

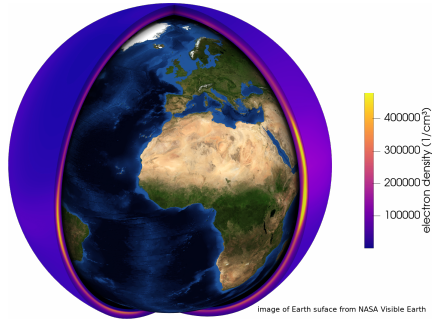
Impact of electron density values from space-geodetic observation techniques on thermospheric density models

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Michael Schmidt², Jürgen Kusche¹

¹ IGG, University of Bonn

² DGFI, Technical University of Munich

07 May 2020



Development of High-precision

Thermosphere Models for **I**mproving **P**recise **O**rbit **D**etermination of Low-Earth-Orbiting Satellites

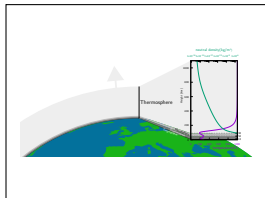


Watch this 2.5 minutes video for a quick introduction

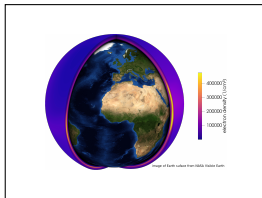


Credit: NASA/ESA

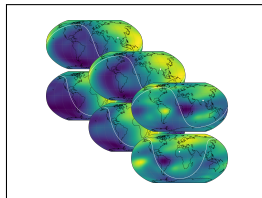
Introduction



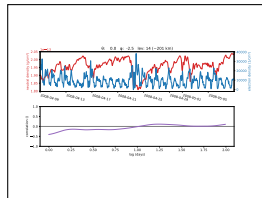
TIE-GCM



Data Assimilation



Correlations



click on an image to jump to the corresponding section

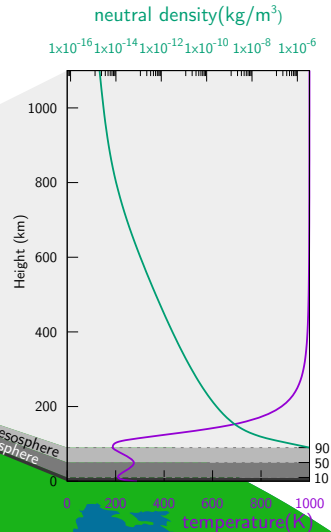


Image: ESA/D.Ducros

- ▶ **atmospheric drag** is largest non gravitational acceleration acting on on LEO satellites
- ▶ atmospheric drag depends on **air density** along the orbit
- ▶ significant differences between models providing air density
- ▶ idea: improve models using **data assimilation**, including electron density observations

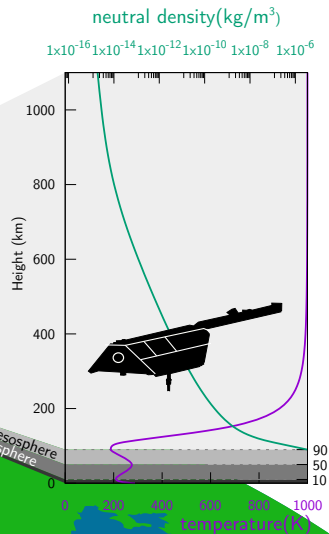
- ▶ highest layer of atmosphere when classifying by temperature
- ▶ thermosphere approximately begins above **90 km**
- ▶ temperature increase due to absorption of **UV radiation**
- ▶ asymptotically approaching **exospheric temperature**

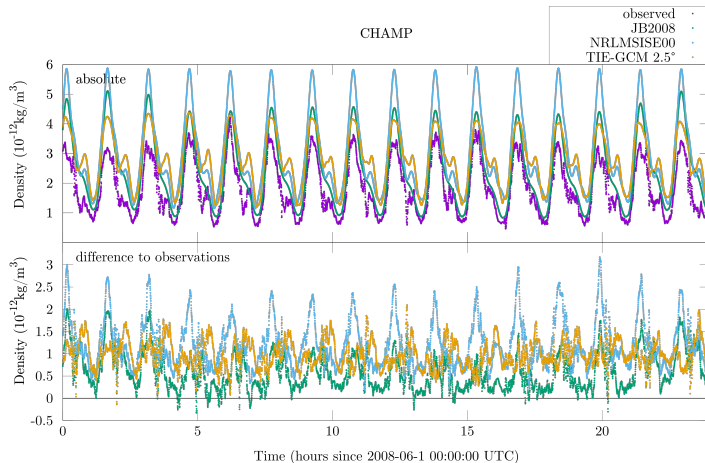
Thermosphere



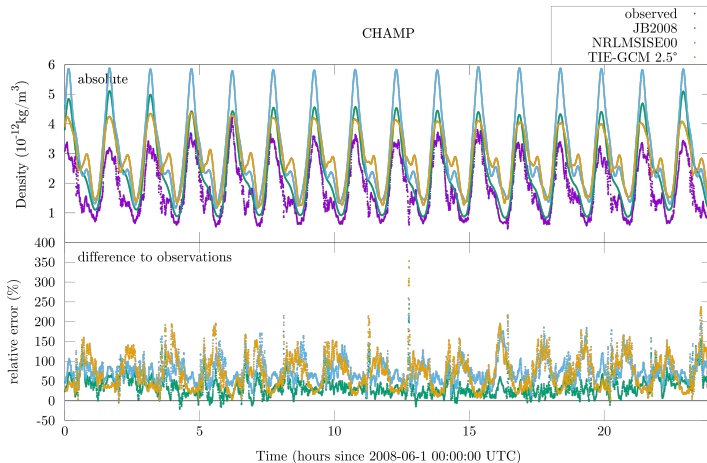
- ▶ the satellite mission CHAMP was flying at approximately 350 km altitude
- ▶ in the following we have a closer look at the density along the CHAMP orbit

Thermosphere

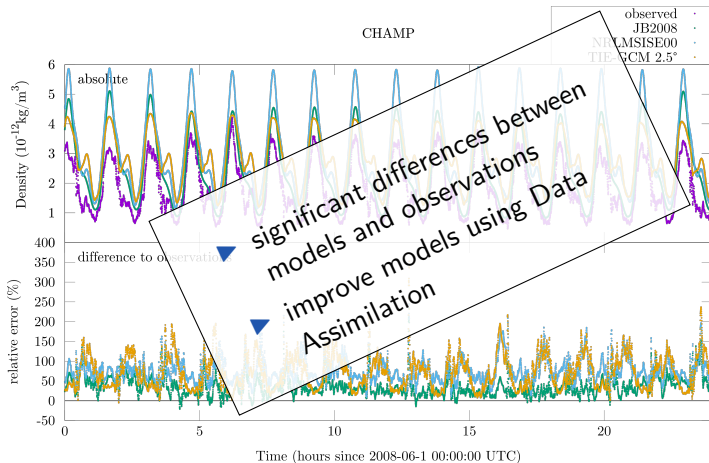




- ▶ solar minimum
- ▶ no geomagnetic storm
- ▶ for more details on observed densities see slide 23

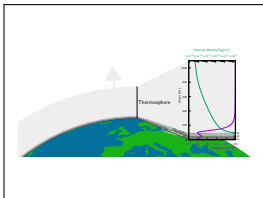


- ▶ solar minimum
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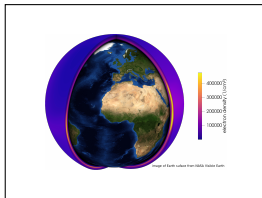


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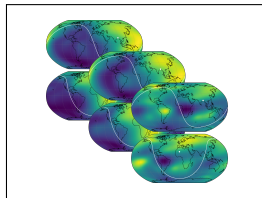
Introduction



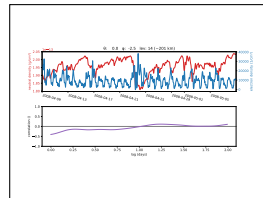
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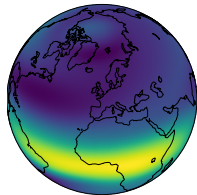


click on an image to jump to the corresponding section

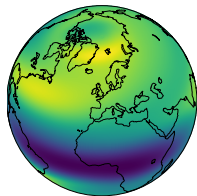
Thermosphere **I**onosphere **E**lectrodynamics **G**eneral **C**irculation **M**odel [3]

- ▶ developed by NCAR High Altitude Observatory
- ▶ physical model
- ▶ written in Fortran 90
- ▶ parallelized with MPI

Thermosphere Ionosphere Electrodynamics General Circulation Model [3]

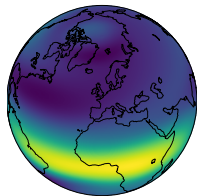


Total Neutral Density

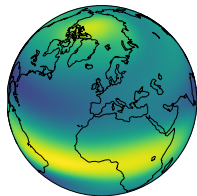


Neutral Temperature

Thermosphere Ionosphere Electrodynamics General Circulation Model [3]

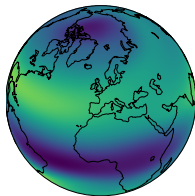


Total Neutral Density



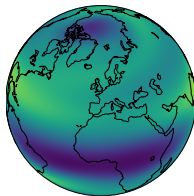
O₂

+



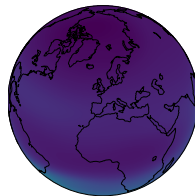
O₁

+



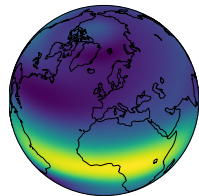
N₂

+

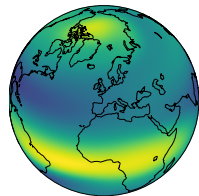


HE

Thermosphere Ionosphere Electrodynamics General Circulation Model [3]

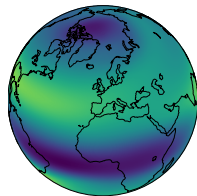


Total Neutral Density



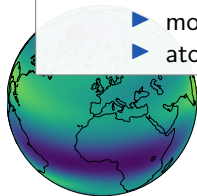
O2

+



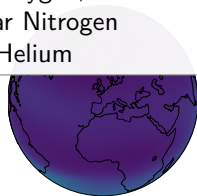
O1

+



N2

+

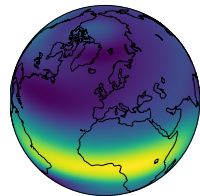


HE

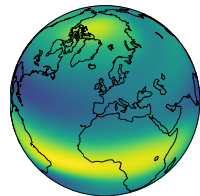
► Total neutral density is derived from 4 individual species:

- molecular Oxygen
- atomar Oxygen,
- molecular Nitrogen
- atomar Helium

Thermosphere Ionosphere Electrodynamics General

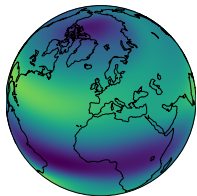


Total Neutral Density



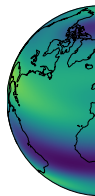
O₂

+

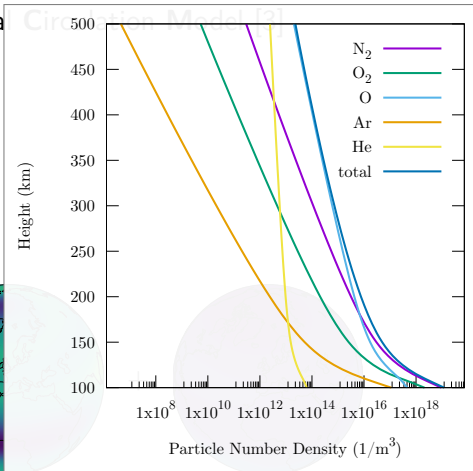


O₁

+

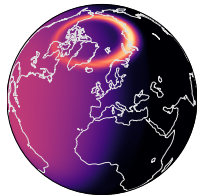


N₂

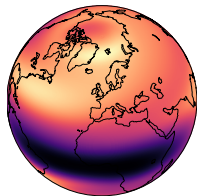


HE

Thermosphere **Ionosphere** Electrodynamics **G**eneral **C**irculation **M**odel [3]

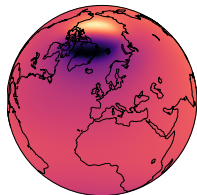


Electron Density



Electron Temperature

Thermosphere Ionosphere **Electrodynamics** General Circulation Model [3]

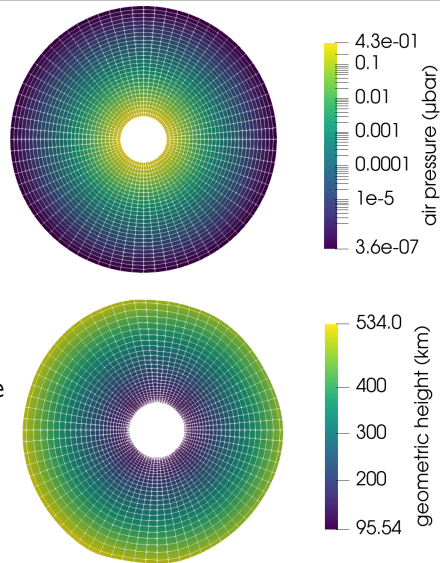


Electric Potential

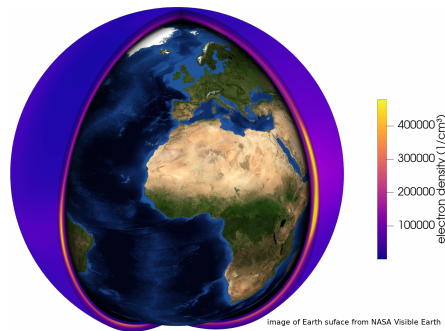


Meridional Ion Drift

- ▶ 4-D regular grid:
longitude, latitude, **pressure level**, time
- ▶ grid has either 5° or 2.5° resolution
- ▶ transformation from pressure level to height makes vertical component **irregular** (but structured) and **time dependent**
- ▶ transformation necessary for interpolation of satellite orbits in model fields

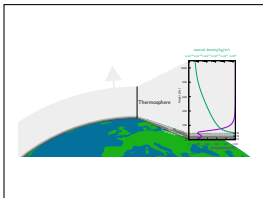


- ▶ TIE-GCM requires more computational power than empirical models
- ▶ free run does not necessarily perform better than empirical models (fit to observations)
- ▶ But, enables us to **assimilate a lot of different data**, especially observations of the **ionosphere**
- ▶ there are more geodetic measurement of the ionosphere than thermosphere density measurements

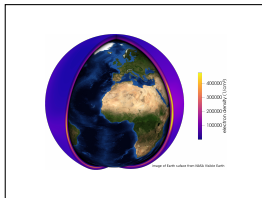


Electron density derived from TIE-GCM on
9 April 2008 12:00 UTC

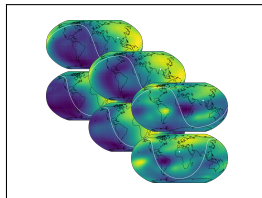
Introduction



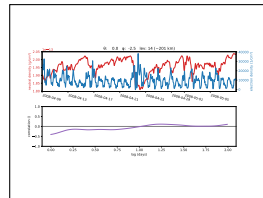
TIE-GCM



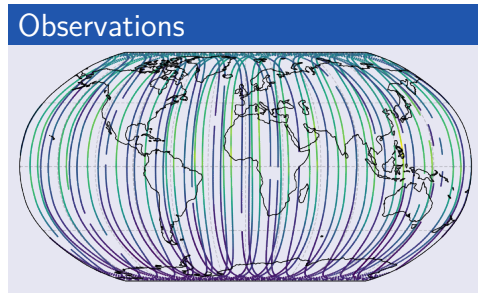
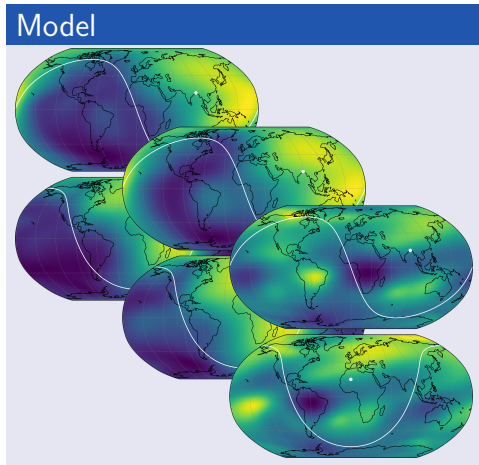
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Correlations

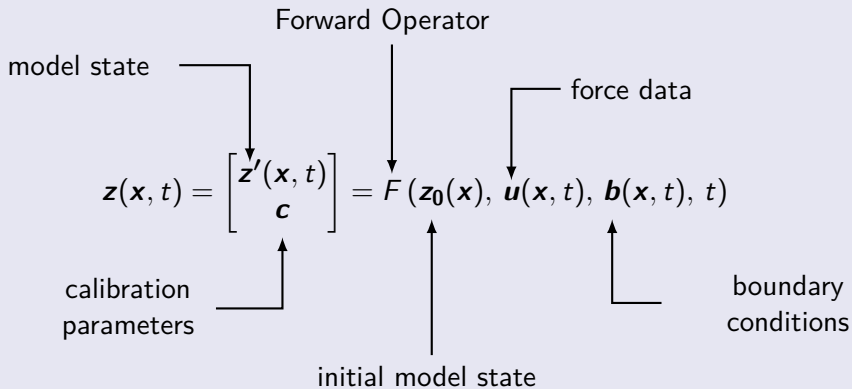


click on an image to jump to the corresponding section

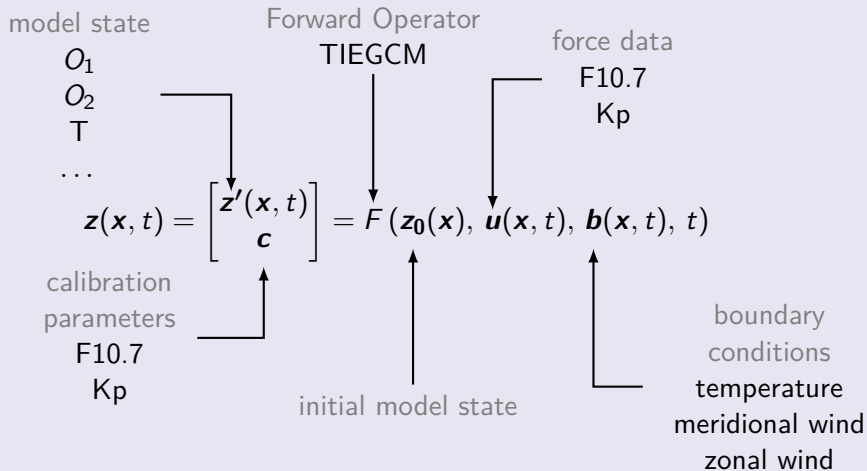


combine a model with observations

Model



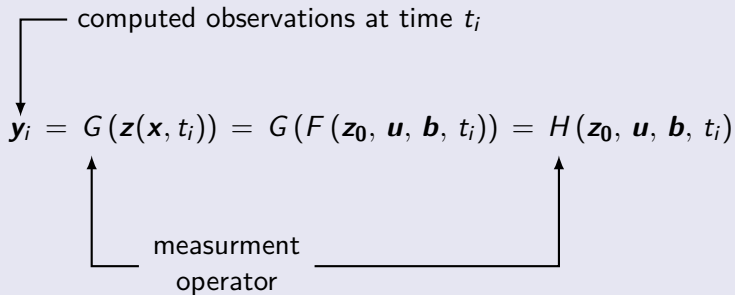
Model



Model

$$\mathbf{z}(\mathbf{x}, t) = \begin{bmatrix} \mathbf{z}'(\mathbf{x}, t) \\ \mathbf{c} \end{bmatrix} = F(\mathbf{z}_0(\mathbf{x}), \mathbf{u}(\mathbf{x}, t), \mathbf{b}(\mathbf{x}, t), t)$$

computed observation



Model

$$\mathbf{z}(\mathbf{x}, t) = \begin{bmatrix} \mathbf{z}'(\mathbf{x}, t) \\ \mathbf{c} \end{bmatrix} = F(\mathbf{z}_0(\mathbf{x}), \mathbf{u}(\mathbf{x}, t), \mathbf{b}(\mathbf{x}, t), t)$$

computed observation

$$\mathbf{y}_i = G(\mathbf{z}(\mathbf{x}, t_i)) = G(F(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)) = H(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)$$

Model

$$\mathbf{z}(\mathbf{x}, t) = \begin{bmatrix} \mathbf{z}'(\mathbf{x}, t) \\ \mathbf{c} \end{bmatrix} = F(\mathbf{z}_0(\mathbf{x}), \mathbf{u}(\mathbf{x}, t), \mathbf{b}(\mathbf{x}, t), t)$$

computed observation

$$\mathbf{y}_i = G(\mathbf{z}(\mathbf{x}, t_i)) = G(F(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)) = H(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)$$

sequential DA

$$\mathbf{z}_i = \mathbf{z}(t_i) = F(\mathbf{z}_{i-1}, t_i)$$

$$\hat{\mathbf{z}}_i = \mathbf{z}_i + \mathbf{K}_i (\underbrace{\ell_i - H(\mathbf{z}_i)}_{\text{observed - computed}})$$

Kalman Gain $\uparrow$ $\uparrow$ observed - computed

Model

$$\mathbf{z}(\mathbf{x}, t) = \begin{bmatrix} \mathbf{z}'(\mathbf{x}, t) \\ \mathbf{c} \end{bmatrix} = F(\mathbf{z}_0(\mathbf{x}), \mathbf{u}(\mathbf{x}, t), \mathbf{b}(\mathbf{x}, t), t)$$

computed observation

$$\mathbf{y}_i = G(\mathbf{z}(\mathbf{x}, t_i)) = G(F(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)) = H(\mathbf{z}_0, \mathbf{u}, \mathbf{b}, t_i)$$

sequential DA

$$\mathbf{z}_i = \mathbf{z}(t_i) = F(\mathbf{z}_{i-1}, t_i)$$

$$\hat{\mathbf{z}}_i = \mathbf{z}_i + \mathbf{K}_i(\ell_i - H(\mathbf{z}_i))$$

- ▶ Amount of parameters in TIE-GCM is huge.
- ▶ with 5° resolution a single field has 75168 cells
- ▶ using error subspace Kalman filters (no need to compute full covariance matrix)

Ensemble Filters

EnKF

Ensemble KF

ETKF

Ensemble Transform KF

SEIKF

Singular Evolutive Interpolated KF

ESTKF

Error Subspace Transform KF

Low-rank Filters

SECKF

Singular Evolutive Extended KF

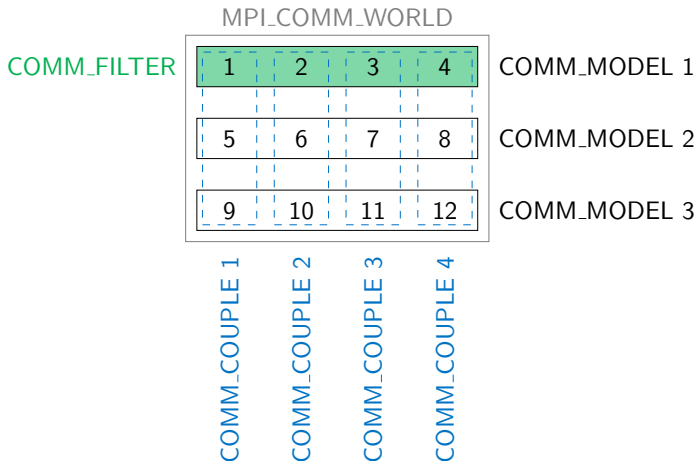
PDAF Parallel
Data
Assimilation
Framework

- ▶ developed at Alfred Wegener Institute
- ▶ implementation of many error subspace filters
- ▶ written in Fortran 90
- ▶ parallelized with MPI

PDAF Parallel
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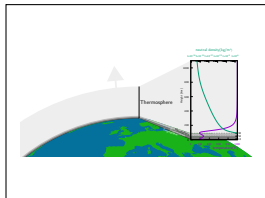
- ▶ developed at Alfred Wegener Institute
- ▶ implementation of many error subspace filters
- ▶ written in Fortran 90
- ▶ parallelized with MPI
- ▶ 'Online mode': TIE-GCM code is extended by calls to PDAF routines
- ▶ no I/O overhead

- ▶ message passing interface (MPI) is used for fully parallel implementation
- ▶ each instance of TIE-GCM (each ensemble member) runs parallel
- ▶ several instances of TIE-GCM are computed parallel

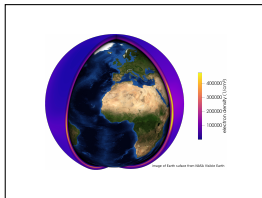


- ▶ Adaptation of the parallelization ✓
- ▶ Initialization of PDAF and the ensemble ✓
- ▶ Modification of the model code for the ensemble integration ✓
- ▶ Implementation of the analysis step
 - ▶ observation operator for NRLMSISE-00 observations **implemented but not tested**
 - ▶ observation operator for electron density observations ✗
 - ▶ observation operator for neutral density observations derived from accelerometers ✗

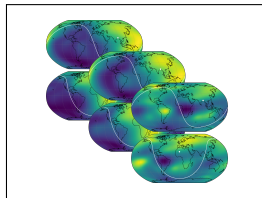
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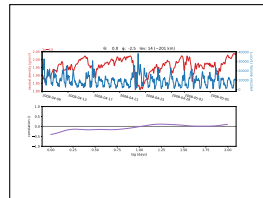
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Correlations



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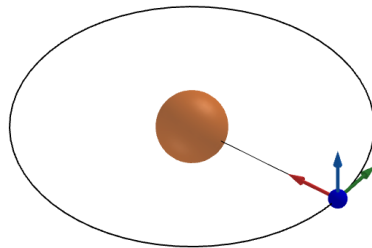
Hypothesis

Assimilating electron densities into a physical model of the Thermosphere improves also the neutral density

- ▶ Due to Corona disruptions we could not work as much on the density data integration as we would have liked
- ▶ But we can show correlations between neutral density and electron density
- ▶ Ee investigate:
 - ▶ correlations within TIE-GCM (free run)
 - ▶ correlations between observations
- ▶ These correlations will control the observability of thermosphere density in the EnKF via ionosphere observations

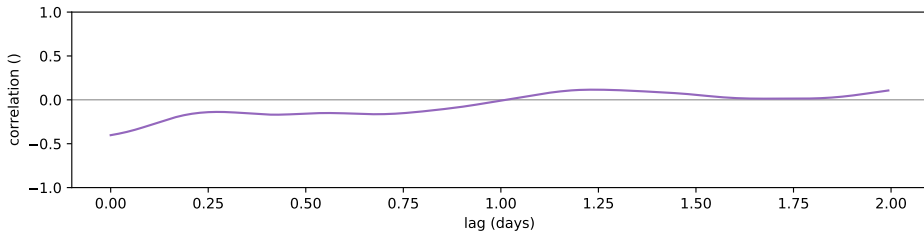
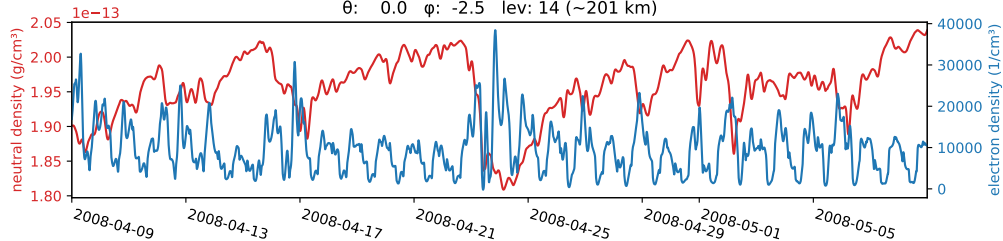
TIE-GCM fields are co-rotating with Earth. For a meaningful correlation analysis we need to compensate the motion of the Sun w.r.t. to the Earth.

- ▶ origin in geocenter
- ▶ x axis is pointing to the Sun
- ▶ z axis is perpendicular to ecliptic
- ▶ y axis completes left-handed coordinate system



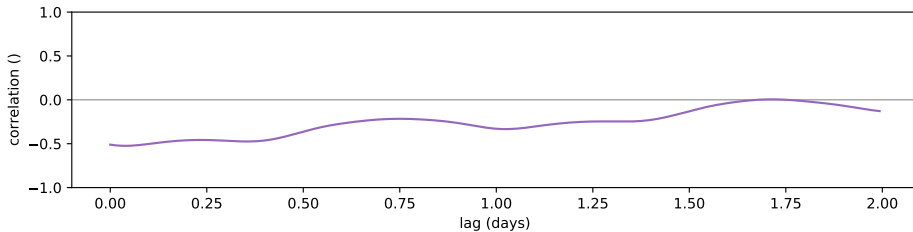
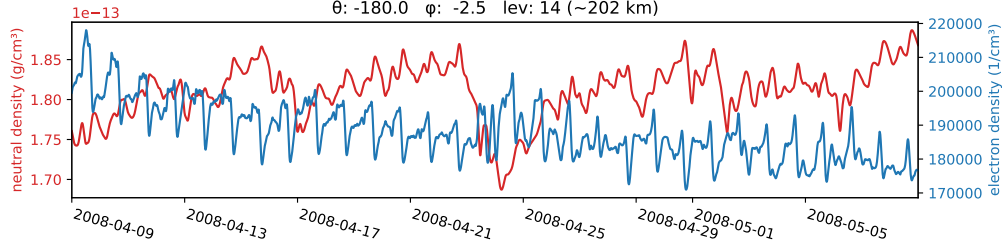
day side

θ : 0.0 ϕ : -2.5 lev: 14 (~201 km)

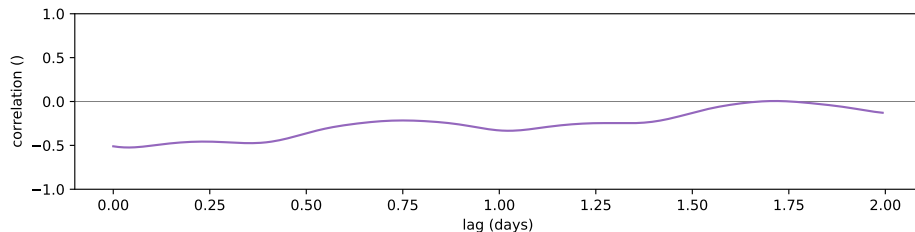
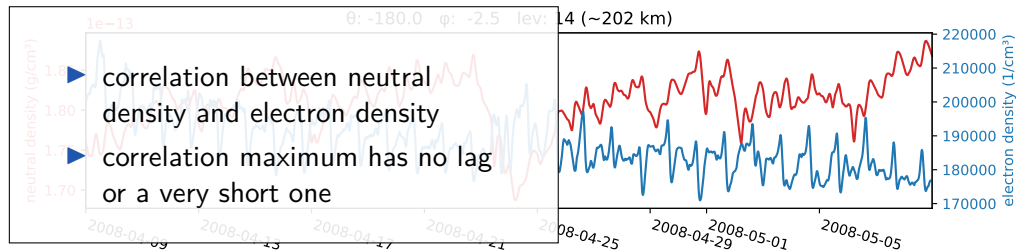


night side

θ : -180.0 ϕ : -2.5 lev: 14 (~202 km)

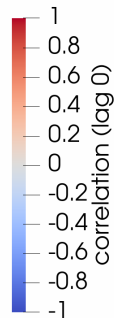
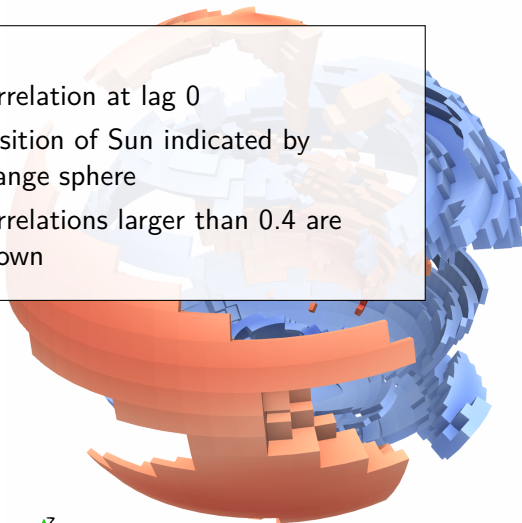


night side

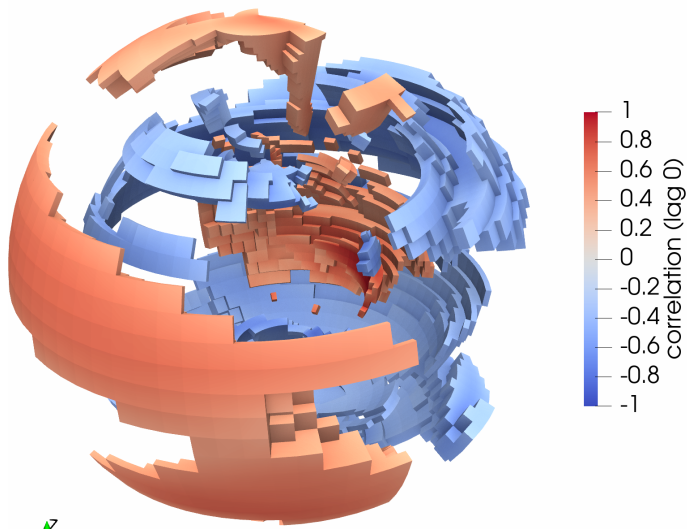




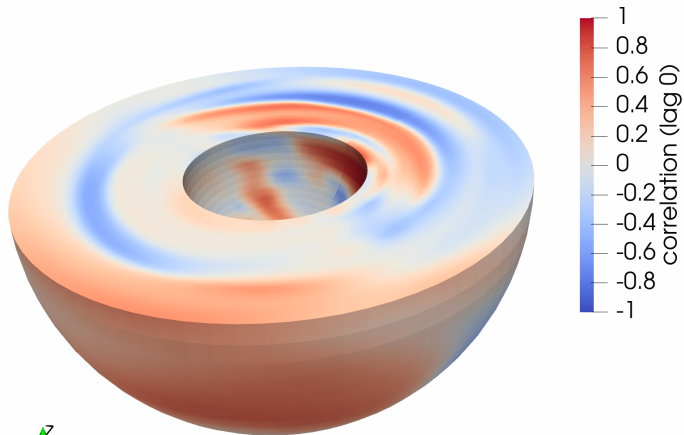
- ▶ correlation at lag 0
- ▶ position of Sun indicated by orange sphere
- ▶ correlations larger than 0.4 are shown



z



z



z

neutral density

derived from **calibrated accelerometer data** [4] considering accelerations due to

- ▶ Earth radiation pressure [5]
- ▶ Sun radiation pressure [5]

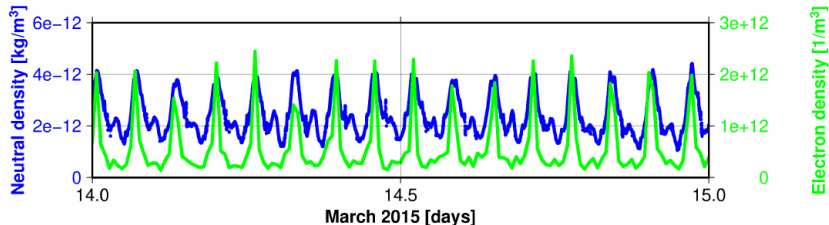
electron density

4D electron density model based on GNSS and satellite altimetry observations as well as radio occultation measurements [1]

- ▶ Neutral density: from GRACE accelerometer data (altitude 410 km)
- ▶ Electron density: from 4D-model interpolated to 10 seconds

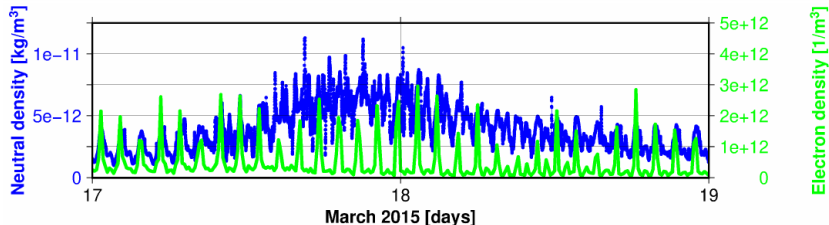
**Quite
time**

Correlation:
86.1%



**Storm
time**

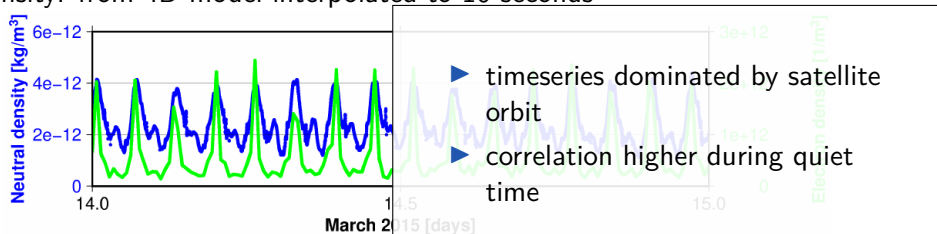
Correlation:
34.3%



- ▶ Neutral density: from GRACE accelerometer data (altitude 410 km)
- ▶ Electron density: from 4D-model interpolated to 10 seconds

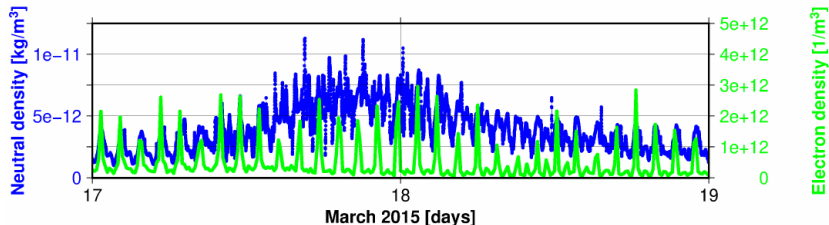
**Quite
time**

Correlation:
86.1%



**Storm
time**

Correlation:
34.3%



- ▶ Correlations within the model indicate that the **electron density has direct (no lag) impact on neutral density**.
- ▶ We also see high correlations between observed neutral densities and electron densities.
- ▶ Thus, we are confident that the assimilation of electron densities is likely to improve neutral density.

- [1] Marco Limberger. *Ionosphere modeling from GPS radio occultations and complementary data based on B-splines*. PhD thesis, Technische Universität München, 2015.
- [2] Lars Prange, Adrian Jäggi, Rolf Dach, Heike Bock, Gerhard Beutler, and Leos Mervart. Aiub-champ02s: The influence of gnss model changes on gravity field recovery using spaceborne gps. *Advances in space research*, 45(2):215–224, 2010.
- [3] Liying Qian, Alan G Burns, Barbara A Emery, Benjamin Foster, Gang Lu, Astrid Maute, Arthur D Richmond, Raymond G Roble, Stanley C Solomon, and Wenbin Wang. The NCAR TIE-GCM: A community model of the coupled thermosphere/ionosphere system. In Joseph Huba, Robert Schunk, and Khazanov George, editors, *Modeling the Ionosphere–Thermosphere System*, Geophysical Monograph Series, pages 73–83. American Geophysical Union (AGU), 1 edition, 2014.
- [4] K. Vielberg, E. Forootan, C. Lück, A. Löcher, J. Kusche, and K. Börger. Comparison of accelerometer data calibration methods used in thermospheric neutral density estimation. *Annales Geophysicae*, 36(3):761–779, 2018.
- [5] Kristin Vielberg and Jürgen Kusche. Extended forward and inverse modeling of radiation pressure accelerations for leo satellites. *Journal of Geodesy*, 94(4):1–21, 2020.