

Retrieval of the fluid Love number k_2 in transit light curves: a feasibility study

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Abstract

With about 4000 confirmed detected exoplanets, the characterization of their interior could potentially unveil information on their formation, migration, and habitability. The Love number k_2 , when hydrostatic equilibrium of the interior is assumed, is an indication of mass concentration towards the body's center. Hence, it helps to further constrain the interior when combined with planetary mass and mean radius. We first summarize the planetary shape model which allows the retrieval of k_2 from transit light curves. Second, we apply our model to synthetic data of WASP-121b and show that a precision < 90 ppm/min is required to reliably retrieve k_2 with present understanding of stellar limb darkening. Therefore we improve recent results based on ellipsoidal shape models.

1. Introduction

Knowledge of the planetary mass and mean radius is not sufficient to infer the interior structure, since the problem is degenerate with radial density profiles [1]. Hot Jupiters orbiting close to their Roche limit undergo strong tidal deformations. This modifies their shape from spherical to more complicated ones. Assuming hydrostatic equilibrium of the interior, the shape is a direct function of the fluid Love numbers k_j , of degree j [2]. In particular, k_2 is an indication of mass concentration towards the body's center, providing additional information about the interior [3]. As a result of these deformations, the stellar eclipsed area during transit will differ from a transiting sphere, modifying the transit light curve. We briefly summarize the planetary shape model (Section 2), and apply it to synthetic data of WASP-121b (Section 3). This leads to constraints on the required noise level and limb darkening precision to reliably retrieve k_2 .

2. Shape model

We assume a spherical star, a circular orbit, synchronous rotation, no interactions between rotation and tides, and absence of non-linear effects in the planetary response to perturbations. The radius at any surface point of colatitude (θ) and latitude (ϕ) is given by Equation (1) [2, 4].

$$r(\theta, \phi) = R_p \left(1 + q \sum_{j=2}^4 h_j P_j(\lambda) \left(\frac{R_p}{d} \right)^{j+1} - \frac{1}{3} h_2 (1 + q) F_p^2 \left(\frac{R_p}{d} \right)^3 P_2(\cos \theta) \right) \quad (1)$$

where R_p is the planetary mean radius, q is the mass ratio, $h_j = 1 + k_j$ in the hydrostatic assumption, P_j are the Legendre polynomials of degree j , d is the semi-major axis, F_p is the ratio between the orbital and rotational periods, θ is the obliquity, and λ is a geometrical factor.

3. Synthetic data

The parameters assumed are taken from [5,6] while an arbitrary value of $k_2 = 0.5$ is chosen. We considered several white noise levels, σ (ppm/2min), reachable after 10 observed transits of WASP-121b with past, current and future observing facilities, summarized in Table 2.

Table 2: Considered white noise levels

| Facility | σ (ppm/2min) |
|----------------|---------------------|
| JWST (NIRSpec) | 23 |
| Kepler | 45 |
| PLATO | 63 |
| CHEOPS | 71 |
| / | 200 |
| TESS | 360 |

These white noise levels were randomly added to create synthetic light curves.

We retrieve the inclination, epoch, limb darkening, semi-major axis, planetary mean radius, and k_2 .

Uniform priors were applied except for the stellar limb darkening coefficients, where two cases were considered: Gaussian priors with standard deviations (σ_{LDC}) of 0.01 and 0.005. In doing so, we can compare our results to recently published performance with ellipsoidal shape models [7].

4. Results

We present in Figure 1 [8] the mean and standard deviation of the measured k_2 , for both considered priors on the limb darkening coefficients. We also show the posterior distributions of k_2 for all light curves realizations to assess the quality of the parameter estimation. The measured value must be precise and accurate to confidently say that the model can retrieve k_2 . Thus, we require a precision of at least 2σ and a relative error $\leq 5\%$.

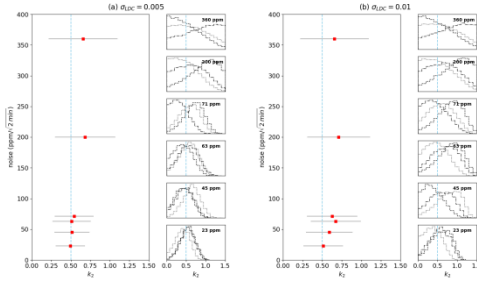


Fig 1. (a) Average values of the three realizations as a function of the noise level, and k_2 posterior distributions, for $\sigma_{LDC} = 0.005$; (b) Same as (a) but for $\sigma_{LDC} = 0.01$.

For a well constrained stellar limb darkening, we get a least a 2σ detection with a relative error $< 5\%$ for noise levels up to 63 ppm/2min. At 71 ppm/2min we also obtain a 2σ detection of k_2 , but with a relative error of about 9%. For higher noise levels, the relative error drastically drops and the posterior distributions of k_2 widen and flatten, covering the whole physical range [0; 1.5] (see Figure 1(a)). When the accuracy on the limb darkening coefficients decreases (Figure 1(b)), we are able to reliably recover k_2 with a noise level of 23 ppm/2min only. For higher noise values, the precision and relative error decidedly decrease.

5. Summary and Conclusions

The proposed three-dimensional shape model allows direct fitting of the true planetary mean radius, and fluid Love number k_2 . Considering the close-in hot Jupiter WASP-121b as a test case, we showed that a noise level ≤ 65 ppm/2min (equivalently 90 ppm/min) and a standard deviation < 0.01 on the limb darkening coefficients are required to reliably retrieve k_2 . We thereby improve the performance of the three-axis ellipsoidal shape models by almost a factor 2. A careful treatment of noise sources is critical to achieve reliable measurements of k_2 , and any improvement on stellar limb darkening would increase the performances summarized above. Such measurements would allow to further constrain exoplanetary internal structures by comparing the measured k_2 to theoretical interior model expectations.

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