Meter-scale Measurements of VHF structure of natural leader streamers

or

The largest streamers can be individually imaged in VHF



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Outline

Under the idea that these slides will be viewed individually, I've organized them like notes. This slide gives the location of different independent sections.

Next slide presents the main arguments I wish to make.

pgs	Section
3	Conclusion
4-7	LOFAR and a mapped lightning flash
8-14	Data on negative leaders
15-17	Comparison between received radio pulses and antenna impulse response
18-19	Hypothesis on source of VHF emission
20-21	Order-of-magnitude energy estimate
22-25	Order-of-magnitude charge estimate

Many figures and arguments are borrowed from Hare et al. [2020], PRL

Conclusion

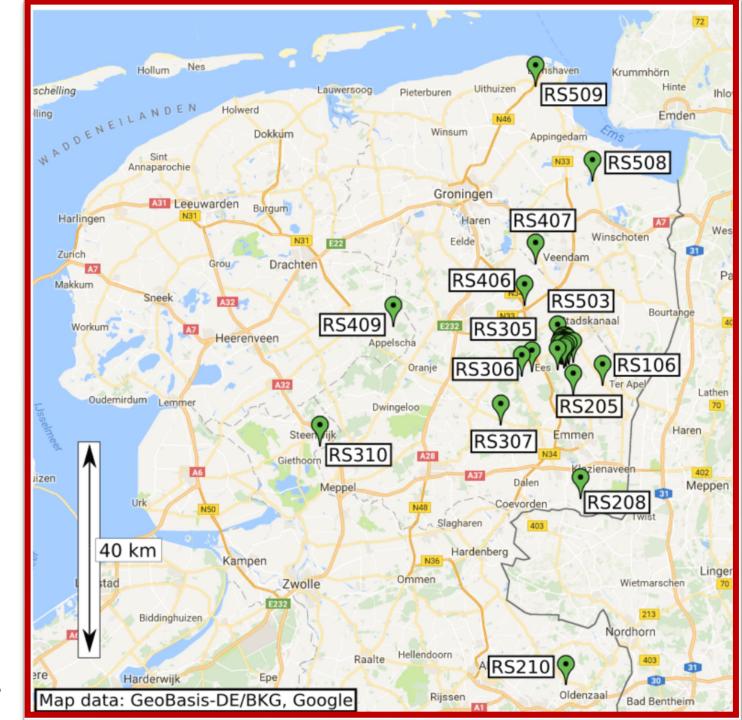
- Each leader step produces a burst of VHF sources
 - 2/3 of sources from one location (≈ 1 m)
 - 1/3 from about 3 m distance
 - Multiple discrete pulses per burst
- Observed VHF pulses are consistent with antenna impulse response
 - Source of individual pulses must be 10 ns or less in duration
 - Each pulse is most likely due a single streamer
 - Only a few streamers per step are strong enough to make a visible pulse
- Can estimate emitted energy in our frequency band
 - Order-of-magnitude of $2\times 10^{-6}~{\rm J}$
 - Consistent with a total streamer charge with order-of-magnitude of $8\ \mu\text{C}$

Dutch LOFAR

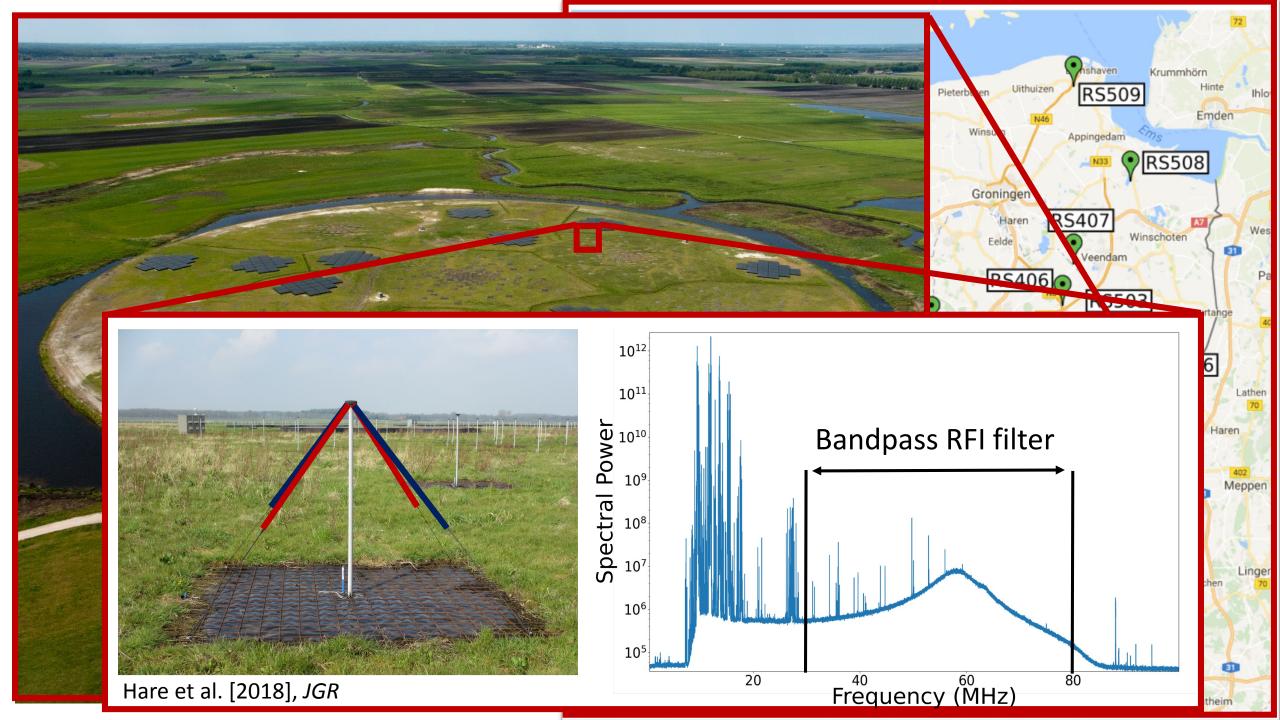
- 24 "core" stations
- 14 "remote" stations
- 3200 km² enclosed area

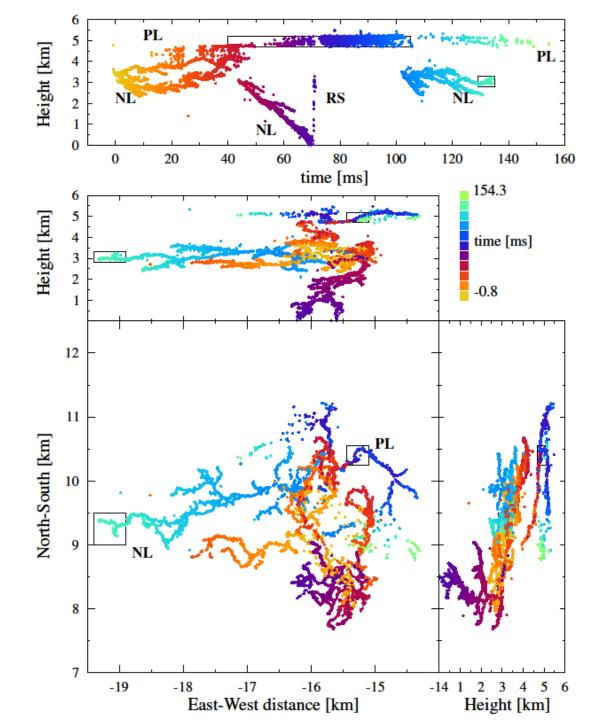
Per Station:

- 96 low-band antennas
 - 10 90 MHz
 - 48 dual-polarized pairs
 - We use 6 dual-polarized pairs out of the 48 pairs
- 20 high-band antennas
 - 110-250 MHz
 - presently not utilized
 - Also shown in Hare et al. [2018], JGR









PL- positive leader NL- negative leader RS- return stroke

> 15,000 sources after cuts ≈ 100 sources per ms

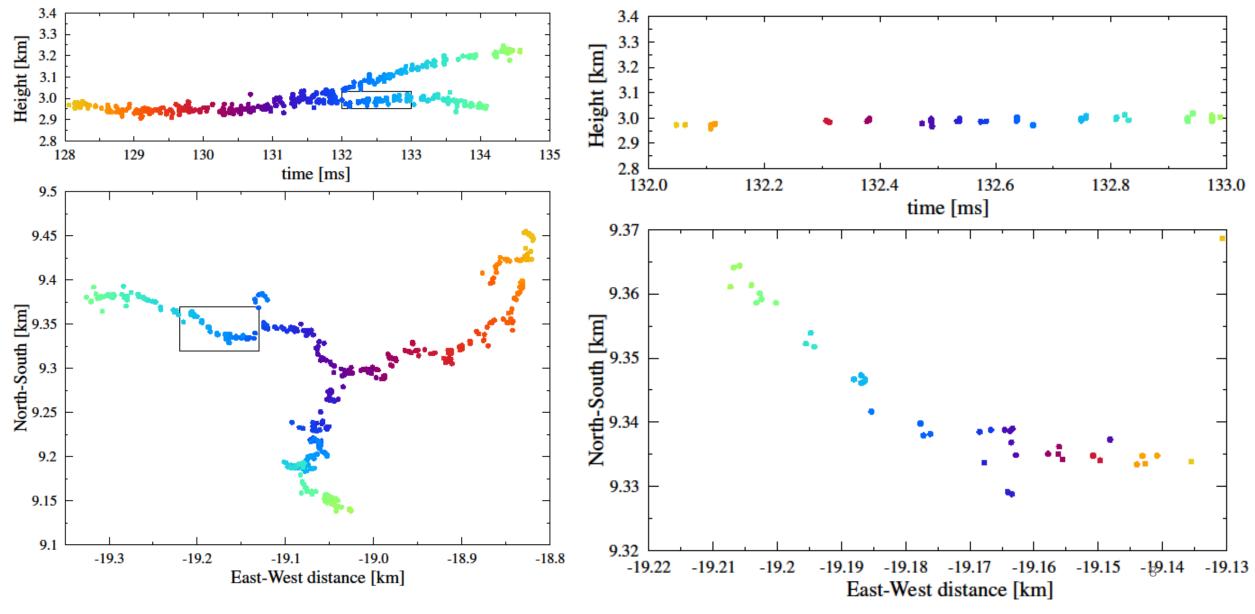
120 ns minimum between sources

Horizontal accuracy around 1 m

Also shown in Hare et al. [2019], Nature 7



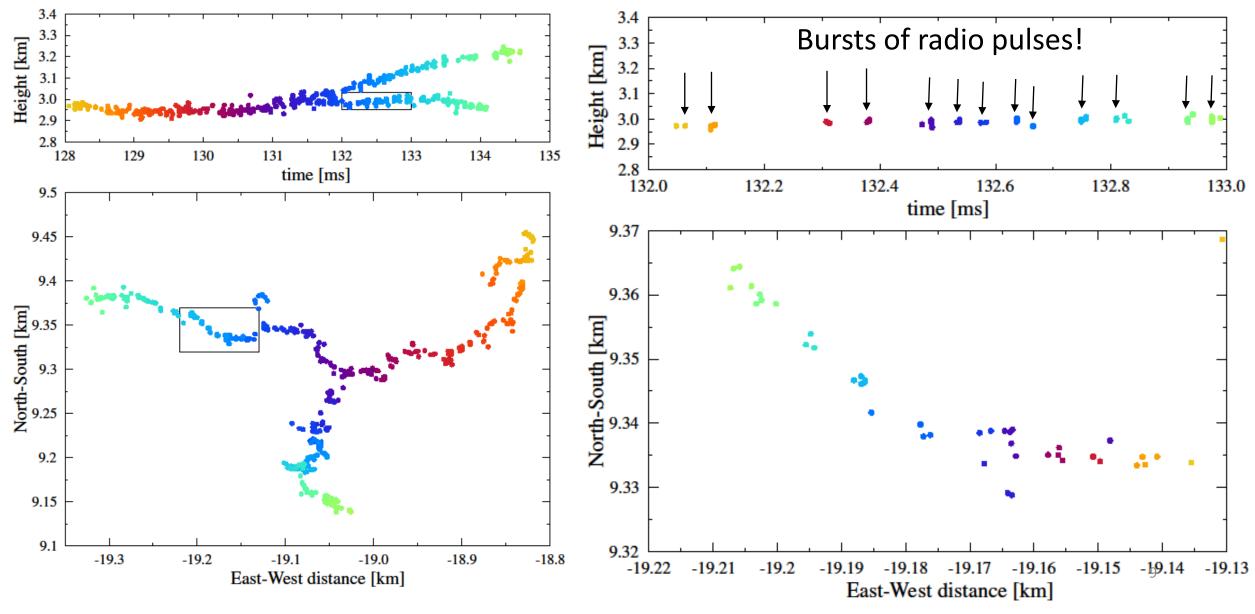
Zoom - In



Also shown in Hare et al. [2019], Nature

Negative Leaders

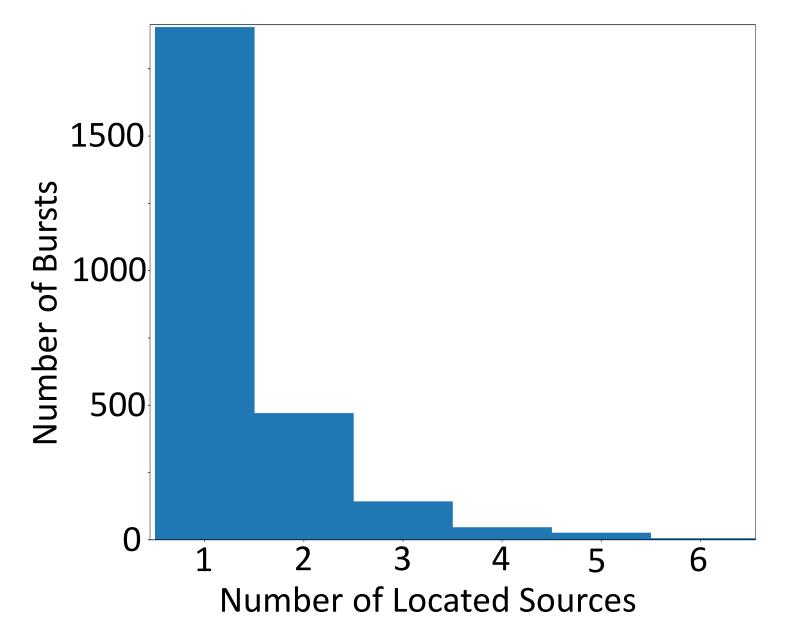
Zoom - In



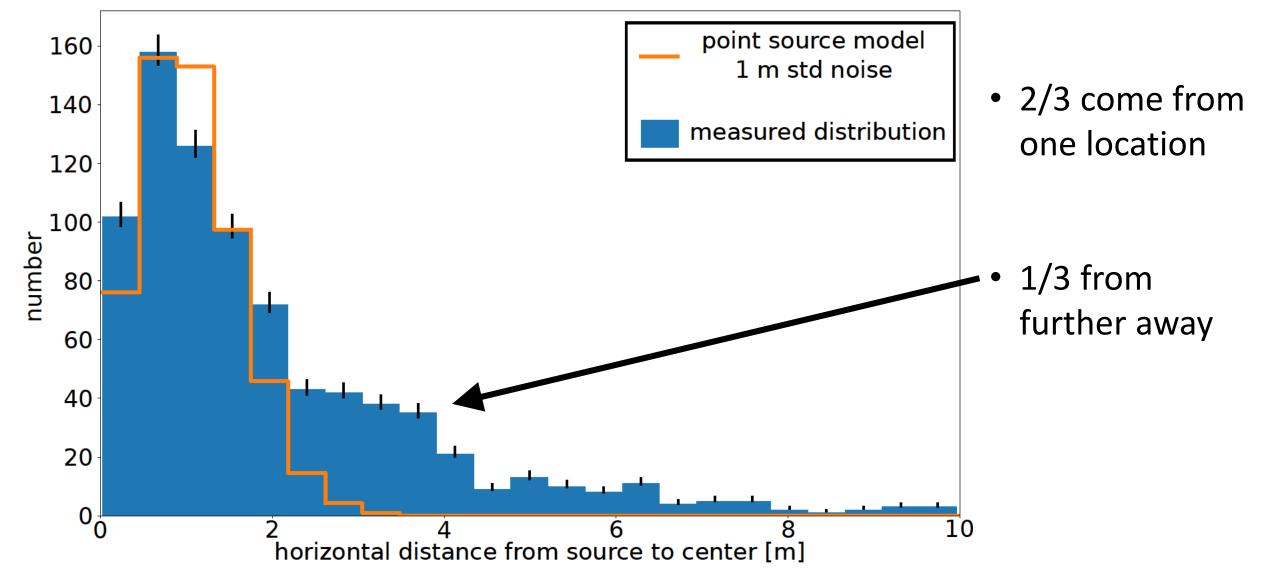
Also shown in Hare et al. [2019], Nature

Distribution of time between Mostly horizontal located sources leaders • 3-4 km altitude 10³ 10³ Uniformly distributed \bullet distribution [number/µs] 101 101 00 sources should be flat 10² in log-space 20 5 10 15 Strong spike below 2 µs Thus bursts are real, not statistical artifact 10-1 50 250 100 150 200 300 0 time between subsequent sources [µs] 10

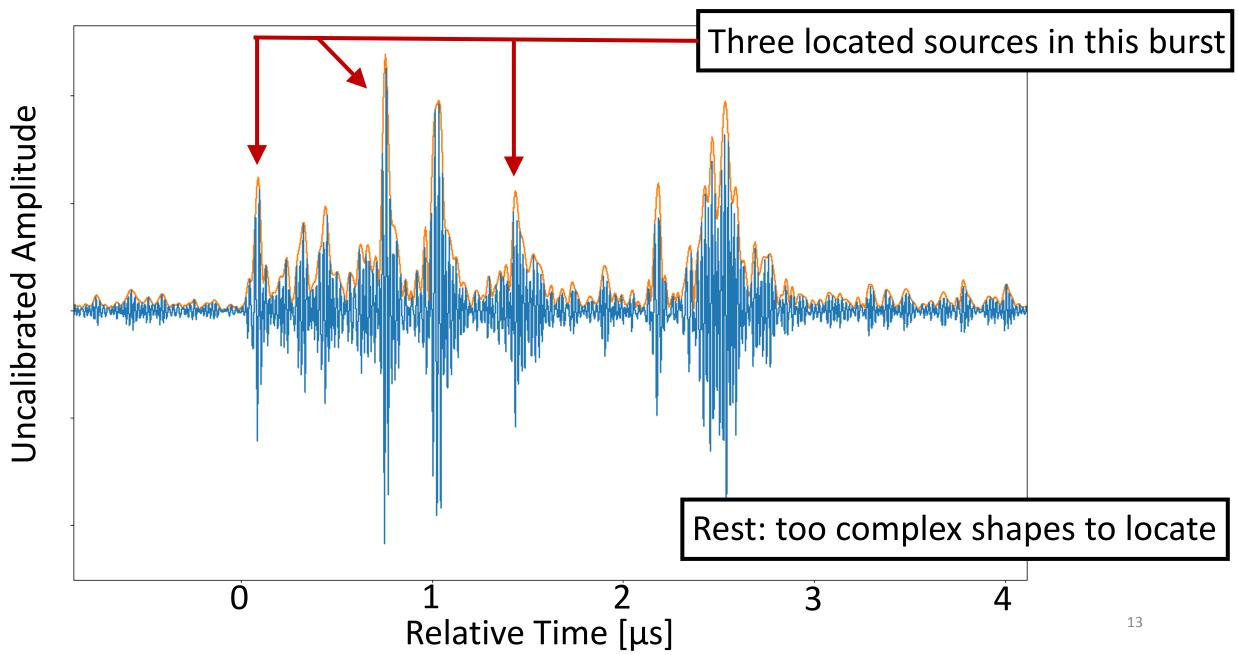
Number of Sources per Burst



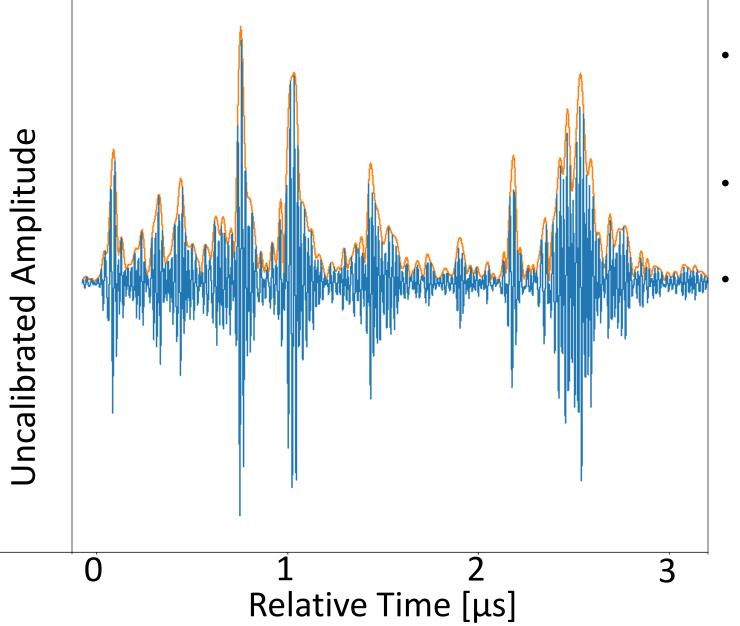
Spatial Distribution of Sources in a Burst



Typical Raw Trace of Burst : we still miss a lot



Typical Raw Trace of Burst : key observations



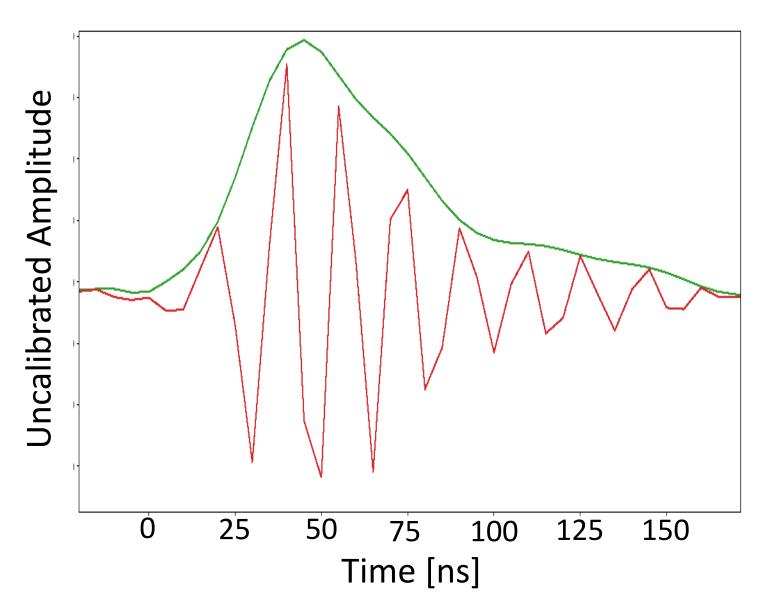
Notes

- VHF signal is very impulsive
 - There are few of the strongest amplitude pulses
- Amplitude distribution is exponential
 - Many more of lower-amplitude pulses

Very little temporal structure

• Pulses occurred at a random rate

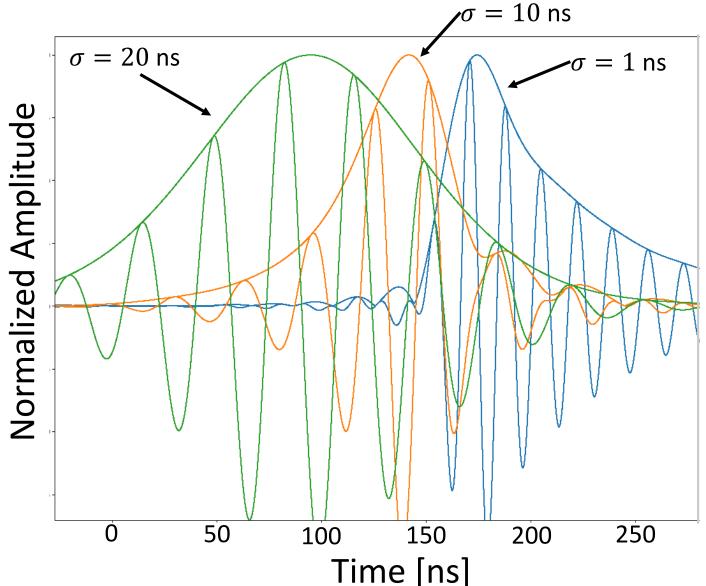
Zoom-in on one pulse



- Figure shows a relatively clean pulse
- Very similar to impulse response
- FWHM is about 50 ns

Antenna Frequency Response

Impulse response convolved with Gaussian with 1, 10, and 20 ns widths



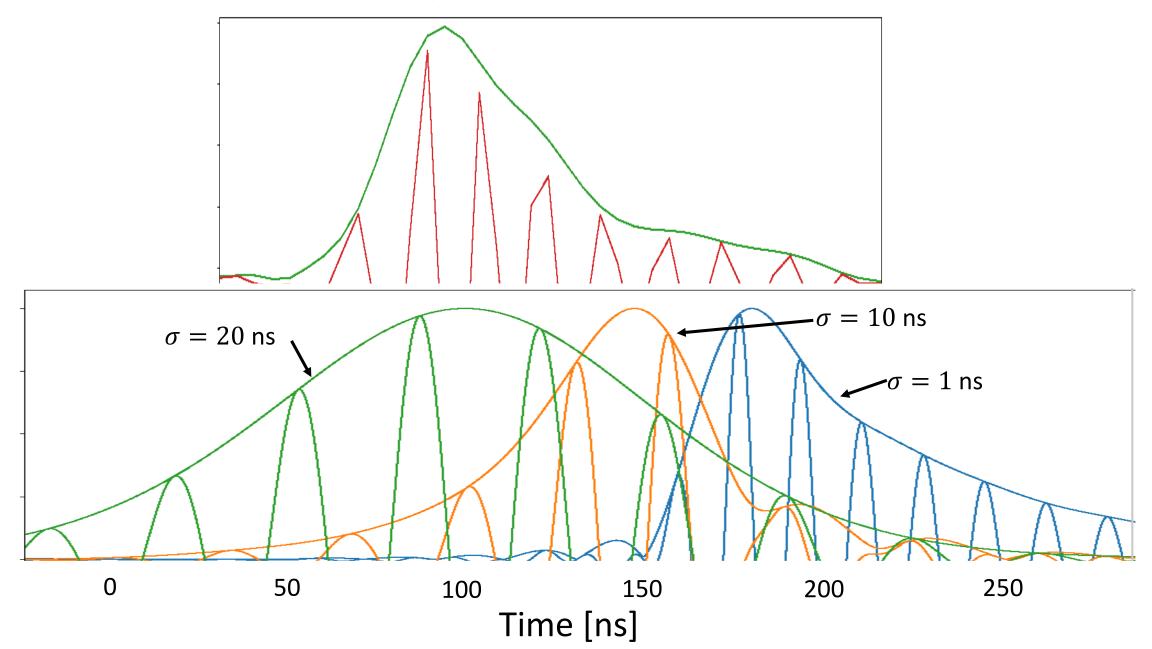
Gaussian σ	Resulting FWHM
1 ns	≈ 50 ns
10 ns	≈ 50 ns
20 ns	≈ 100 ns

Conclusion:

- Signal consistent with impulse response
- Signal must be around 10 ns in duration or shorter

Direct visual comparison on next slide

Antenna Response VS Observed Pulse



What is the source of VHF emission?

Each pulse is due to one streamer

- Only the very strongest streamers visible in VHF
- Vast majority of 2¹⁶ streamers are below noise threshold
- Explains impulsive temporal structure
 - Individual pulses are seen because there are very few of the strongest streamers

Each pulse is many streamers

- Streamers in one pulse would need to occur within 10 ns to explain pulse width
- But there would need to be a waiting time between pulses to explain impulsive nature of the data
- Resulting groups of streamers would then need to occur with a random rate and exponential amplitude spectrum
- No known mechanism for this

Explanation of Spatial Distribution?

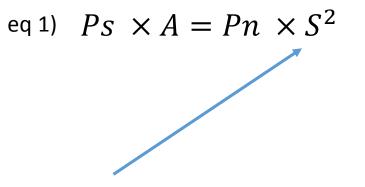
Why do pulses seem to come from one location?

- Our hypothesis:
 - Detected VHF pulses aren't due to typical streamer propagation
 - VHF pulses are made when an ionization wave breaks up into streamers
 - Each new streamer emits a VHF pulse
 - Most pulses are below noise
 - Explains why majority of pulses are from same location

• Other possibilities?

Emitted energy estimate

First we can estimate emitted power density, using noise background to calibrate signal Noise is dominated by galactic background, which has a well-known power spectra



A = sensitivity reduction due to high-zenithal angle ($\approx 1/20$) Pn = known power density due to galactic background $\approx 2 \times 10^{-12} \text{ W/m}^2$

S = signal amplitude relative to noise background (\approx 200) Ps = signal power density in 30-80 MHz band

 S^2 is received power relative to noise background power

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Relate power density to energy

eq 1) $Ps \times A = Pn \times S^2$

eq 2) $E = \tau Ps 4\pi D^2$

au : pulse width (pprox 1 ns)

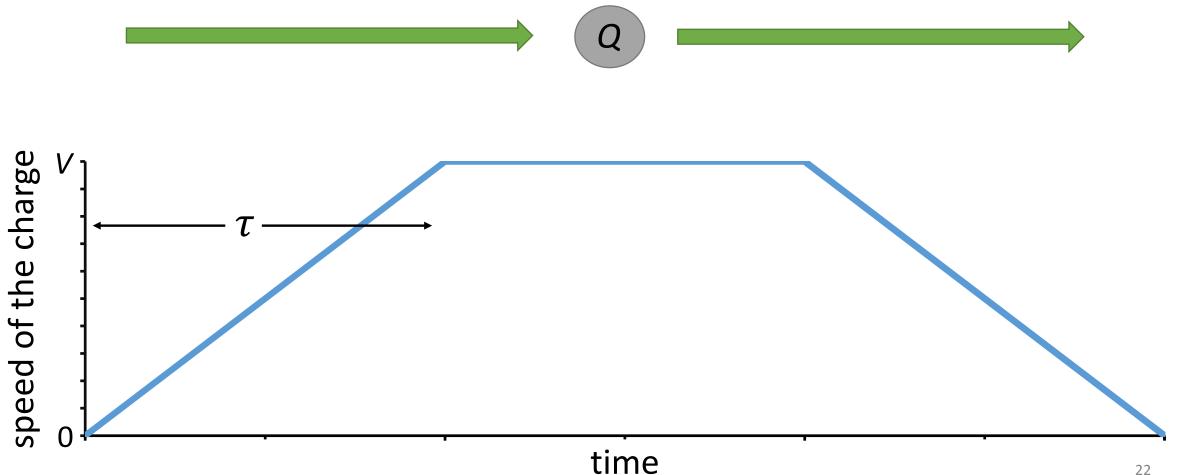
D : distance between antenna and source ($\approx \, 10 \; \rm km$)

E : estimated energy emitted in band

eq 3)
$$E = \frac{\tau Ps \ 4\pi D^2 \ S^2}{A} = 2 \times 10^{-6} \ J$$

Charge Estimate : simple charge model

Assume streamer can be approximated by a charge, Q, that accelerates, moves forward, then deacelerates



Charge Estimate

eq 4)
$$Pq = \frac{1}{(4\pi)^2 \varepsilon_0 c^3} \left(\frac{Qv}{\tau D}\right)^2$$

: emitted power density

D = distance from source (≈ 10 km) V = maximum velocity (≈ 1 mm/ns) τ = acceleration time (≈ 1 ns)

Charge Estimate

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Account for frequency band

eq 5) $Pq \times F = Ps$ F = fraction power in our band (30 – 80 MHz) ≈ 0.1 for pulse width between 1 – 10 ns (order of magnitude)

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Combine equations 1, 4, and 5, and solve for Q

eq 6)
$$Q = 4\pi S \sqrt{\frac{Pn \varepsilon_0 c^3}{A F} \frac{\tau D}{v}} = 8 \ \mu C = 5 \times 10^{13}$$
 electrons