

# A better strategy for interpolating gravity and magnetic data

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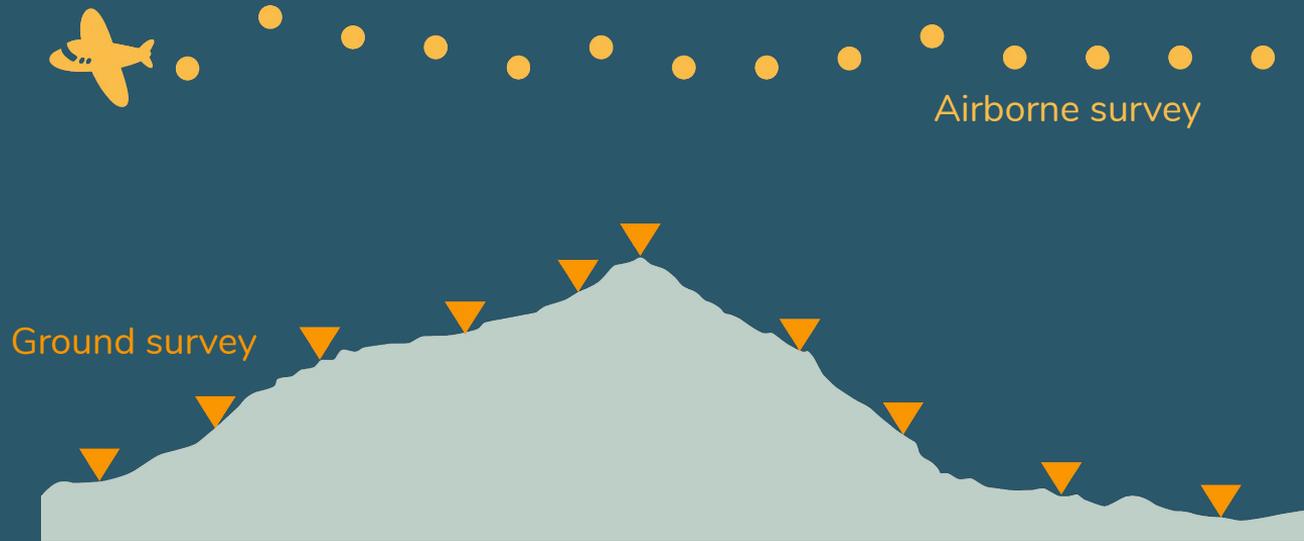
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# Gravity and magnetic data



- Above surface
- Irregular paths
- At different heights

# What do we know about gravmag data?

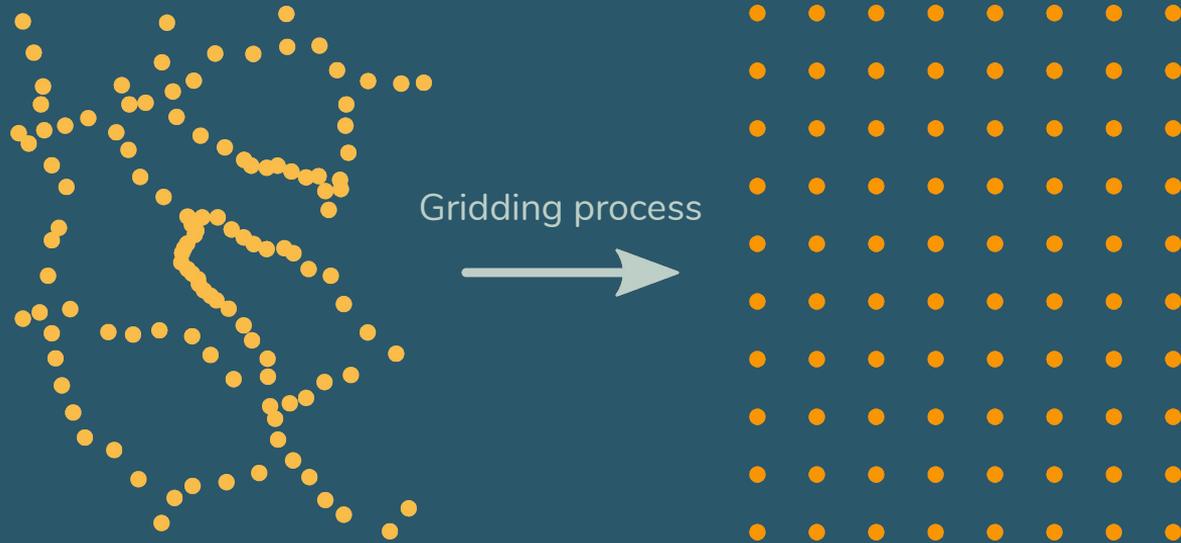


Harmonic fields



Depend on height

And... are usually needed in regular grids



# All purpose 2D griders are not the best option



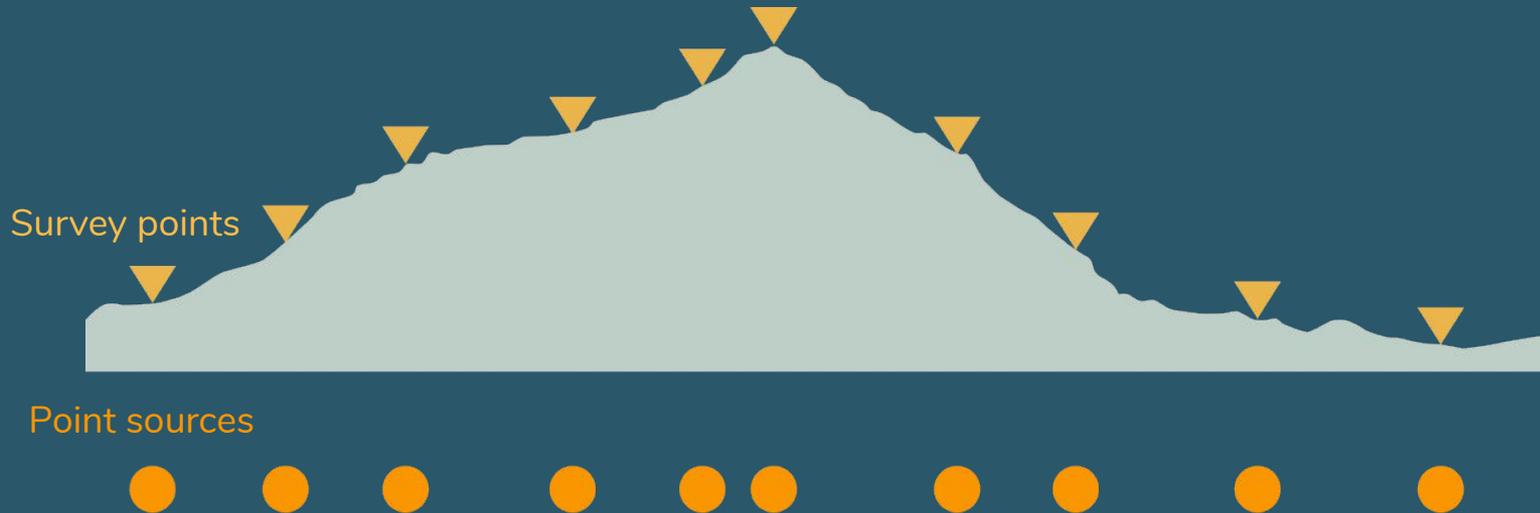
Resulting grid is  
not harmonic



Ignore height  
dependency

# Equivalent Sources

Define a set of point sources that generate the same observed field.



# Equivalent Sources

Use the equivalent sources to predict the field on grid points



# Advantages of equivalent sources



Grid values are  
harmonic

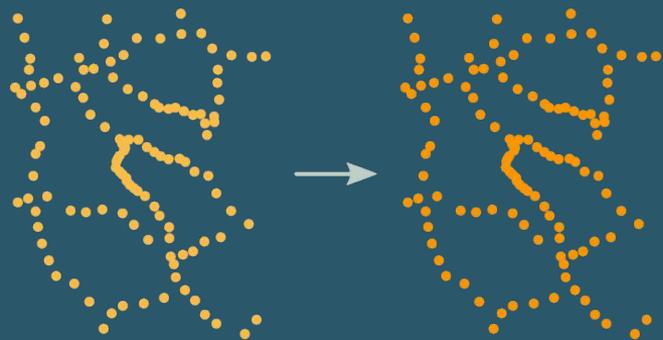


Consider the  
observation heights

Where to put the  
equivalent sources?

# Classical Strategies

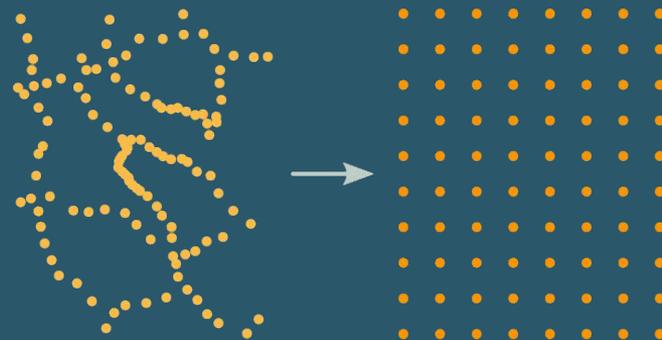
Sources below data points



Data points

Sources

Regular grid of sources

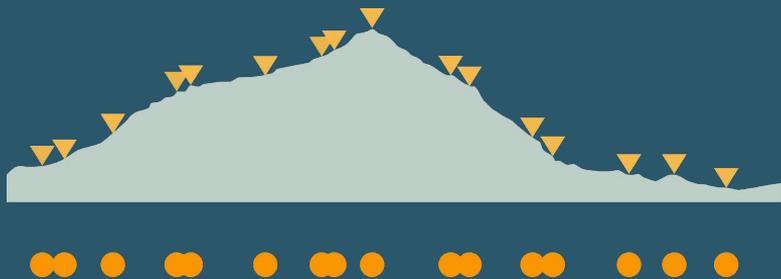


Data points

Sources

# Classical Strategies

Sources below data points



Disadvantages:

- Could create aliases on anisotropic distribution of sources (e.g. many sources along flight paths).

Regular grid of sources

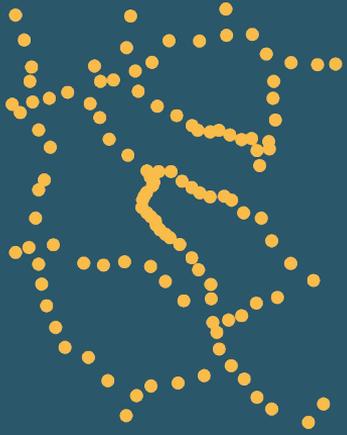


Disadvantages:

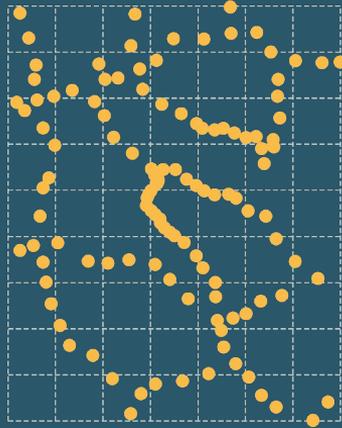
- May require too many sources to produce accurate predictions, needing high computational load.

A new strategy

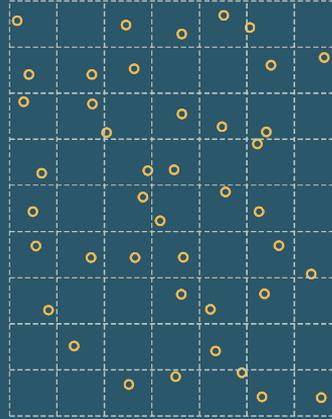
# Block-averaged sources



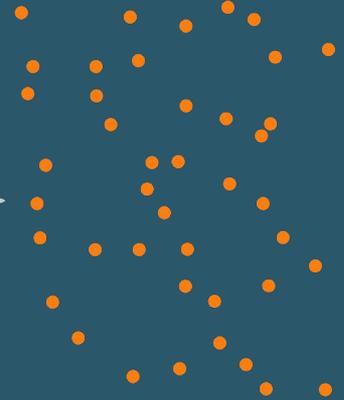
Data points



Divide the region in **blocks** of equal size

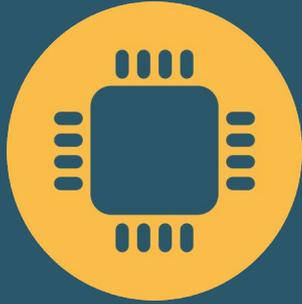


**Average** data coordinates per block



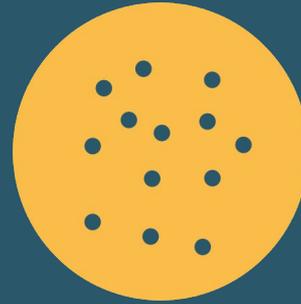
Sources under each averaged location

# Advantages of block-averaged sources



Reduces computational load

Reduces the number of point sources

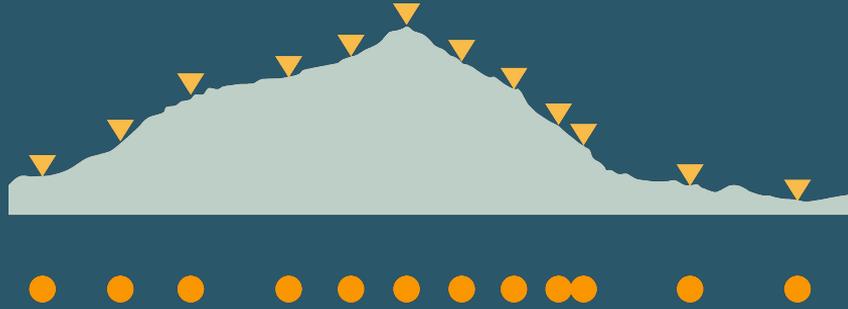


Prevents aliasing

Creates non-anisotropic sources

But... at which depth?

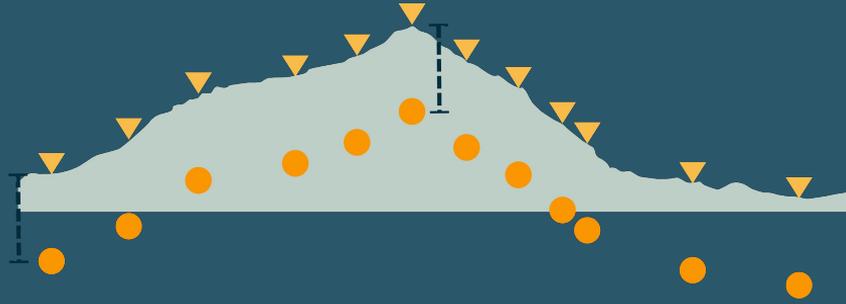
## Constant Depth



`sources_depth = depth`

All sources at the same depth.

## Relative Depth



$$\text{sources\_depth} = \text{data\_height} - \text{depth}$$

Sources at the same relative depth  
from its corresponding data point.

# Variable Depth



$$\text{sources\_depth} = \text{data\_height}$$

$$- \text{depth}$$

$$- f \cdot \text{distance\_n\_neighbours}$$

constant factor

mean distance to nearest neighbours

## Variable Depth



- **Scattered** data produce **deep** sources.
- **Clustered** data produce **shallow** sources.

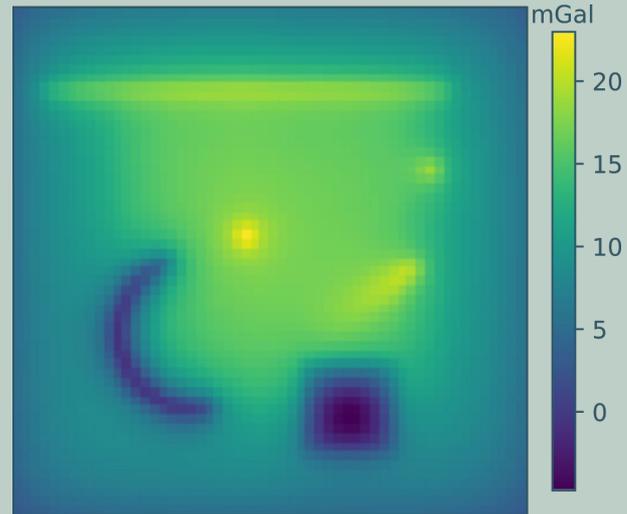


How good are they?

# Comparison of source distributions

1. Synthetic gravity model

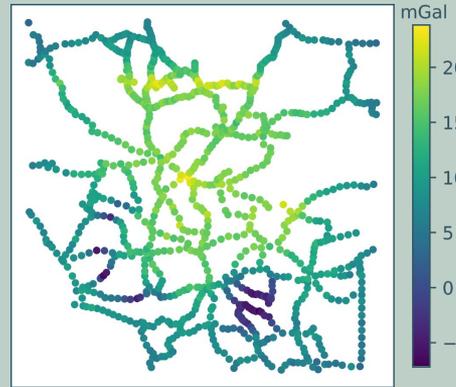
Synthetic gravity model



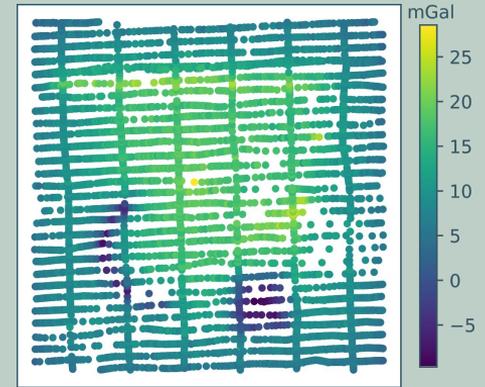
# Comparison of source distributions

1. Synthetic gravity model
2. Synthetic surveys

Ground survey



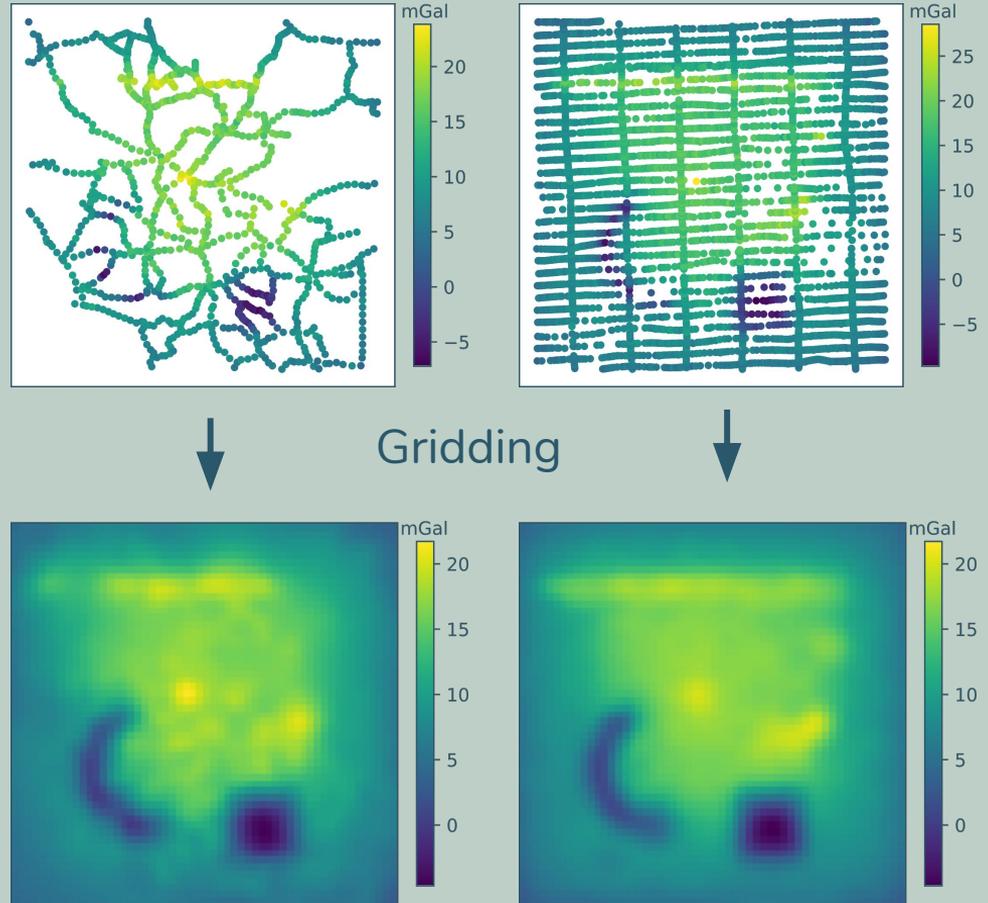
Airborne survey



# Comparison of source distributions

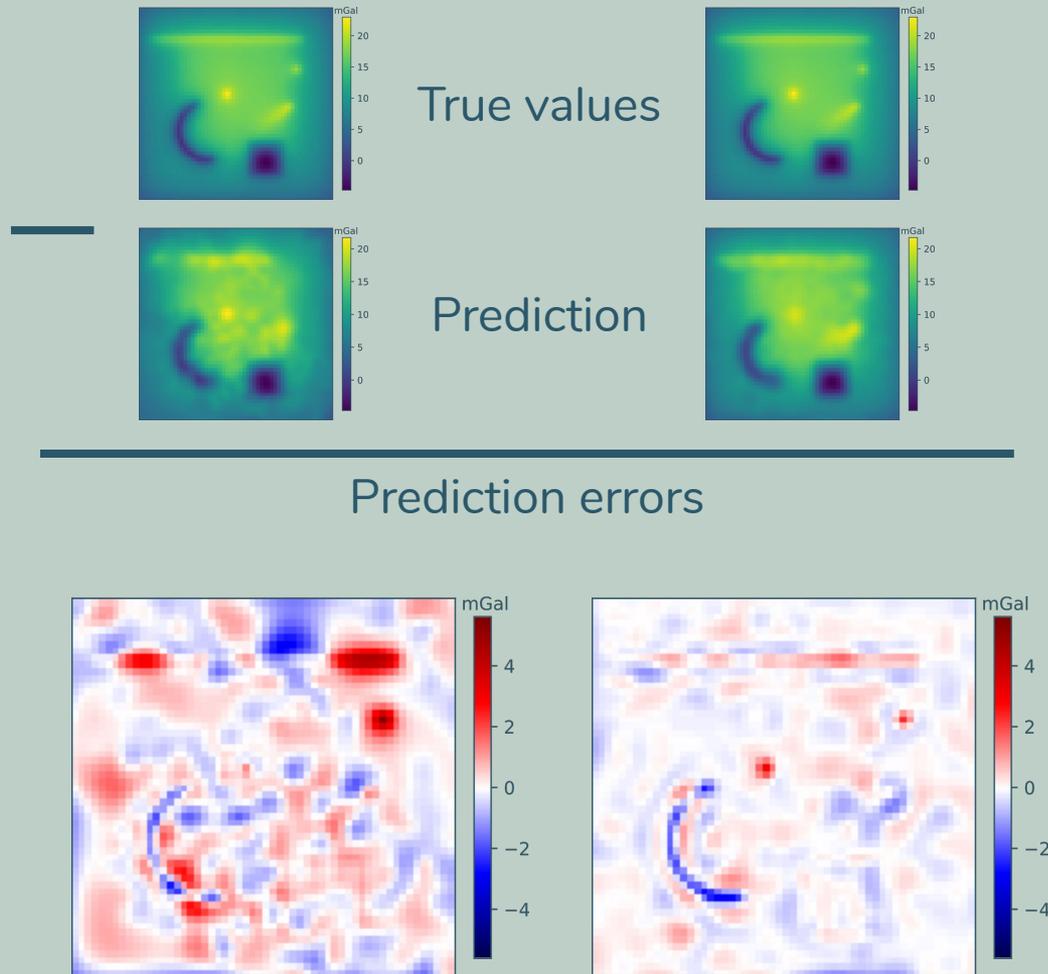
1. Synthetic gravity model
2. Synthetic surveys
3. Grid data with each source distribution

\* Obtaining seven grids for each synthetic survey



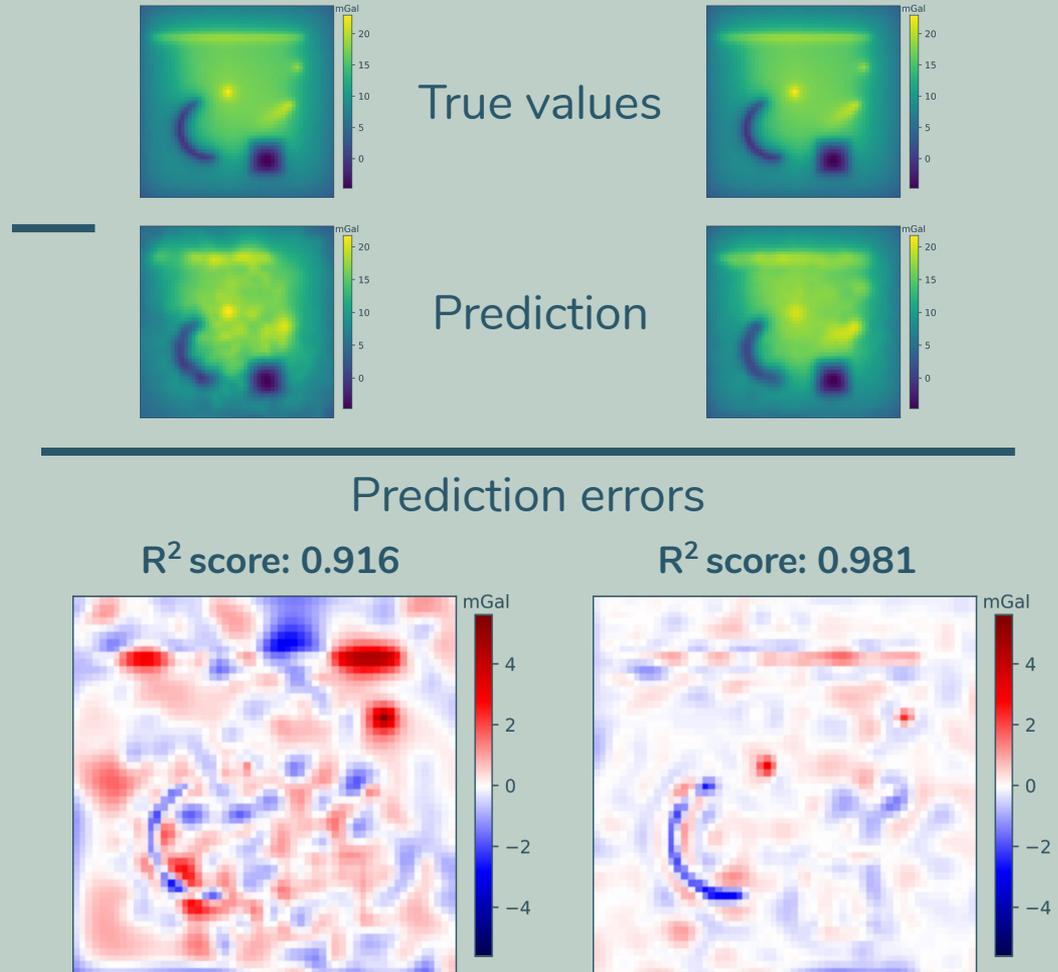
# Comparison of source distributions

1. Synthetic gravity model
2. Synthetic surveys
3. Grid data with each source distribution
4. Compare against true values



# Comparison of source distributions

1. Synthetic gravity model
2. Synthetic surveys
3. Grid data with each source distribution
4. Compare against true values
5. Score the interpolation





## R<sup>2</sup> scores

**All source distributions achieve accurate interpolations**

Ground survey	Constant depth	Relative depth	Variable depth
Sources below data	0.862	0.862	0.878
Grid sources	0.847	-	-
Block-averaged sources	<b>0.867</b>	<b>0.866</b>	<b>0.916</b>
Airborne survey	Constant depth	Relative depth	Variable depth
Sources below data	0.974	0.975	0.975
Grid sources	0.978	-	-
Block-averaged sources	<b>0.974</b>	<b>0.975</b>	<b>0.981</b>

## R<sup>2</sup> scores

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Block-averaged sources	0.974	0.975	0.981

**Variable depth produce slightly better results**

But... how many sources do they use?

	Ground survey	Airborne survey
Sources below data	963	5673
Grid sources	1444	6162
Block-averaged sources	518	1663

But... how many sources do they use?

	Ground survey	Airborne survey
Sources below 100m	5673	5673
Grid sources	6162	6162
Block-averaged sources	518	1663

**Block-averaged distribution  
creates less sources**

# Conclusions

- New strategy for gridding: **block-averaged sources**.
- Produces **accurate interpolations**, comparable with classical strategies.
- Create **less sources**, requiring **less computational load**.
- May help **solving aliasing** problems.
- Using a **variable depth** may give **more accurate** results.

# Acknowledgements



Fatiando a Terra

Open-source Python tools for Geophysics  
[www.fatiando.org](http://www.fatiando.org)



This research was possible thanks to the work of  
developers and maintainers of open-source software.

# Want to read more about this?

Article and code will be released soon... stay tuned:



COMPUTER-ORIENTED  
GEOSCIENCE LAB

<https://www.compgeolab.org/>

Slides are available for download:

<https://doi.org/10.6084/m9.figshare.12217973>



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