

Molecular escape of H₂ from Titan's atmosphere: kinetic Monte Carlo simulations

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Abstract

A molecular model of H₂ diffusion through a static background gas of N₂ and CH₄ in Titan's upper atmosphere and subsequent escape is compared to Cassini density measurements and continuum model results. Normalizing the densities and temperatures at the lower boundary of the simulation region ($r_o = 3685$ km, $T_o \sim 132$ K & $T_o \sim 161$ K) to recent INMS data [3] we found that the increase in the N₂ densities measured when Titan is in Saturn's plasma sheet results in a decrease in the H₂ densities above the exobase and a 10% decrease in the escape rate compared to simulations using N₂ densities measured when Titan is outside the plasma sheet.

1. Introduction

A wealth of measurements on the structure of Titan's upper atmosphere has been provided by the Cassini spacecraft during its several flybys. However interpreting the globally averaged densities of the major atmospheric components, N₂, CH₄ and H₂, remains the subject of much discussion, e.g. Ref. 1. Continuum models of hydrodynamic escape and models the diffusion of CH₄ and H₂ through a static N₂ background gas require significant escape fluxes to match the Cassini data [1]. In contrast molecular models of thermal escape have reproduced Cassini density measurements of N₂ and CH₄ without requiring large escape rates [2]. In this study a similar molecular model to that discussed in Ref. 2 is used to consider the diffusion and escape of H₂ in a static background gas of N₂ and CH₄ and the results are compared with Cassini density measurements and the continuum models of diffusion and escape.

2. Escape and Jeans flux

A molecule has the highest probability to escape from a planet in the exosphere region where molecular collisions are rare. The lower boundary to this region is the exobase which is defined as the

radial distance where molecules can travel an atmospheric scale height without suffering a collision. At the exobase distance r_x the theoretical Jeans escape flux F_J is evaluated as a function of temperature T_x and density n_x where λ_x is the Jeans parameter at the exobase. The Jeans parameter is the ratio of the gravitational energy (GMm/r_x) to the thermal energy (kT_x) at the exobase where G is the gravitational constant, M is the planet mass, m is the molecular mass and k is the Boltzmann constant. At Titan the exobase distance derived from N₂ is $r_x \sim 4075$ km and the Jeans parameters are ~ 50 , 30 and 4 for N₂, CH₄ and H₂ respectively.

$$\lambda_x = GMm/kT_x r_x \quad (1)$$

$$F_J = \frac{1}{4} n_x \left(\frac{8kT_x}{\pi m} \right) (1 + \lambda_x) \exp[-\lambda_x] \quad (2)$$

3. Cassini density data

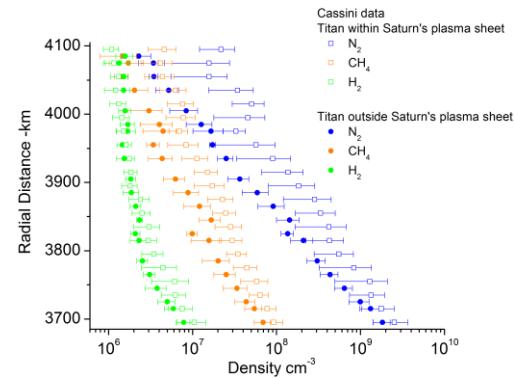


Figure 1: Globally averaged INMS density data for Titan when located within and out of Saturn's plasma sheet.

The Cassini density data obtained by the Ion Neutral Mass Spectrometer (INMS) in Titan's upper atmosphere is considered most accurate for radial

distances between ~ 3500 km and 4075 km (Fig 1). In addition the density data is highly variable. For example, enhancements seen in the N_2 densities measurements vs. r when Titan orbits within Saturn's plasma sheet are suggestive of non-thermal heating processes occurring in the upper atmosphere [3]. Earlier we showed the continuum models of orbitally averaged data sets required escape rates that were much too large for N_2 and CH_4 [2] for a specific n_o and T_o at the lower boundary r_o .

5. Summary and Conclusions

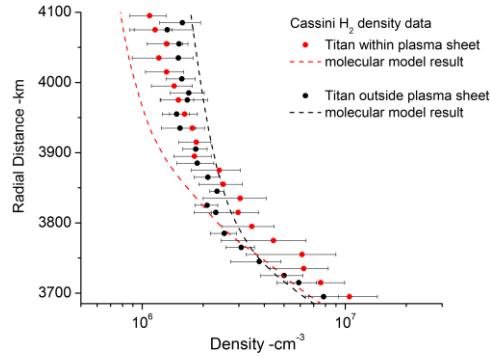


Figure 2: Comparison of molecular simulation results (dashed lines) to averaged INMS density data for H_2 for Titan orbits within (open red triangles) and outside (open black circles) of Saturn's plasma sheet.

A set of molecular simulations are performed for the diffusion and escape of H_2 from Titan's atmosphere using hydrostatic density profiles of N_2 and CH_4 for $r_o = 3685$ km and $T_o = (132 \& 165)$ K from fits to the INMS density data obtained while Titan orbited within and outside Saturn's plasma sheet (Fig. 2). The molecular simulations describe collisions with variable cross section sizes based on the relative velocity between molecules, and allow for the exchange of rotational energy with translation energy. For the temperatures given above T_o the molecular model obtains H_2 escape rates of $\sim 1.1 \times 10^{28} \text{ s}^{-1}$ and $1.0 \times 10^{28} \text{ s}^{-1}$, $\sim 1.5 \cdot F_J$ and $1.4 \cdot F_J$ respectively. The above molecular simulations do not fit the averaged INMS data points, however the simulation for conditions when Titan is outside the plasma sheet obtains H_2 densities roughly within the variations of the data. Furthermore H_2 is produced by CH_4 photo-dissociation on the sunlit side of Titan therefore a globally averaged data set of H_2 densities for day and night flybys may underestimate the H_2 densities at

the upper most altitudes. While the INMS averaged densities for N_2 and CH_4 increase when Titan orbits in the plasma sheet the H_2 densities are indistinguishable. Roughly consistent with the INMS data the molecular simulations show a decrease in H_2 densities with an increase in temperature and density of the N_2 background gas (Fig. 2).

Acknowledgements

Financial support is provided by NASA through Planetary Atmospheres Program (Grant NNX09AB68G) and by NASA's Cassini Mission at the Jet Propulsion Laboratory. Special thanks to Joseph Westlake (University of Texas at San Antonio) and Jared Bell (Southwest Research Institute) for the INMS data sets.

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