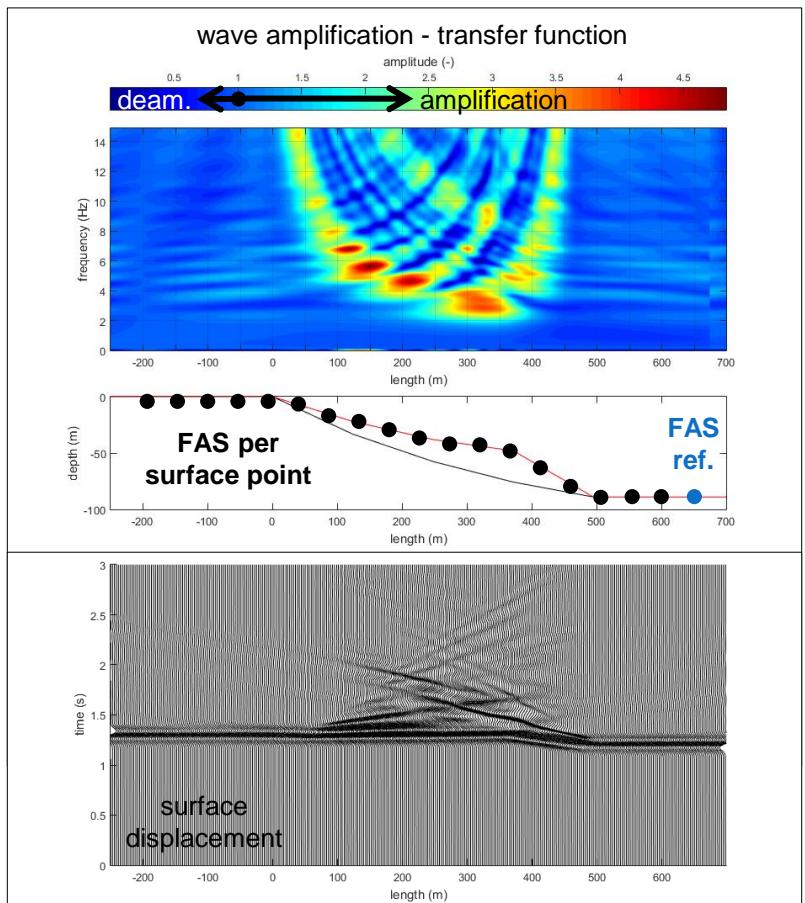
simple

2D

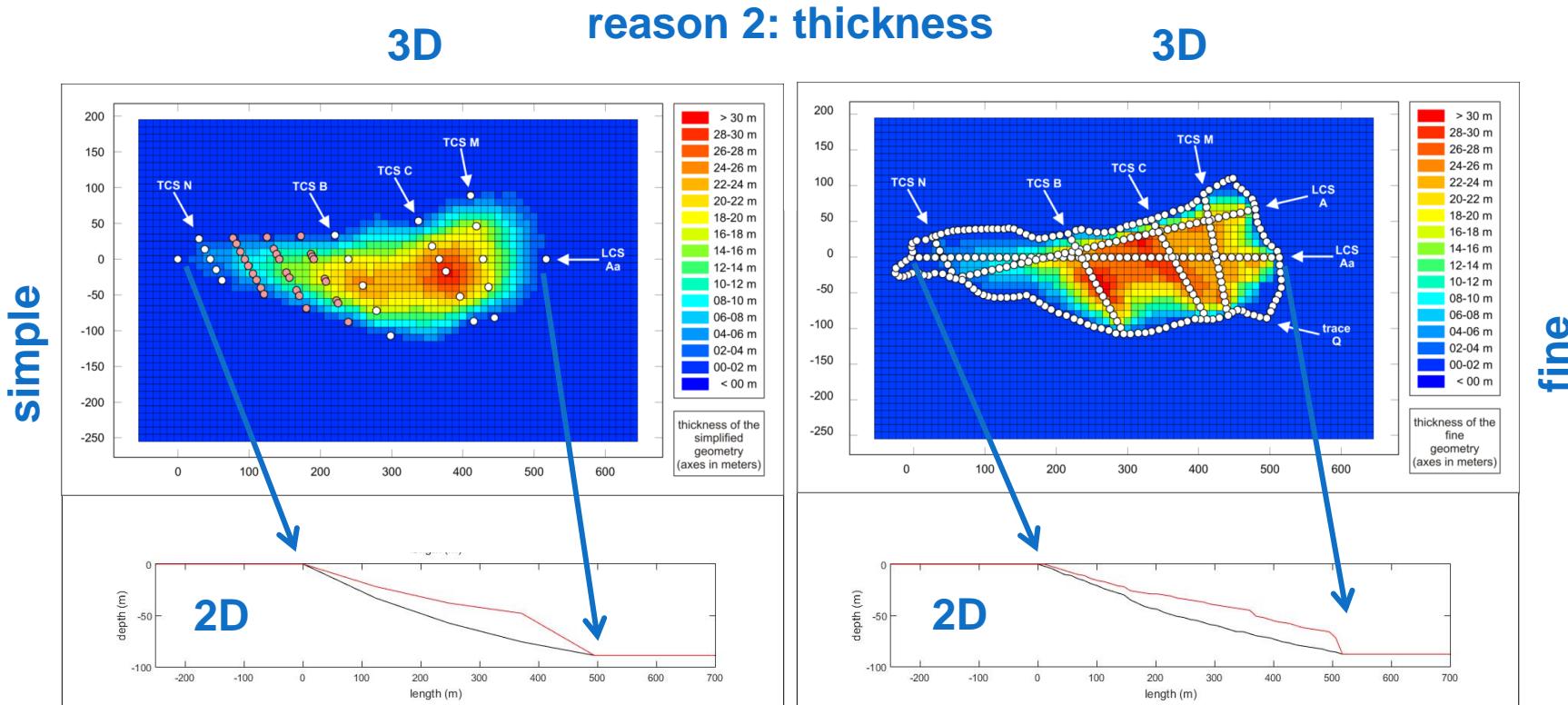
reason 1: site effects

2D

fine



Running FDM-Models



The 2D simple geometry seems much more representative for the entire landslide (in 3D) than the 2D fine geometry. It does not have such a steep toe all along!

Can we compare the two methods, and if yes how?

comparison of Newmark (1965) & FDM

method	geometry	input	signal	output	behavior	domain
Newmark (1965)	2D (simple)	W, I, c, Φ, β	acceleration time-histories	d_{cum} (1 value)	elasto-perfectly-plastic	(time related)
finite difference method	2D & 3D (simple & fine)	v_s, ρ, u, c', Φ' and as function thereof G, K	velocity time-histories	d_{res} (1 value per point)	visco-elasto-perfectly-plastic	time domain

NEWMARK (1965)

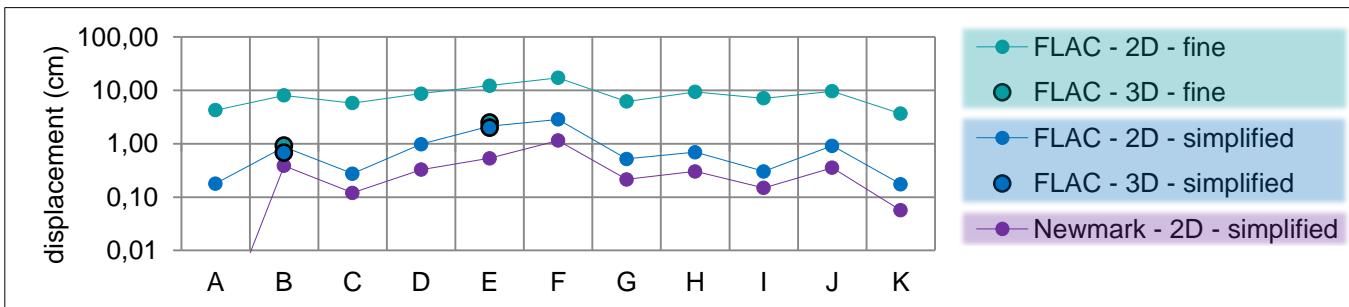
analysis with FDM

Can we compare the two methods, and if yes how?

comparison of Newmark (1965) & FDM

Signal	Newmark (1965) 2D simple	FDM 2D simple	FDM 2D fine	FDM 3D simple	FDM 3D fine
A	0.00	0.18	4.25		
B	0.38	0.86	7.99	0.68	0.92
C	0.12	0.28	5.76		
D	0.33	0.98	8.64		
E	0.53	2.12	12.20	1.99	2.50
F	1.15	2.85	17.06		
G	0.21	0.52	6.15		
H	0.30	0.69	9.35		
I	0.15	0.30	7.08		
J	0.35	0.91	9.58		
K	0.06	0.17	3.64		
average	0.33	0.90	8.34	1.33	1.71

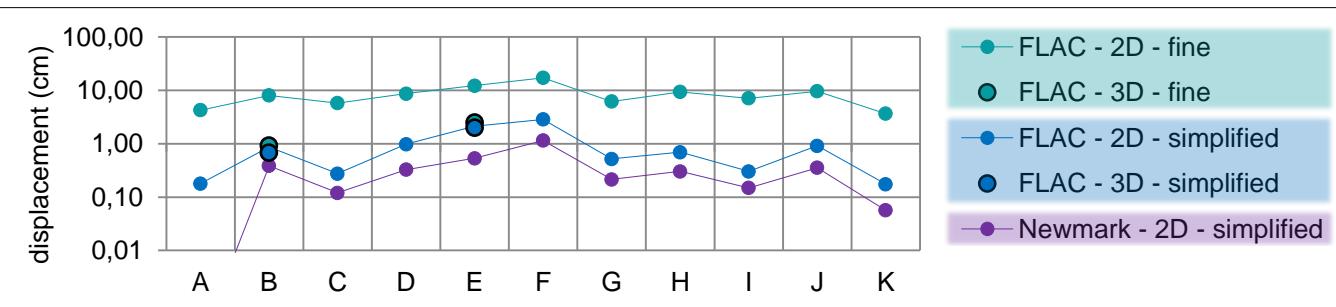
- max. value policy
- signal priority in 2D (FDM ≈ Newmark)
- all in cm-range
- factors 6-24 for models 2D/fine



Can we compare the two methods, and if yes how?

comparison of Newmark (1965) & FDM

Signal	Newmark (1965) 2D simple	FDM 2D simple	FDM 2D fine	FDM 3D simple	FDM 3D fine
A	0.00	0.18	4.25		
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- max. value policy
- signal priority in 2D (FDM ≈ Newmark)
- all in cm-range
- factors 6-24 for models 2D/fine

→ 3D is great!
 → fine models can be misleading
 → Newmark (1965) is better than we think

References

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- Kramer S. L., 1996. *Geotechnical Earthquake Engineering*. Prentice Hall, ed. ?, 653 p.

**Thank you for reading our display,
we look forward to chat with you
on Monday, May 4th, from 10:45 to 12:30!**

