

# Giant Planet Evolution: The Effect of Convection and Mixing

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## Abstract

We model the long-term evolution of giant planets accounting for the change in the compositional gradient with time. Core erosion is modeled by convective-mixing using both the Ledoux and Schwarzschild criteria for convection. We find that in some cases compositional gradients prevent convective mixing, and as a result, the assumption of an adiabatic interior is no longer valid. In other cases, mixing leads to layered-convection, which results in a stair-like internal structure and a slower cooling [2]. In addition, the process of mixing (if it occurs) enriches the gaseous envelope in heavy elements from the core. These have a direct effect on the planetary evolution, and therefore on the planetary radius and luminosity. We suggest that the memory of the primordial internal structure remains even after billions of years.

## 1. Introduction

The existence of heavy-element cores in gas giant planets and their physical properties are important for understanding giant planet formation, evolution, and internal structure. Typically, evolution models assume a compositional distribution that does not change with time. This assumption, however, is not necessarily correct. It is possible that the heavy-element core becomes soluble in the gaseous envelope [4]. Recent studies of the solubility of analogous phases have shown that heavy elements can dissolve in liquid metallic hydrogen in planetary interior conditions (e.g. [6]).

## 2. Convection

We use a planetary evolution code [1,5] that models convection by using the Ledoux criterion:

$$\nabla_R > \nabla_A + \nabla_{\text{Ledoux}} \quad (1)$$

where  $\nabla_A$  and  $\nabla_R$  are the adiabatic and radiative gradients, respectively. The compositional gradient of material  $X$  of type  $j$  contributes the convection via

$$\nabla_{\text{Ledoux}} = \sum_j \frac{\partial \ln T}{\partial X_j} \frac{\partial X_j}{\partial \ln p}. \quad (2)$$

For  $\nabla_{\text{Ledoux}} = 0$  the Ledoux convection criterion converges to the Schwarzschild criterion.

When mixing of materials is considered, we use the compositional balance equation allowing for convective-mixing-diffusion by:

$$\frac{\partial X_j}{\partial t} = - \frac{\partial F_j}{\partial m}. \quad (3)$$

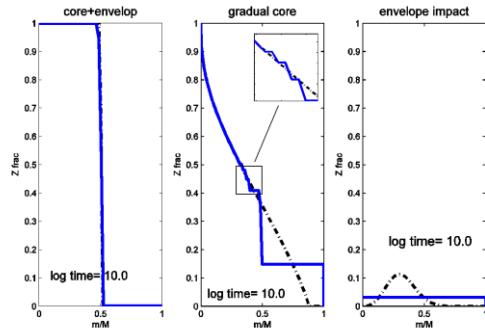
The particle flux of the  $j^{\text{th}}$  species  $F_j$  is proportional to the abundance gradient, and is determined by the Mixing Length Recipe (MLR) [3,1].

## 3. Results

During the planetary evolution, a "competition" between the stabilizing effect of the compositional gradient and the un-stabilizing effect of the temperature gradient essentially determines the planetary evolution and the final structure of planet. For example, when using the Ledoux criterion for an initial configuration of core + envelope, convection cannot occur in the core-envelope boundary which acts as a "bottle neck" for the heat transfer. This leads to a much warmer interior and a slower cooling rate. On the other hand, an initial structure with a gradual distribution of the heavy elements can evolve into an interior with layered-convection, where several convective regions in the planet are separated

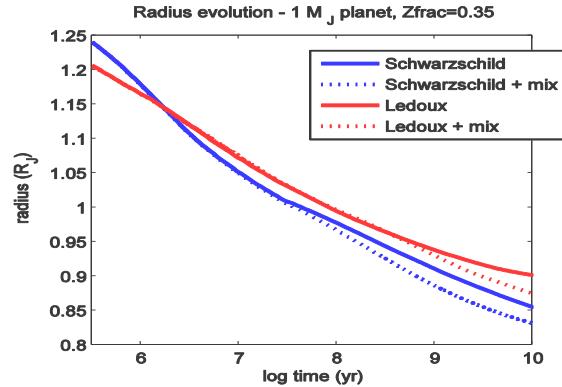
by thin diffusive layers, i.e., a stair-like internal structure. The cooling rate of the planet is controlled by this structure, which affects also the heavy element enrichment of the envelope.

Figure 1 presents the heavy element distribution after  $10^{10}$  years of evolution, for different initial configurations. For all cases the Ledoux criterion is used and mixing is simulated using MLR.



**Figure 1:** Heavy element mass fraction vs. normalized planetary mass for  $1 M_J$  planets with different initial distributions. Initial structure (dashed dotted) and a structure after  $10^{10}$  years of evolution (solid) are presented. **Left:** pure heavy element core and gaseous envelope; **Center:** gradual distribution; **Right:** local heavy element "cloud".

Figure 2 shows the effect of the mixing and convection criterion on the radius' evolution for a  $1 M_J$  planet with a primordial gradual composition distribution (as in Fig.1 center).



**Figure 2:** Radius' evolution of  $1 M_J$  planet with  $z=0.35$  assuming a gradual initial distribution, for different convection criteria (blue – Schwarzschild, red – Ledoux), with (dotted) and without (solid) elements mixing.

As expected, for the Ledoux criterion (red curves) convection regions are limited due to the stabilizing compositional gradient. This leads to a slower heat transfer rate and slower contraction, and therefore, a larger radius. When only the temperature gradient is considered (blue curves), the cooling is faster, leading to a smaller radius. When mixing is allowed (dotted curves) the heavy elements mix within the gaseous envelope leading to smaller radii after about  $10^8$  years. The planetary radius for a stair-like internal structure (red dotted) contracts in the same rate (or even faster) than the case with a gradual distribution that is held fixed (red solid).

## 4. Summary and Conclusions

- The primordial internal structure of a giant planet has an important influence on the long-term evolution even after billions of years.
- Convection controls the heavy-element distribution and vice versa, as a result, slightly different initial configurations can lead to very different evolutions and final structures.

## References

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