

# Quantum Absolute Sensors for Gravity measurements

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<https://syrte.obspm.fr/spip/science/iaci/>

# Gravimetry & Sensors

$$\vec{g} \quad g = |\vec{g}|$$

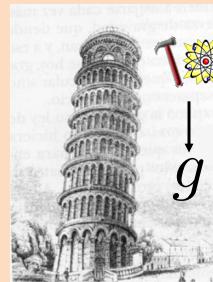
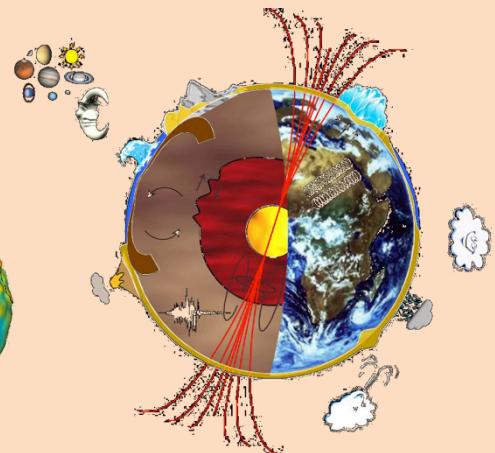
$$1 \mu Gal = \frac{10 nm.s^{-2}}{\sim 10^{-9} g}$$

$$\text{grad } \vec{g}$$

$$1 E = 10^{-9} s^{-2} = 0.1 \mu Gal.m^{-1}$$

## Geophysical studies

*Crustal deformations,  
mass changes, geoid, ...*

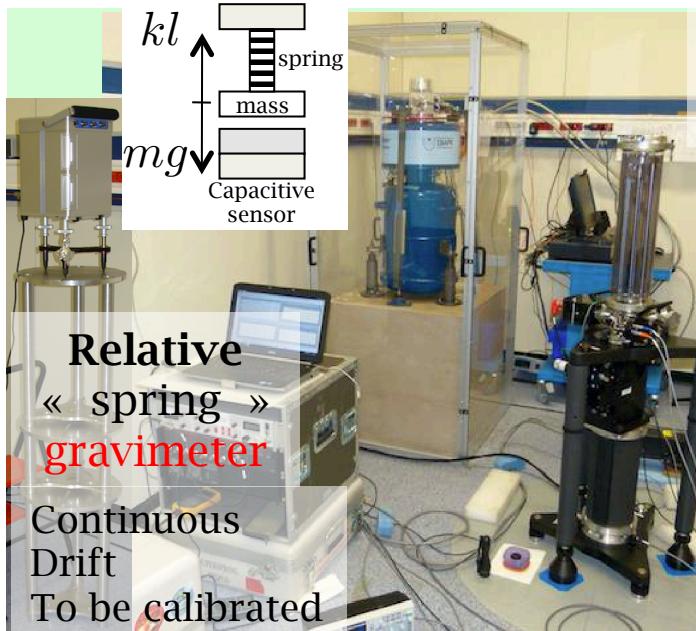


**Tests of Fundamental physics**  
*G, equivalence principle*

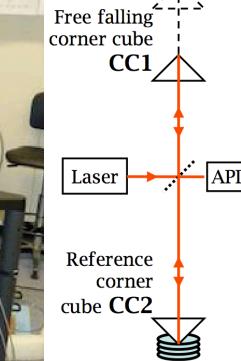


## Metrology

*Redéfinition du kg,  
Kibble balance*



**Absolute  
Free Fall Corner  
Cube gravimeter**



Not continuous  
(0.3 Hz)  
dead time,  
#FF limited  
(mechanical  
wear)

$$U \sim 20 - 30 nm.s^{-2} \\ \sim 10 nm.s^{-2} \text{ in } 90 \text{ s}$$

**FTG (Lockheed  
Martin)**



**EGG (ARKEX)**



**Gradiometers:** Combination of  
accelerometers, (gyro  
stabilized plateform),  
Electrostatic, superconducting

Differential measurements

$$FTG : 20 - 2 E.Hz^{-1/2}$$

$$SG : 0.5 E.Hz^{-1/2}$$

$$GOCE : \sim 10 mE.Hz^{-1/2}$$

**GOCE (ESA)**

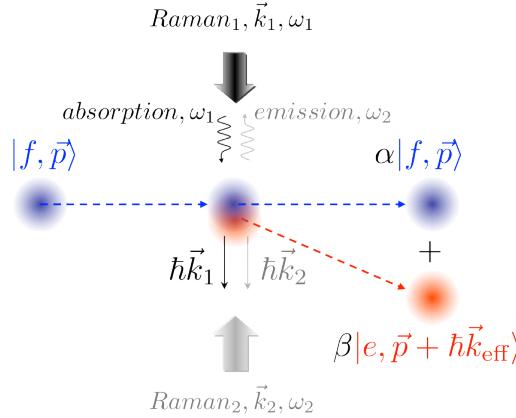
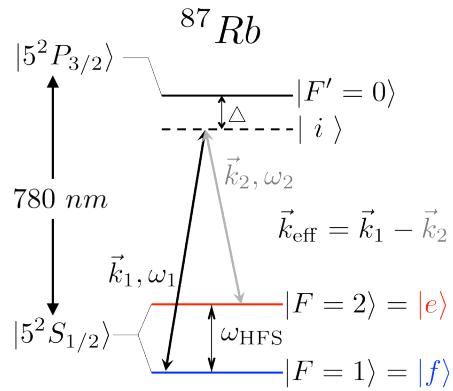


**VK1 (UWA)**

# Atom interferometer

Stimulated Raman transitions

3 level atom



Two photon transition coupling  $|f\rangle$  and  $|e\rangle$

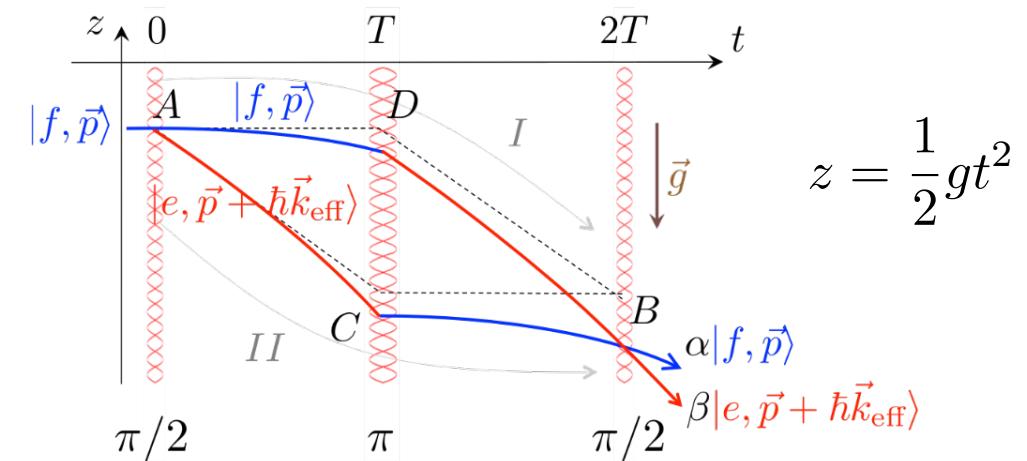
$$\phi(t) = \omega_{\text{eff}}t - \vec{k}_{\text{eff}}\vec{z}(t) + \varphi_{\text{eff}}(t)$$

**Interest of Raman transitions:**

Bijection internal - external state

**Consequence :** detection on internal state

*Sampling of the positions at the 3 pulses*



$$P_{|\vec{p}\rangle \rightarrow |\vec{p} + \hbar \vec{k}_{\text{eff}}\rangle} = \frac{1}{2}(1 - C \cos \Delta \Phi)$$

$$\begin{aligned} \Delta \Phi &= \Phi_{II} - \Phi_I \\ &= (\phi_A - \phi_C) - (\phi_D - \phi_B) \\ &= \phi(0) - 2\phi(T) + \phi(2T) \end{aligned}$$

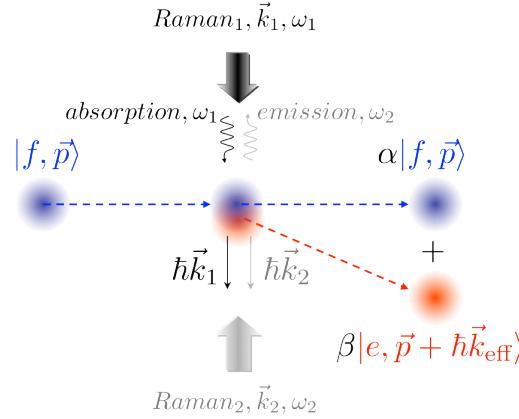
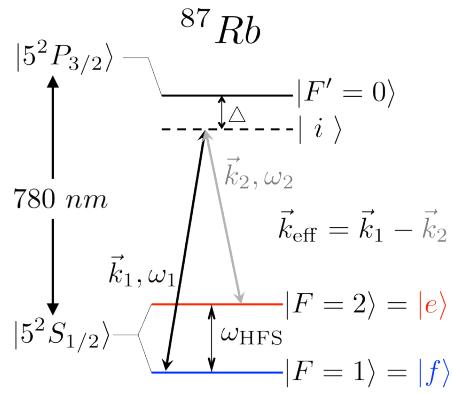
$$\Delta \Phi = -\vec{k}_{\text{eff}} \vec{g} T^2$$

Scales as  $T^2$ , benefits of cold atoms

# Atom interferometer

Stimulated Raman transitions

3 level atom



Two photon transition coupling  $|f\rangle$  and  $|e\rangle$

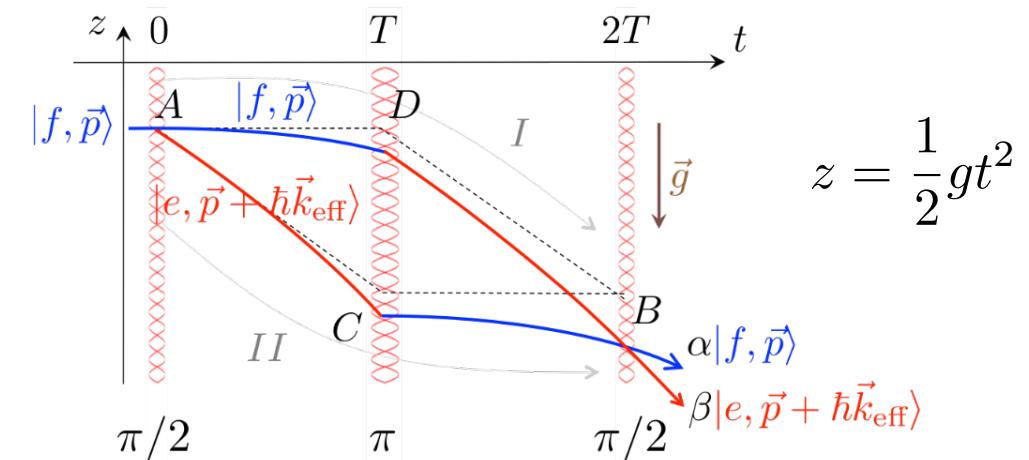
$$\phi(t) = \omega_{\text{eff}}t - \vec{k}_{\text{eff}}\vec{z}(t) + \varphi_{\text{eff}}(t)$$

**Interest of Raman transitions:**

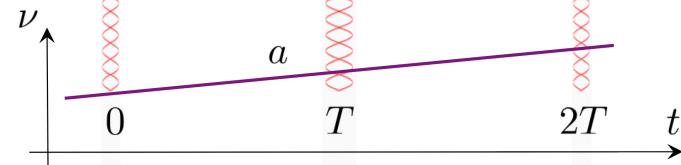
Bijection internal - external state

**Consequence :** detection on internal state

*Sampling of the positions at the 3 pulses*



$$P_{|\vec{p}\rangle \rightarrow |\vec{p} + \hbar\vec{k}_{\text{eff}}\rangle} = \frac{1}{2}(1 - C \cos \Delta\Phi)$$



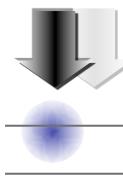
$$\Delta\Phi = -\vec{k}_{\text{eff}}\vec{g}T^2 + aT^2$$

$$g = a/k_{\text{eff}}$$

Scales as  $T^2$ , benefits of cold atoms

# Cold Atom Gravimeter (CAG) sequence

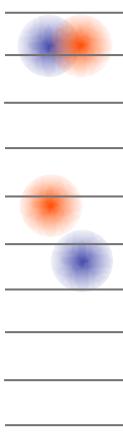
Extinction PMO-3D



Laser 1

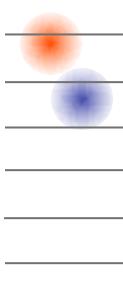
Bring two lasers in a co-propagating way and retroreflect them on a mirror

Impulsion 1 :  $\pi/2$



$$z(0) = 0$$

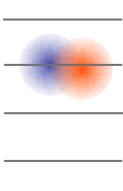
Impulsion 2 :  $\pi$



$$z(T) = \frac{1}{2}gT^2$$

Position of the equiphases defined by the mirror position

Impulsion 3 :  $\pi/2$



$$z(2T) = 2gT^2$$

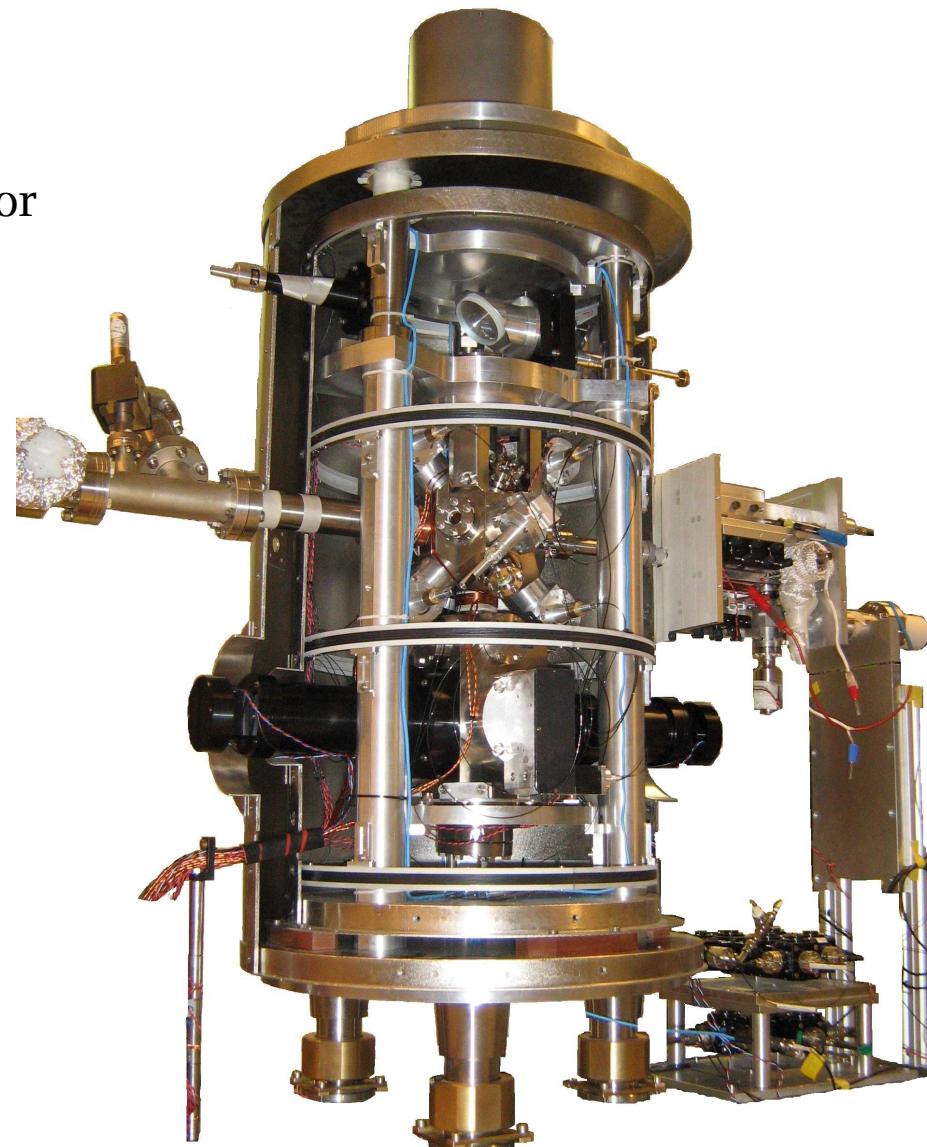
Detection



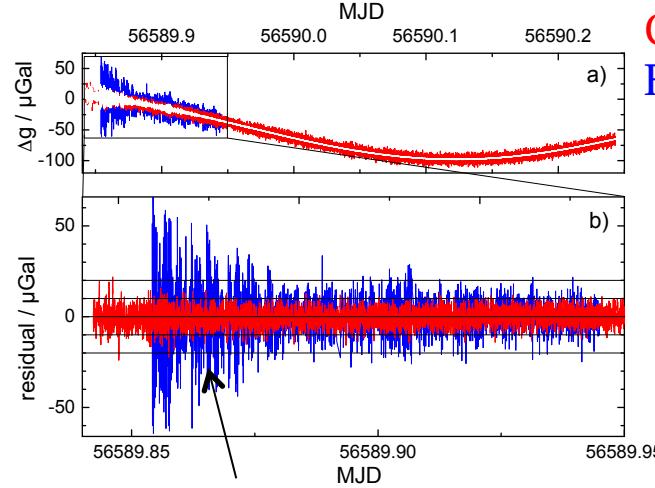
Mirror

Laser 2

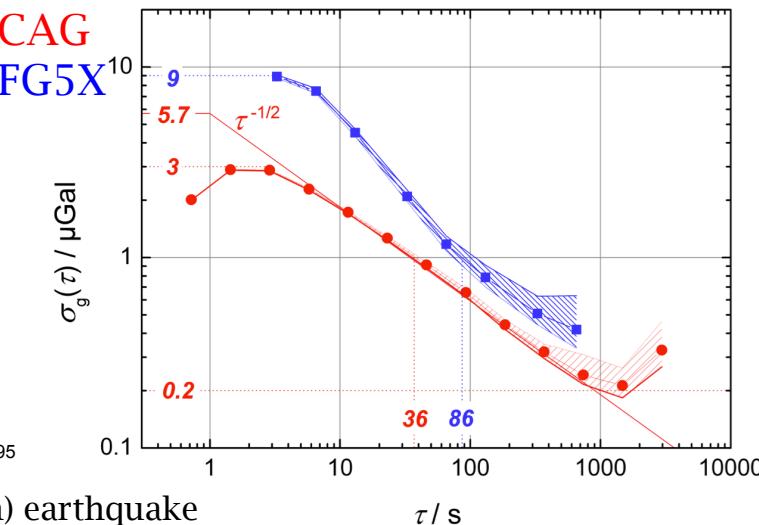
atomic measurement  
= measure of the relative displacement atoms/mirror



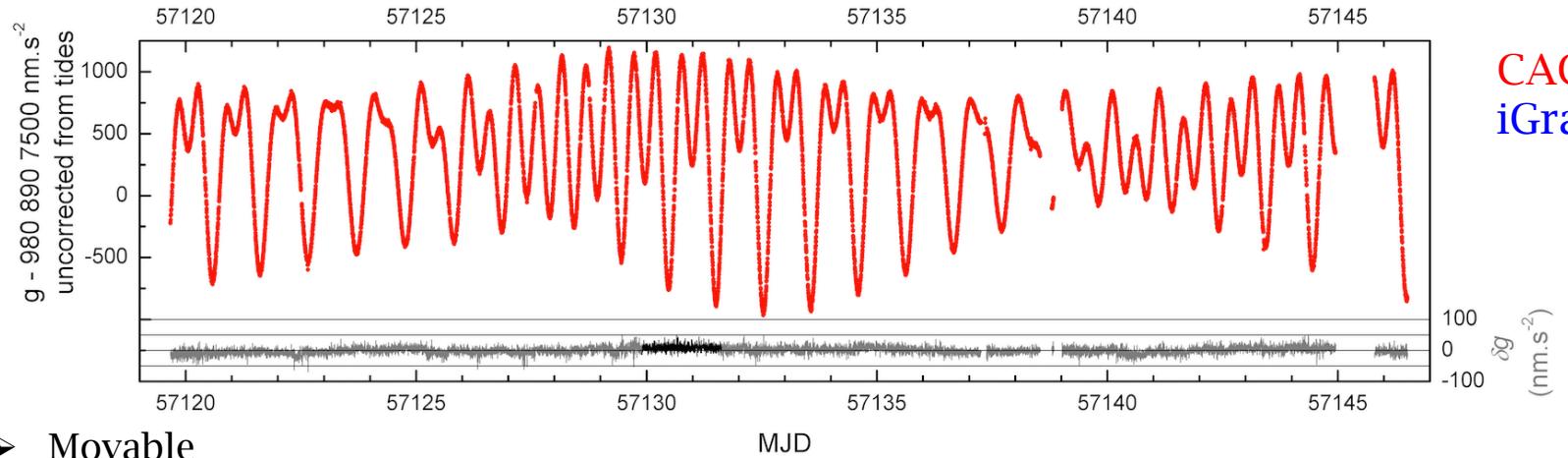
# CAG performances & capabilities



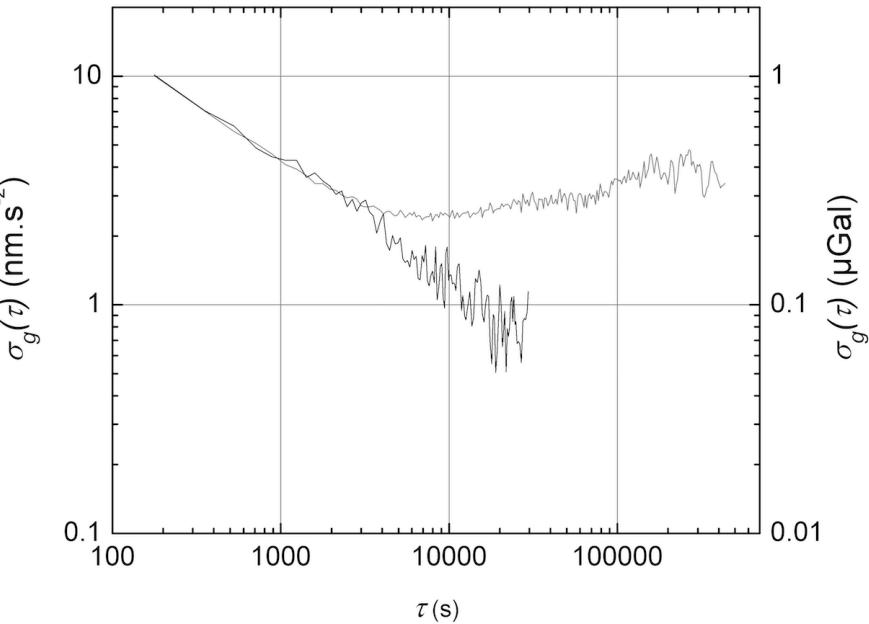
Excess noise due (end of an) earthquake  
Better immunity of the CAG



P. Gillot et al., Metrologia 51 (2014)



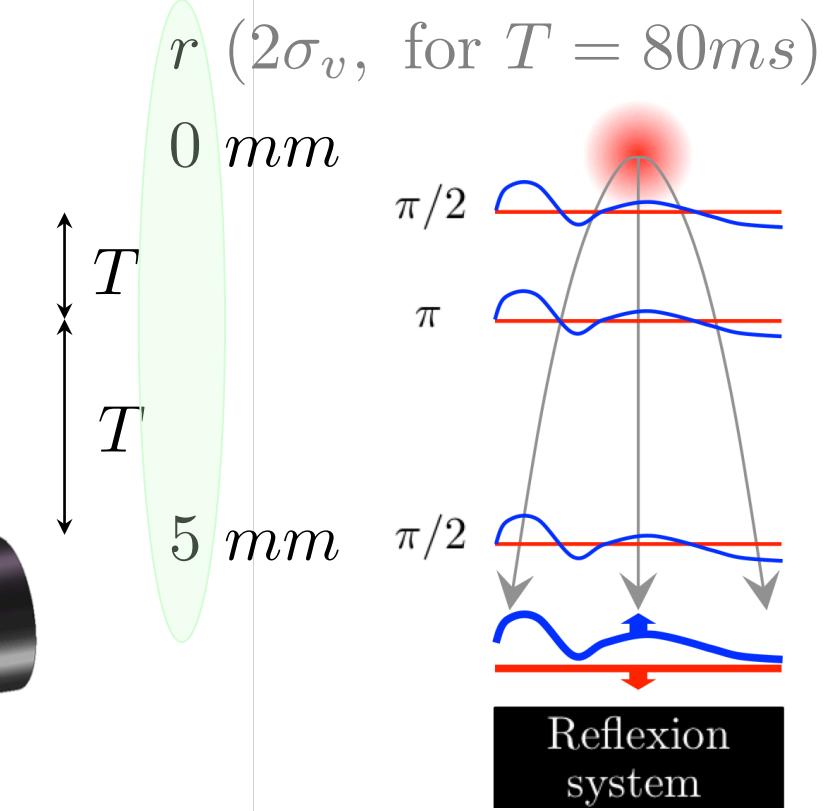
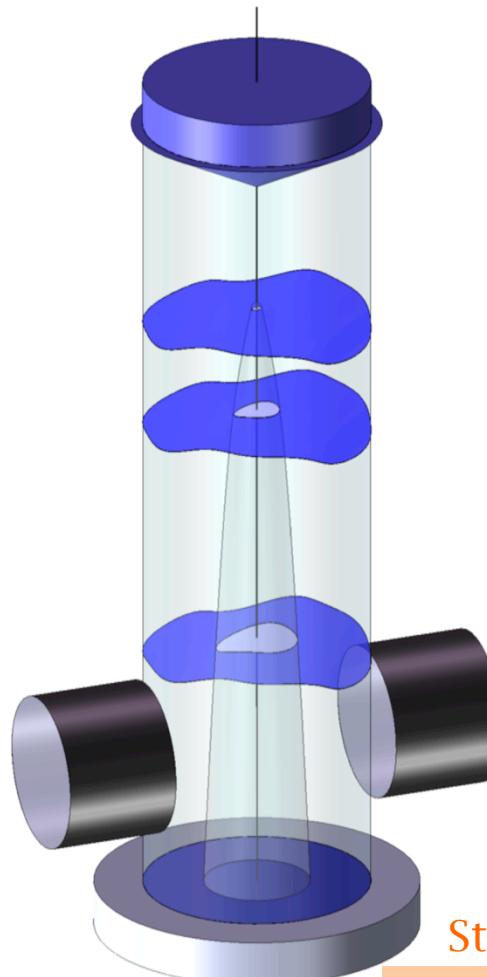
CAG  
iGrav



- Movable
- Comparison with other technologies
- Participation to international Key Comparisons
- Continuous accurate measurement
- Industrial transfer

# Wavefront distortion and cloud expansion

Cold Atoms  
 $T_{emp} \sim 2\mu K$   
 $\sigma_v \sim 14 \text{ mm.s}^{-1}$



Following an atomic trajectory the total phase coming from wavefront imprinted at each pulse is non zero due to the ballistic expansion of the atomic cloud.

Study case: curvature

$$\phi \sim Kr^2 \quad \Delta\Phi = 2K\sigma_v^2 T^2 = \frac{k_{\text{eff}}}{R} \frac{k_B T_{emp}}{m_{\text{Rb}}} T^2$$

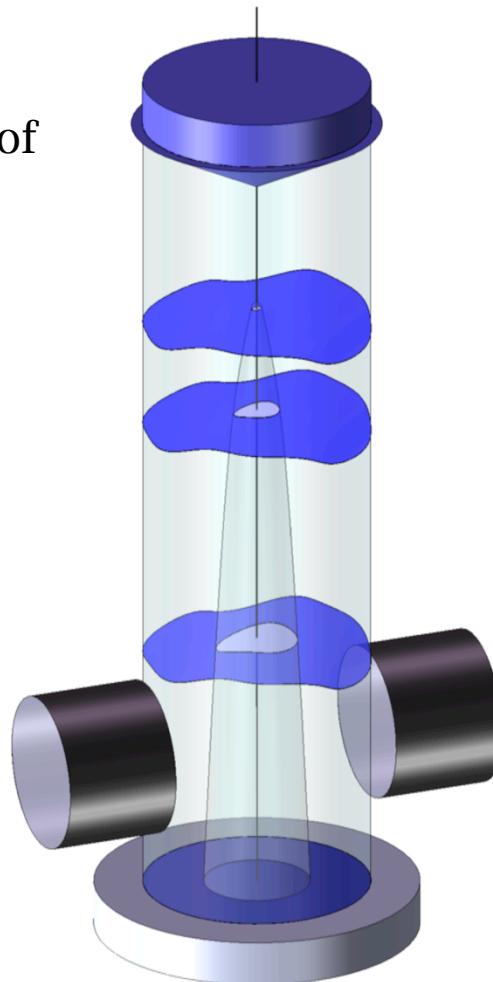
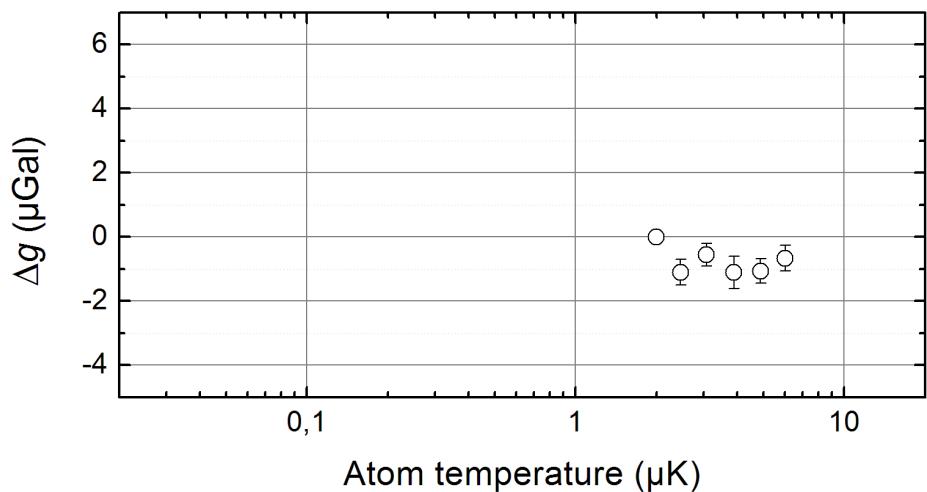
for  $\Delta g = 10^{-9}g$ ,  $R = 20\text{km}$ ,  $\lambda/300 \text{ PV}$  ( $2r = 1\text{cm}$ )

# Wavefront Bias determination

Previous determination:

Increase the temperature to modify the effect of  
**wavefront aberrations**

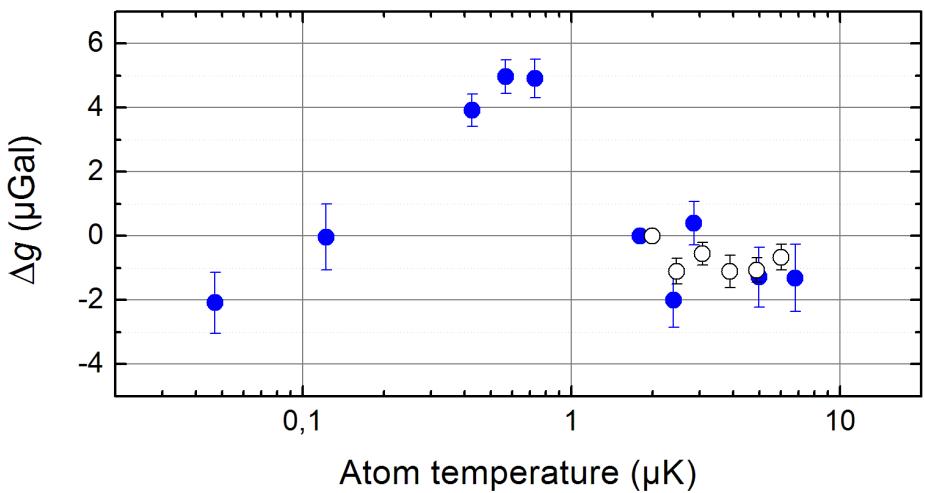
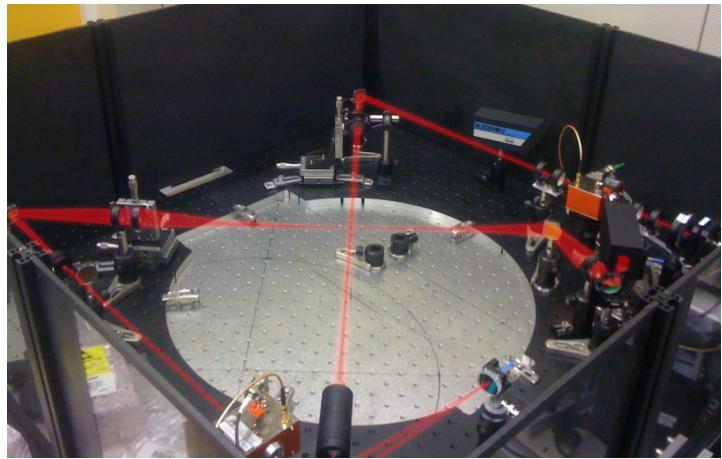
*A.Louchet-Chauvet et al New J. Phys. 13, 065025 (2011)*



$$\Delta g = (0 \pm 4) \mu\text{Gal}$$

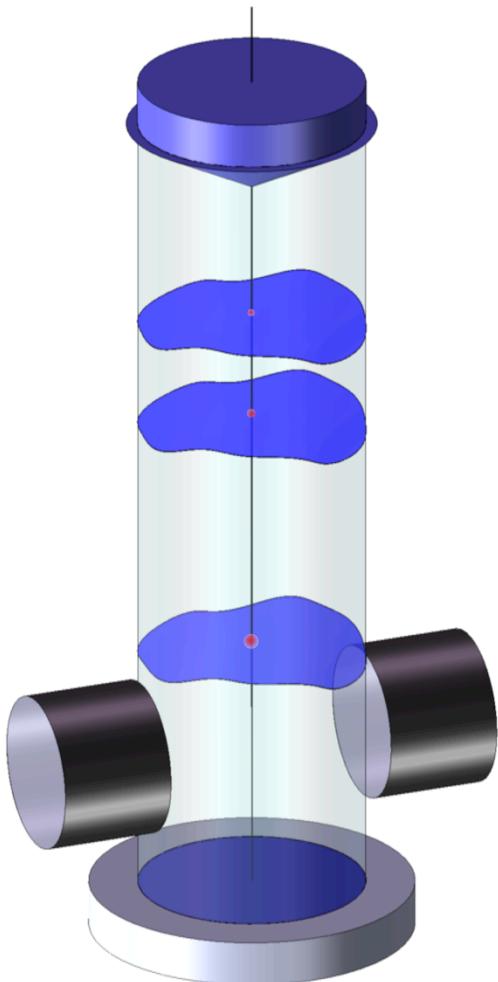
Effect	Bias $\mu\text{Gal}$	$u$ $\mu\text{Gal}$
Alignments	0.3	0.5
Frequency reference	0.5	<0.1
RF phase shift	0.0	<0.1
$v_{gg}$	-13.4	<0.1
Self gravity effect	-2.1	0.1
Coriolis	-5.3	0.8
Wavefront aberrations	0.0	4.0
LS1	0.0	<0.1
Zeeman	0.0	<0.1
LS2	-3.6	0.8
Detection offset	0.0	0.5
Optical power	0.0	0.5
Cloud indice	0.4	<0.1
Cold collisions	<0.1	<0.1
CPT	0.0	<0.1
Raman $\alpha$ LS	0.3	<0.1
Finite Speed of Light	0.0	<0.1
<b>TOTAL</b>	<b>-22.9</b>	<b>4.3</b>

# Implement Ultracold Source on CAG



Differential gravity measurements as a function of the atomic temperature from 50nK to 7μK

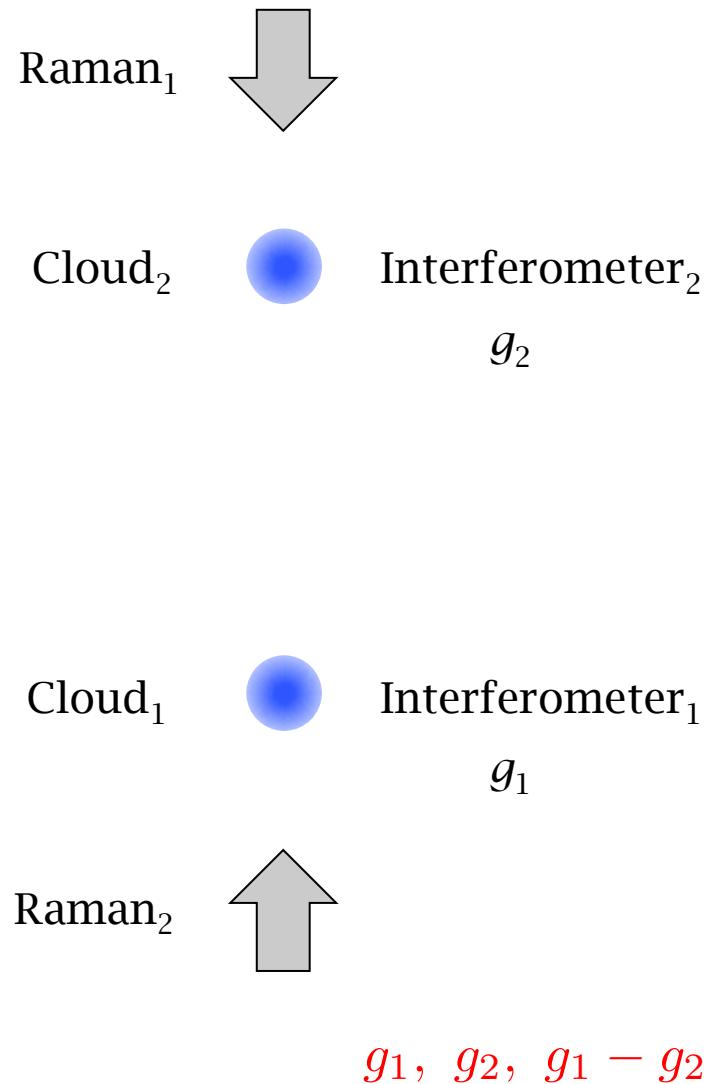
R. Karcher et al., New J. Phys. 20 (2018) 113041



$$\Delta g = (-5.3 \pm 1.3) \mu Gal$$

Effect	Bias μGal	u μGal
Alignments	0.3	0.5
Frequency reference	0.5	<0.1
RF phase shift	0.0	<0.1
$v_{gg}$	-13.4	<0.1
Self gravity effect	-2.1	0.1
Coriolis	-5.3	0.8
Wavefront aberrations	-5.6	1.3
LS1	0.0	<0.1
Zeeman	0.0	<0.1
LS2	-3.6	0.8
Detection offset	0.0	0.5
Optical power	0.0	0.5
Cloud indice	0.4	<0.1
Cold collisions	<0.1	<0.1
CPT	0.0	<0.1
Raman α LS	0.3	<0.1
Finite Speed of Light	0.0	<0.1
<b>TOTAL</b>	<b>-28.5</b>	<b>2.0</b>

# Quantum dual gravi-gradio meter



- Simultaneous interferometers on two cold atom clouds with common Raman lasers
- Differential measurement allows for extracting the acceleration difference (and thus the Earth gravity gradient)
- Suppression of common mode noise, and in particular of the vibration noise
- Adapted for onboard measurements
- $g$  and  $\Delta g$ : resolve ambiguities in determination of mass and position

How to increase the sensitivity ?

$$\Delta\Phi = \vec{k}_{\text{eff}} \vec{g} T^2$$

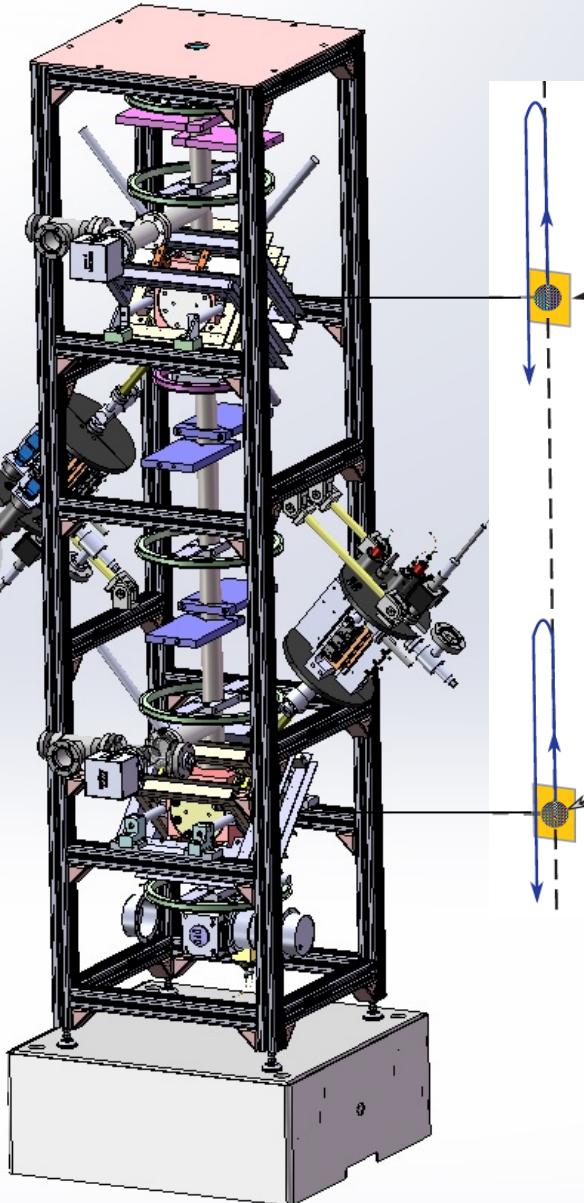
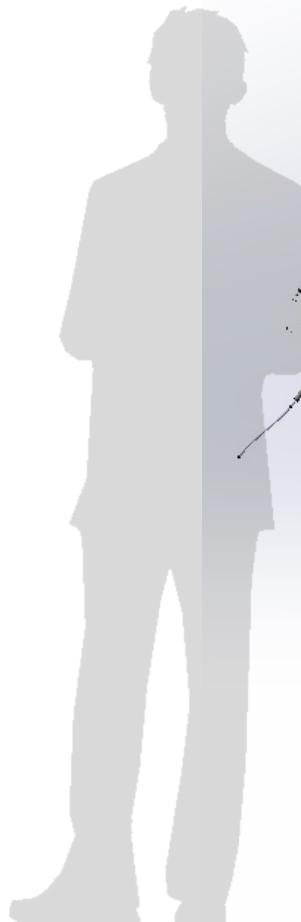
↑      ↑

Increase the scale factor

New tools

- High order Bragg diffraction LMBS with up to N photons
- Ultracold atoms  
Fast generation on atom chip

# Quantum dual gravi-gradio meter



- 2 ultracold Rb clouds obtained on 2 chips
- 2 clouds launched with elevator
- 2 Interferometers driven by LMTB

Targeted parameters

$$T_c = 2s \quad N_{\text{atoms}} = 5 \cdot 10^5$$
$$T_{emp} = 10 - 100 nK$$
$$p = 100 \hbar k \quad 2T = 0.5s$$

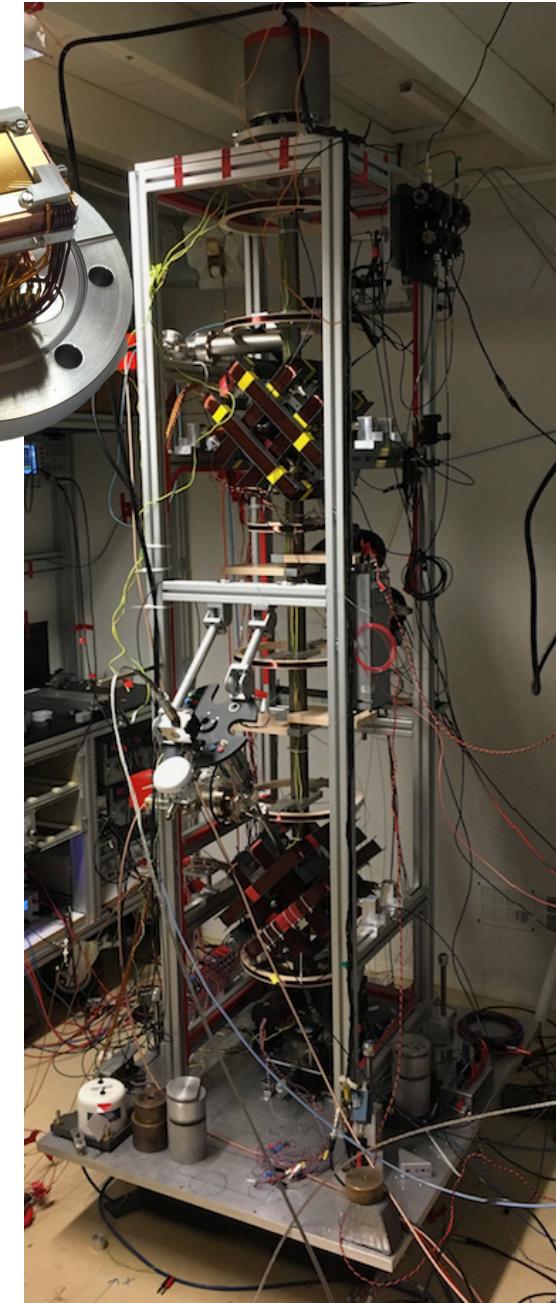
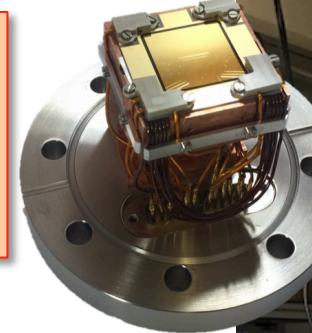
$$\sigma_g^1 = 9 \times 10^{-11} m.s^{-2}.Hz^{-1/2}$$

If limitated by QNP

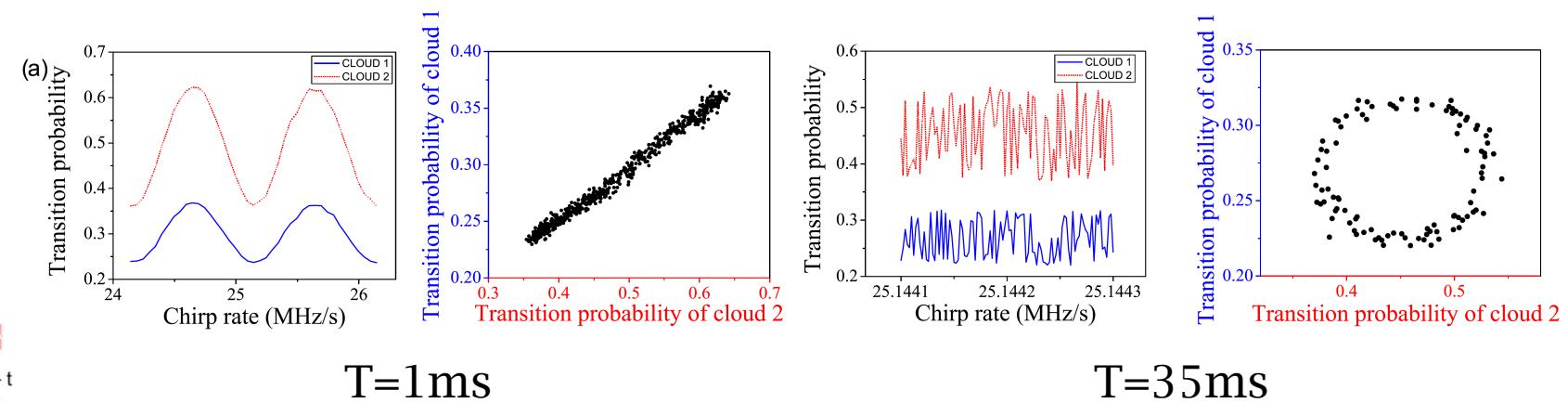
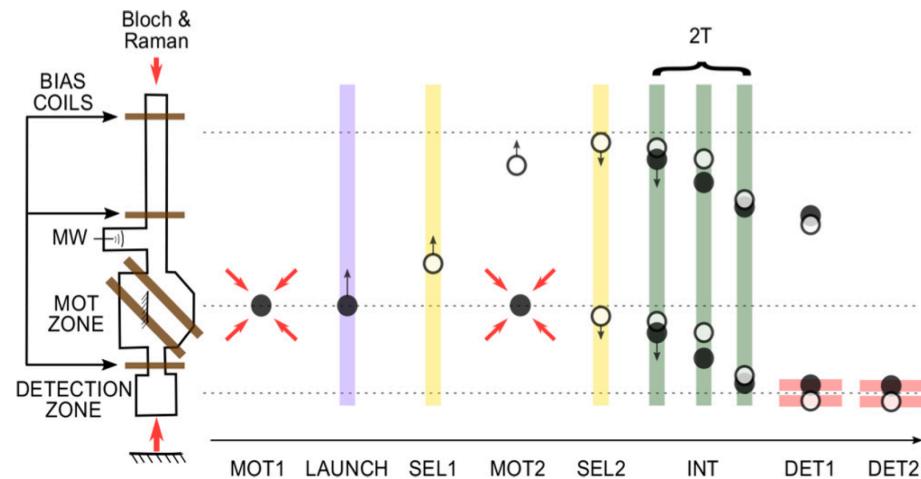
$$\Delta z = 1m$$

$$\sigma_{\text{gradg}} = 126 \text{ } mE @ 1s$$

More than one order of magnitude better than state of the art



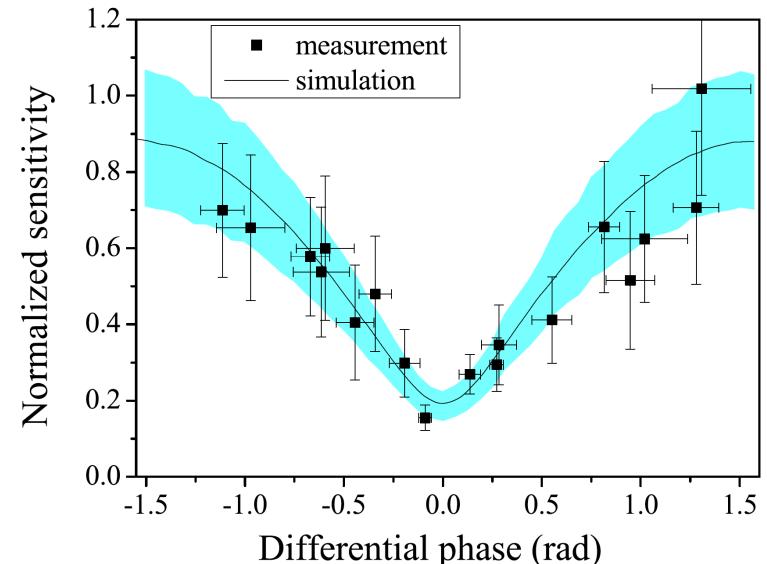
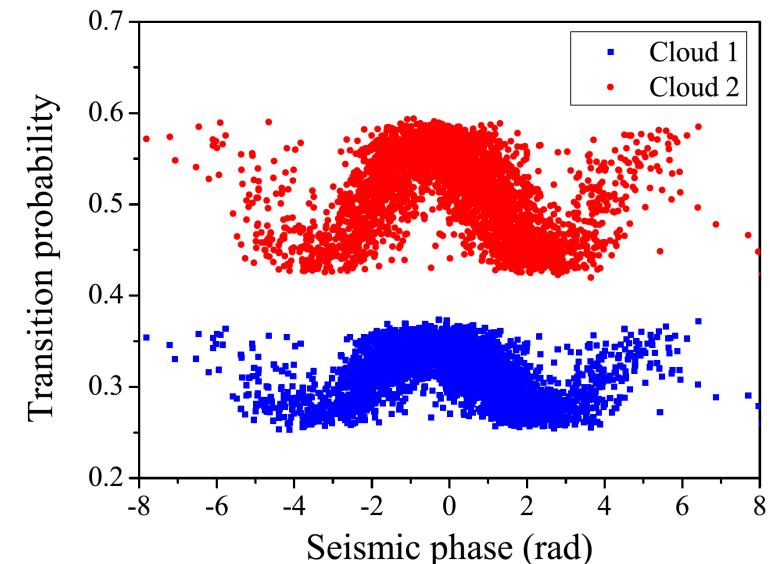
# Quantum dual gravi-gradio meter, first results



$T=1\text{ms}$

$T=35\text{ms}$

$T=60\text{ms}$

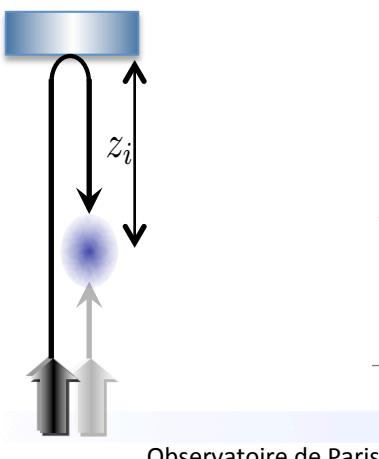
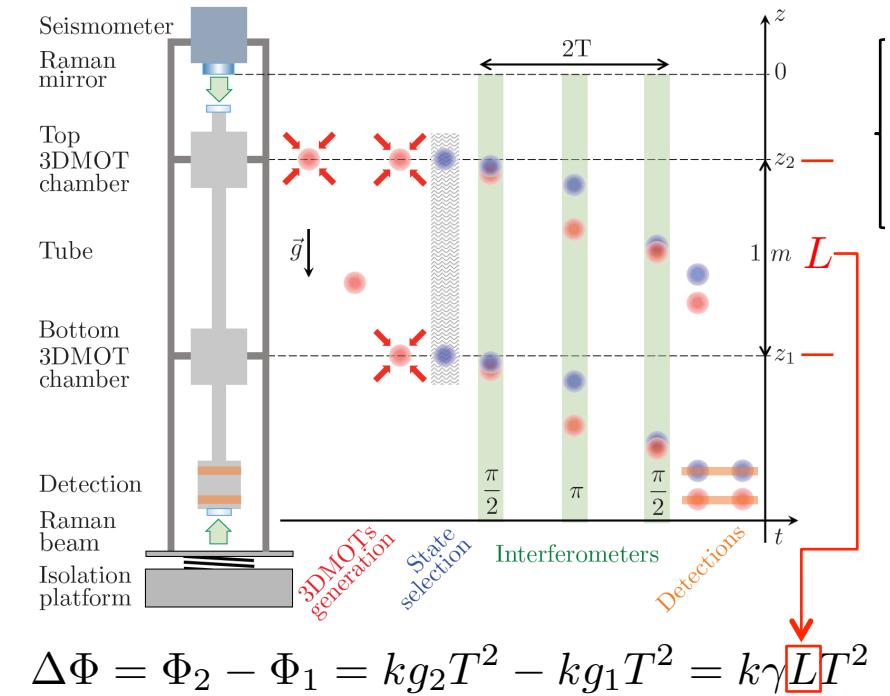


Use of a seismometer

$$P_i = A_i + \frac{C_i}{2} \cos(D_i \Phi_{\text{vib},s} + \Phi_i)$$

M. Langlois et al., Phys. Rev. A 96 053624 (2017)

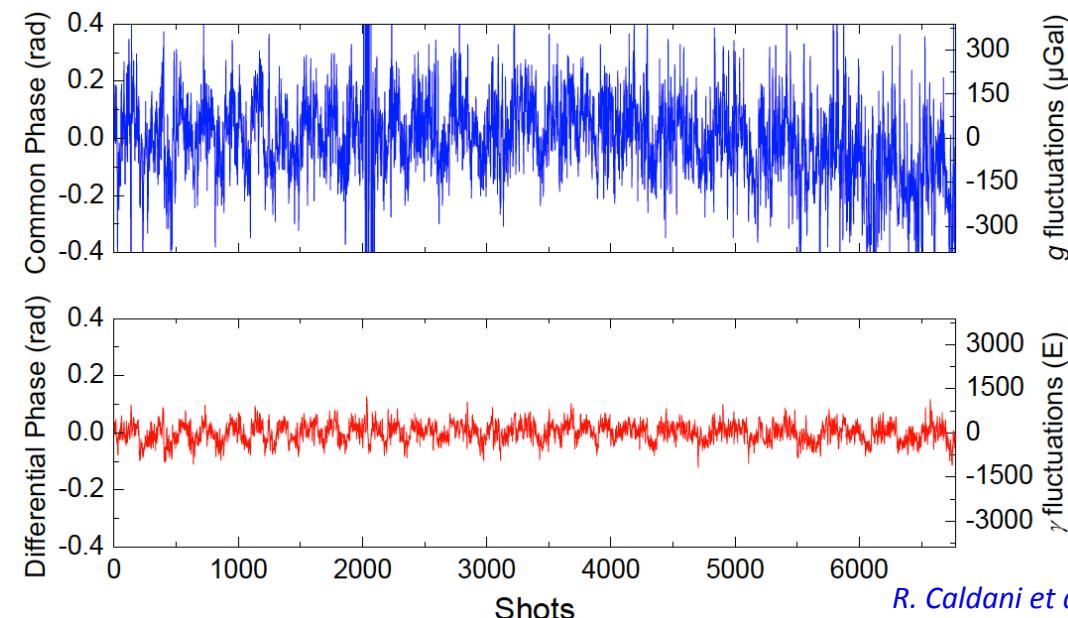
# Quantum dual gravi-gradio meter, first results



$$\Phi_i = kg_i T^2 + aT^2 + K_i \Delta\nu \quad \begin{cases} \Delta\Phi_i^{FC} = aT^2 \\ \Delta\Phi_i^{FJ} = K_i \Delta\nu \end{cases}$$

$$\left. \begin{array}{l} \Delta\Phi = 0 \rightarrow \Delta\nu_0 = \frac{k(g_1 - g_2)T^2}{K_2 - K_1} \\ \Phi_1 = \Phi_2 = 0 \rightarrow 2\pi a_s = -k \left( \frac{K_2 g_1 - K_1 g_2}{K_2 - K_1} \right) = -kg_s \end{array} \right\} \frac{K_i = 8\pi z_i/c}{g_i = g_0 + \gamma z_i} \quad \left. \begin{array}{l} \Delta\nu_0 = -\gamma \frac{kT^2 c}{8\pi} \\ a_s = -kg_0 \end{array} \right\}$$

**Accurate** determinations of **both** the gravity acceleration (at the mirror position) and the gravity gradient, **INDEPENDANT OF THE BASELINE L**



Collaboration with Muquans, see D1741 EGU2020-9185 7<sup>th</sup> of may G.4.2

# Conclusions and Prospects

Quantum gravimeter demonstrated **accurate** and **continuous**  $g$  measurements in **a single instrument**.

*$g$  in  $h_{\text{LNE-2017}}$ , taken into account by CODATA for  $h_{\text{2018}}$  for new kg definition  
Measurement included in French geoïde.*

International and National comparisons done to guarantee users and stakeholders .

QAI are now suitable for applications previously limited to superconducting gravimeters and/or free fall corner cube gravimeters.

AI technology transferred to industrie, commercial instruments already exist.

see D1574 EGU2020-8969 G.4.4

see D1566 EGU2020-9076 G.4.4

Performances will be improved with UC atoms, opening the « sea of problems » and new applications.  
→ **sub- $\mu$ Gal objective**

Dual **Gravi-Gradio** sensor under development. *The measurement of both quantities, which depend differently on the masses and their positions, will allow to resolve ambiguities between masses and positions of gravity anomaly sources.*

see D1741 EGU2020-9185 7<sup>th</sup> of may G.4.2

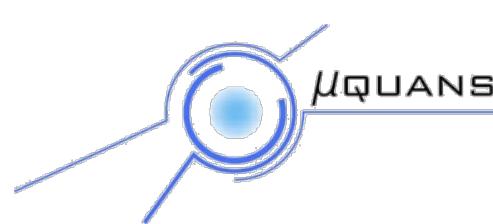
Onboard gravity mapping will soon be possible with UC atoms gradiometers based on LMBS.

- Why not going to space ?
- Atoms are free falling but satellites also, (increase of T up to 10s?), 2T=5s, **2mE@1s**

<https://syrte.obspm.fr/spip/science/iaci/>

<https://syrte.obspm.fr/spip/science/iaci/publications/>

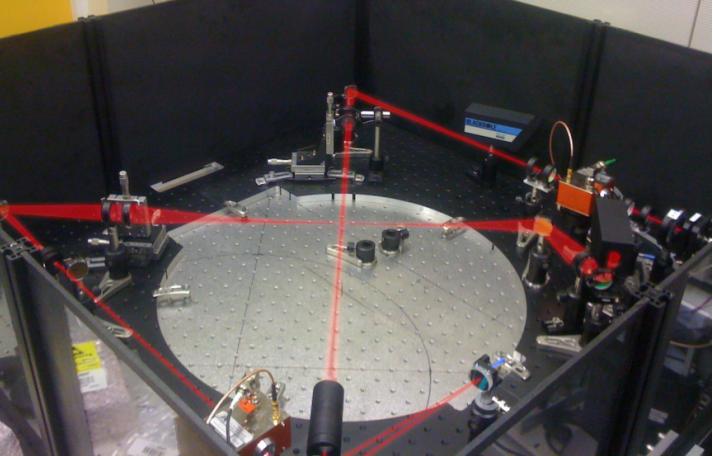
# Thank you



<https://syrte.obspm.fr/spip/science/iaci/>  
<https://syrte.obspm.fr/spip/science/iaci/publications/>

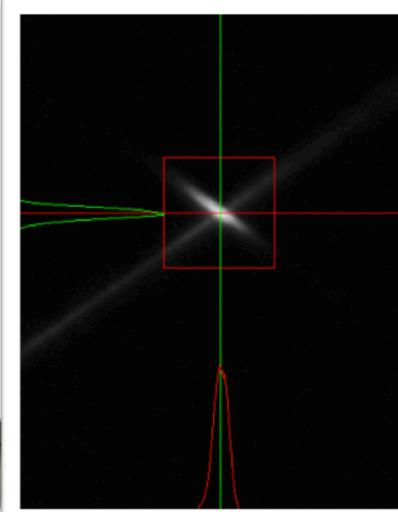
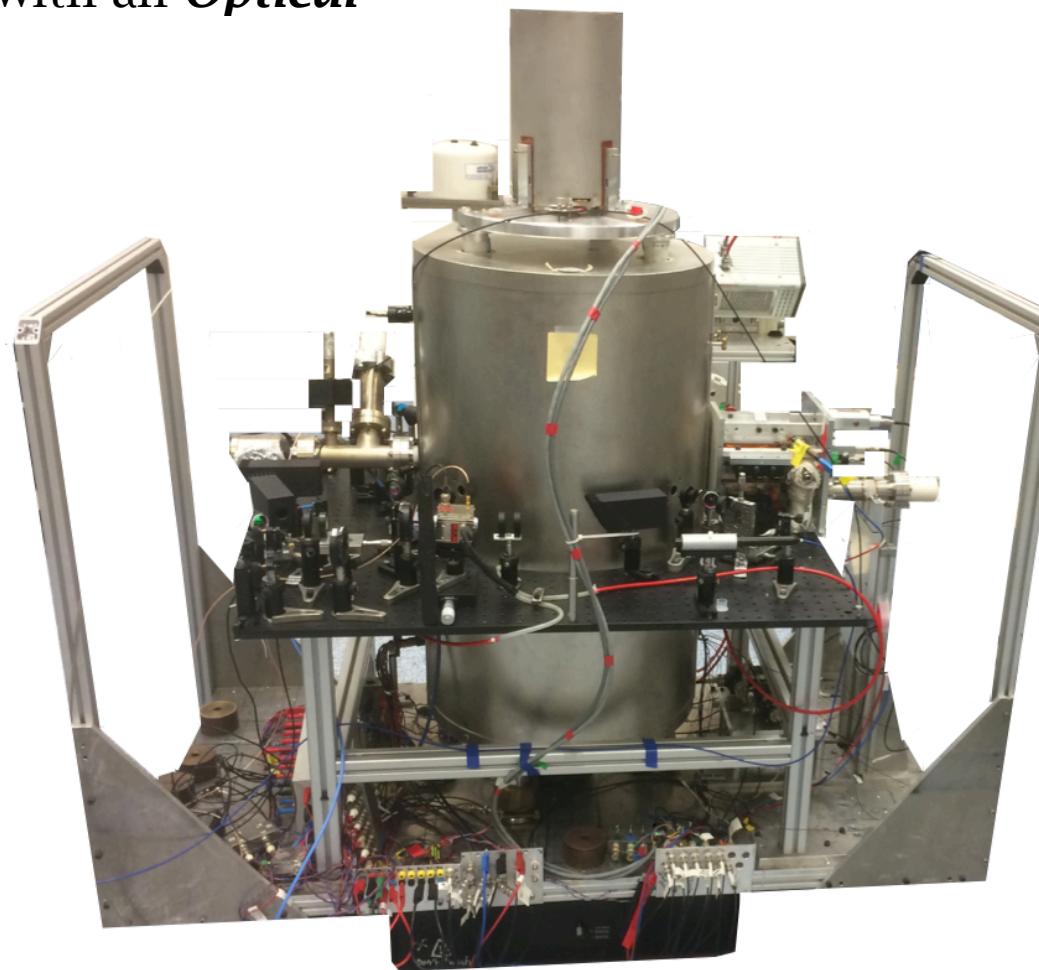
# Implement Ultracold Source on CAG

*Evaporative cooling* and *trapping* techniques with an *Optical Dipole Trap*



## Parameters :

- A crossed dipole trap , total depth :  $680 \mu\text{K}$
- Laser Kheopsys 1550 nm, 30 W
- First arm **for large volume**  $P = 14.8 \text{ W}$ , waist =  $170 \mu\text{m}$
- Second arm **for tight confinement**  $P = 8 \text{ W}$ , waist =  $27 \mu\text{m}$



Access to a wide range of temperature from **50nK to 10 $\mu\text{K}$**

# Comparison with other gravimeters

Type	Techno	Institut / Company	Name	$\nu_c$ Hz	u $\mu\text{Gal}$	u <sub>wfab</sub> $\mu\text{Gal}$	$\sigma_g$ $\mu\text{Gal}$	$\tau$ s	Rq
Abs	FFCC	Micro-g	FG5X	0.3	2.0	.	~ 1.0	~ 100	dead time, wearing
		Lacoste		0.1	.	.	1.0	~ 700	
Rel	Supra	GWR	iGrav	1.0	.	.	0.01	600	drift
Abs	Atom	SYRTE	CAG	2.8	2.0	1.3	5.7	1	T=80ms dropped atoms
				.	.	.	1.0	36	
				.	.	.	0.06	20 000	
Abs	Atom	HUB	GAIN	0.7	3.2	2.2	9.6	1	T=260ms launched atoms
				.	.	.	1.0	100	
				.	.	.	0.05	100 000	
Abs	Atom	HUST	AQG	0.5	5.0	.	4.2	1	T=300ms launched atoms
				.	.	.	1.0	18	
				.	.	.	0.3	200	
Abs	Atom	muquans	AOSense	.	.	.	59.4	1	dropped atoms
				.	.	.	1.0	4000	
				.	.	.	0.3	200 000	
Abs	Atom	M Squared		.	.	.	.	.	