



## One Candidate Mechanism of Low-Frequency Oscillation - Coriolis Parameter Variance Associated with Latitude

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Although there being a notion that the atmosphere is not determinedly predictable beyond a few weeks due to that non-integrable properties of the atmosphere may produce chaos, but recent some papers have confirmed the facts of oscillation of low-frequency existing in atmosphere, such as Blocking; MJO, Kelvin Wave and Monsoon Trough whose vary periodicities is various from one week to 70 days, some of them especially perform eastward-propagation from tropical ocean, however, what mechanism exactly of this kind of low-frequency vibration still remain unclear hitherto, at least is not agreed unanimously among scientists, so this issue motivate many researcher to do further studying the cause of atmospheric low-frequency fluctuation, particularly paying attention to large-scale persistent flow patterns. So as to explore and explain low-frequency phenomenon here the model is employed to establish a nonlinear differential equation based on the Non-Equilibrium between geostrophic force and pressure gradient force, therefore, the one-dimension nonlinear differential equation may be expressed like below:

$$L \frac{d^2\theta}{dt^2} = (2\Omega V \sin \varphi - \frac{1}{\rho} \frac{\partial p}{\partial x}) \cos \theta + (g - \frac{1}{\rho} \frac{\partial p}{\partial z}) \sin \theta \quad (1)$$

Here  $x$  the zonal coordinate;  $z$  the vertical coordinate;  $L$  equal to the earth radius ( $R_e$ ) added by altitude of middle level in troposphere; undoubtedly  $L$  is approximately  $R_e$ ; meridian wind is  $V$ ;  $g$  being the acceleration of gravity;  $2\Omega \sin \varphi$  is just Coriolis parameter ( $f$ );  $p$  is pressure;  $t$  is time;  $\rho$  is air density;  $\theta$  denote the angle between two line of earth radius of the cone fixed in the center of earth,  $\theta$  is also oscillation angle. Using the approach of linearization and series then the periodicity of low-frequency geostrophic waver may be calculated by below formula (2).

$$T = \frac{2\pi}{\sqrt{\frac{\bar{\theta}}{L} (2\Omega V \sin \varphi - \frac{1}{\rho} \frac{\partial p}{\partial x})}} \quad (2)$$

$\bar{\theta}$  is about 1.0, the rest symbols is same as equation (1) above, besides  $\partial p / \partial x = 1 \text{ hPa/300 km}$ ;

$\rho = 1.3 \text{ kg} \cdot \text{m}^{-3}$ ;  $V = 8 \text{ m} \cdot \text{s}^{-1}$ ;  $\Omega = 7.3 \times 10^{-5} \text{ s}^{-1}$ ;  $L \approx R_e = 6.378 \times 10^6 \text{ m}$ ;  $\varphi$  is different latitude from 12.8 to 80, so the various periodicities of low frequency vibration calculated via formula (2) is showed in follow table 1.

Table 1 the periodic oscillation associated with latitudes

|                           |              |    |    |    |    |    |    |    |     |     |
|---------------------------|--------------|----|----|----|----|----|----|----|-----|-----|
| Latitude(°N)              | 12.8         | 14 | 15 | 20 | 30 | 40 | 50 | 60 | 70  | 80  |
| Period (days)             | 70           | 42 | 34 | 21 | 14 | 11 | 10 | 9  | 8.7 | 8.4 |
| $\partial p / \partial x$ | 1 hPa/300 km |    |    |    |    |    |    |    |     |     |

Main conclusion: (Eq. 1) owing to the existing probability of absolute geostrophic balance almost reaches zero in real atmosphere, so that in most cases non-geostrophic equilibrium dominate in the atmosphere, or is often referred as quasi-geostrophic equilibrium which is ubiquitous in real atmosphere, this is possibly one source of low-frequency oscillation; (Eq. 2) it is inferred that low frequency oscillation (30-70days) initiate from tropical region (low latitude), especially commence from tropical ocean area; relatively, shorter periods of oscillation (one week or so) originate from high latitude; furthermore, there is exist of two weeks-oscillations in mid-latitude.(3)

depending on a properties of continuous medium in atmosphere, the so-called "high frequency" of shorter than one week similar to Rossby wave trains generally propagate possibly from high-latitude toward to low-latitude.